

ROBOOP, A Robotics Object Oriented Package in C++ Reference Manual

1.31

Generated by Doxygen 1.5.1

Thu Dec 14 08:52:17 2006

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Chapter 1

ROBOOP, A Robotics Object Oriented Package in C++ Hierarchical Index

1.1 ROBOOP, A Robotics Object Oriented Package in C++ Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

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Robot	95
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Spl_path	119
Spl_Quaternion	121
Stewart	122
Trajectory_Select	139

Chapter 2

ROBOOP, A Robotics Object Oriented Package in C++ Class Index

2.1 ROBOOP, A Robotics Object Oriented Package in C++ Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Clik (Handle Closed Loop Inverse Kinematics scheme)	7
Computed_torque_method (Computer torque method controller class)	11
Config (Handle configuration files)	14
Control_Select (Select controller class)	16
Data (Basic data element used in Config class)	18
Dynamics (Dynamics simulation handling class)	19
GNUcurve (Object for one curve)	25
Impedance (Impedance controller class)	26
IO_matrix_file (Read and write data at every iterations in a file)	34
Link (Link definitions)	36
LinkStewart (LinkStewart definitions)	41
mRobot (Modified DH notation robot class)	58
mRobot_min_para (Modified DH notation and minimal inertial parameters robot class)	67
New_dynamics (This is an example of customize Dynamics class)	75
Plot2d (2d plot object)	78
Plot3d (3d plot object)	80
Plot_file (Creates a graphic from a data file)	81
Proportional_Derivative (Proportional derivative controller class)	82

Quaternion (Quaternion class definition)	85
Resolved_acc (Resolved rate acceleration controller class)	92
Robot (DH notation robot class)	95
Robot_basic (Virtual base robot class)	105
Spl_cubic (Natural cubic splines class)	117
Spl_path (Cartesian or joint space trajectory)	119
Spl_Quaternion (Cubic quaternions spline)	121
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Chapter 3

ROBOOP, A Robotics Object Oriented Package in C++ File Index

3.1 ROBOOP, A Robotics Object Oriented Package in C++ File List

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config.cpp (Configuration class functions)	149
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demo.cpp (A demo file)	157
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puma560akb_no_motor.m	??
quaternion.cpp (Quaternion functions)	172
quaternion.h (Quaternion class)	177
robot.cpp (Initialisation of differents robot class)	183
robot.h (Robots class definitions)	187
rtest.cpp (A test file)	191
sensitiv.cpp (Delta torque (linearized dynamics))	193
stanford_no_motor.m	??
stewart.cpp (Initialisation of Stewart platform class)	194
stewart.h (Stewart class definitions)	195
trajectory.cpp (Trajectory member functions)	196
trajectory.h (Header file for trajectory generation class)	197
utils.cpp (Utility functions)	199
utils.h (Utility header file)	202

Chapter 4

ROBOOP, A Robotics Object Oriented Package in C++ Class Documentation

4.1 Clik Class Reference

```
#include <clik.h>
```

4.1.1 Detailed Description

Handle Closed Loop Inverse Kinematics scheme.

Definition at line 87 of file clik.h.

Public Member Functions

- [Clik](#) ()
- [Clik](#) (const [Robot](#) &robot_, const DiagonalMatrix &Kp_, const DiagonalMatrix &Ko_, const Real eps_=0.04, const Real lambda_max_=0.04, const Real dt=1.0)

Constructor.

- [Clik](#) (const [mRobot](#) &mrobot_, const DiagonalMatrix &Kp_, const DiagonalMatrix &Ko_, const Real eps_=0.04, const Real lambda_max_=0.04, const Real dt=1.0)

Constructor.

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- [Clik](#) (const [mRobot_min_para](#) &mrobot_min_para_, const DiagonalMatrix &Kp_, const DiagonalMatrix &Ko_, const Real eps_=0.04, const Real lambda_max_=0.04, const Real [dt](#)=1.0)

Constructor.

- [Clik](#) (const [Clik](#) &x)

Copy constructor.

- [~Clik](#) ()
- [Clik](#) & [operator=](#) (const [Clik](#) &x)

Overload = operator.

- void [q_qdot](#) (const [Quaternion](#) &qd, const ColumnVector &pd, const ColumnVector &pddot, const ColumnVector &wd, ColumnVector &[q](#), ColumnVector &[qp](#))

Obtain joints position and velocity.

Private Member Functions

- int [endeff_pos_ori_err](#) (const ColumnVector &pd, const ColumnVector &pddot, const [Quaternion](#) &qd, const ColumnVector &wd)

Obtain end effector position and orientation error.

Private Attributes

- Real [dt](#)

Time frame.

- Real [eps](#)

Range of singular region in Jacobian DLS inverse.

- Real [lambda_max](#)

Damping factor in Jacobian DLS inverse.

- short [robot_type](#)

Robot type used.

- [Robot](#) robot

Robot instance.

- [mRobot mrobot](#)
mRobot instance.
- [mRobot_min_para mrobot_min_para](#)
mRobot_min_para instance.
- DiagonalMatrix [Kp](#)
Position error gain.
- DiagonalMatrix [Ko](#)
Orientation error gain.
- ColumnVector [q](#)
Clik joint position.
- ColumnVector [qp](#)
Clik joint velocity.
- ColumnVector [qp_prev](#)
Clik previous joint velocity.
- ColumnVector [Kpep](#)
Kp times position error.
- ColumnVector [Koe0Quat](#)
Ko times orientation error (quaternion vector part).
- ColumnVector [v](#)
Quaternion vector part.

4.1.2 Member Function Documentation

4.1.2.1 void Clik::q_qdot (const [Quaternion](#) & *qd*, const ColumnVector & *pd*, const ColumnVector & *pdd*, const ColumnVector & *wd*, ColumnVector & *q_*, ColumnVector & *qp_*)

Obtain joints position and velocity.

Parameters:

qd,: Desired eff orientatio in base frame.

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pd,: Desired eff position in base frame.
pdd,: Desired eff velocity in base frame.
wd,: Desired eff angular velocity in base frame.
*q*_,: Output joint position.
*qp*_,: Output joint velocity.

Definition at line 269 of file `clik.cpp`.

References `CLICK_DH`, `CLICK_mDH`, `CLICK_mDH_min_para`, `dt`, `endeff_pos_ori_err()`, `eps`, `Integ_Trap()`, `Robot_basic::jacobian_DLS_inv()`, `Koe0Quat`, `Kpep`, `lambda_max`, `mrobot`, `mrobot_min_para`, `q`, `qp`, `qp_prev`, `robot`, `robot_type`, `Robot_basic::set_q()`, and `v`.

4.1.2.2 `int Clik::endeff_pos_ori_err (const ColumnVector & pd, const ColumnVector & pdd, const Quaternion & qqqd, const ColumnVector & wd)` [`private`]

Obtain end effector position and orientation error.

Parameters:

pd,: Desired eff position in base frame.
pdd,: Desired eff velocity in base frame.
qqqd,: Desired eff orientation in base frame.
wd,: Desired eff angular velocity in base frame.

Definition at line 224 of file `clik.cpp`.

References `CLICK_DH`, `CLICK_mDH`, `CLICK_mDH_min_para`, `Robot_basic::kine()`, `Ko`, `Koe0Quat`, `Kp`, `Kpep`, `mrobot`, `mrobot_min_para`, `q`, `robot`, `robot_type`, `Quaternion::s()`, `Robot_basic::set_q()`, `Quaternion::v()`, and `x_prod_matrix()`.

Referenced by `q_qdot()`.

4.2 Computed_torque_method Class Reference

```
#include <controller.h>
```

4.2.1 Detailed Description

Computer torque method controller class.

The dynamic model of a robot manipulator can be expressed in joint space as

$$B(q)\ddot{q} + C(q, \dot{q})\dot{q} + D\dot{q} + g(q) = \tau - J^T(q)f$$

The driving torques can be expressed as

$$\tau = B(q)(\ddot{q}_d + K_d(\dot{q}_d - \dot{q}) + K_p(q_d - q)) + C(q, \dot{q})\dot{q} + D\dot{q} + g(q) + J^T(q)f$$

where K_p , K_d are diagonal positive definite matrix.

Definition at line 220 of file controller.h.

Public Member Functions

- [Computed_torque_method](#) (const short dof=1)
Constructor.
- [Computed_torque_method](#) (const [Robot_basic](#) &robot, const DiagonalMatrix &Kp, const DiagonalMatrix &Kd)
Constructor.
- ReturnMatrix [torque_cmd](#) ([Robot_basic](#) &robot, const ColumnVector &qd, const ColumnVector &qpd, const ColumnVector &qppd)
Output torque.
- short [set_Kd](#) (const DiagonalMatrix &Kd)
Assign the velocity error gain matrix $K_d(i, i)$.
- short [set_Kp](#) (const DiagonalMatrix &Kp)
Assign the position error gain matrix $K_p(i, i)$.

Private Attributes

- int [dof](#)
Degree of freedom.

- ColumnVector [q](#)
Robot joints positions.
- ColumnVector [qp](#)
Robot joints velocity.
- ColumnVector [qpp](#)
Robot joints acceleration.
- ColumnVector [zero3](#)
 3×1 zero vector.
- DiagonalMatrix [Kp](#)
Position error gain.
- DiagonalMatrix [Kd](#)
Velocity error gain.

4.2.2 Member Function Documentation

4.2.2.1 short Computed_torque_method::set_Kd (const DiagonalMatrix & Kd_)

Assign the velocity error gain matrix $K_d(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not $dof \times dof$.

Definition at line 571 of file controller.cpp.

References dof, Kd, and WRONG_SIZE.

Referenced by Computed_torque_method().

4.2.2.2 short Computed_torque_method::set_Kp (const DiagonalMatrix & Kp_)

Assign the position error gain matrix $K_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not $dof \times dof$.

Definition at line 588 of file controller.cpp.

References `dof`, `Kp`, and `WRONG_SIZE`.

Referenced by `Computed_torque_method()`.

4.3 Config Class Reference

```
#include <config.h>
```

4.3.1 Detailed Description

Handle configuration files.

Definition at line 97 of file config.h.

Public Member Functions

- [Config](#) (const bool [bPrintErrorMessages](#)=true)
Constructor.
- short [read_conf](#) (std::ifstream &inconffile)
- void [clear](#) ()
Clear the data buffer.
- void [print](#) ()
Print the configuration data.
- bool [section_exists](#) (const std::string §ion) const
- bool [parameter_exists](#) (const std::string §ion, const std::string ¶meter) const
- template<typename T> bool [select](#) (const std::string §ion, const std::string ¶meter, T &value) const
Get a parameter data, of a certain section, into the string value.
- short [write_conf](#) (std::ofstream &outconffile, const std::string &file_title, const int space_between_column)
- template<typename T> bool [add](#) (const std::string §ion, const std::string ¶meter, const T &value)
Added the value(string) of the parameter in the section in the configuration data. The functions will added the parameter and the section if it does not already exist.

Private Attributes

- [Conf_data](#) [conf](#)
Data store from/to configuration file.

- bool [bPrintErrorMessages](#)
Print error messages on stderr.

4.3.2 Member Function Documentation

4.3.2.1 `template<typename T> bool Config::select (const std::string & section, const std::string & parameter, T & value) const` `[inline]`

Get a parameter data, of a certain section, into the string value.

Returns:

false if the data can not be found and true otherwise.

Definition at line 109 of file config.h.

References [conf](#).

4.4 Control_Select Class Reference

```
#include <control_select.h>
```

4.4.1 Detailed Description

Select controller class.

This class contains an instance of each controller class. The active controller will be selected when reading a controller file. "type" value correspond to the active controller, ex:

- type = NONE : no controller selected
- type = PD : Proportional Derivative
- type = CTM : Computer Torque Method
- type = RRA : Resolved Rate Acceleration
- type = IMP : [Impedance](#)

Bellow is an exemple of RRA configuration file (more info on configuration file in [config.h/cpp](#)):

```
[CONTROLLER]

type:    RESOLVED_RATE_ACCELERATION
dof:     6

[GAINS]

Kvp:     500.0
Kpp:     5000.0
Kvo:     500.0
Kpo:     5000.0
```

Definition at line 100 of file control_select.h.

Public Member Functions

- [Control_Select](#) ()
Constructor.
- **Control_Select** (const std::string &filename)
- int [get_dof](#) ()
Return the degree of freedom.
- void **set_control** (const std::string &filename)

Public Attributes

- [Proportional_Derivative](#) `pd`
- [Computed_torque_method](#) `ctm`
- [Resolved_acc](#) `rra`
- [Impedance](#) `impedance`
- short [type](#)
Type of controller: PD, CTM,...
- short [space_type](#)
JOINT_SPACE or CARTESIAN_SPACE.
- `std::string` [ControllerName](#)
Controller name.

Private Attributes

- int [dof](#)
Degree of freedom.

4.5 Data Struct Reference

```
#include <config.h>
```

4.5.1 Detailed Description

Basic data element used in [Config](#) class.

Definition at line 87 of file config.h.

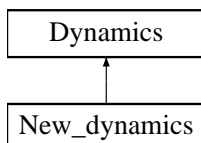
Public Attributes

- std::string [section](#)
- std::string [parameter](#)
- std::string [value](#)

4.6 Dynamics Class Reference

```
#include <dynamics_sim.h>
```

Inheritance diagram for Dynamics::



4.6.1 Detailed Description

[Dynamics](#) simulation handling class.

Definition at line 60 of file `dynamics_sim.h`.

Public Member Functions

- [Dynamics](#) ([Robot_basic](#) *robot_)
Constructor.
- virtual [~Dynamics](#) ()
- void [set_dof](#) ([Robot_basic](#) *robot_)
Set the degree of freedom.
- short [set_controller](#) (const [Control_Select](#) &x)
Set the control variable from the [Control_Select](#) reference.
- short [set_trajectory](#) (const [Trajectory_Select](#) &x)
Set the path_select variable from the [Trajectory_Select](#) reference.
- ReturnMatrix [set_robot_on_first_point_of_splines](#) ()
Set the robot on first point of trajectory.
- void [set_time_frame](#) (const int nsteps)
Set the number of iterations.
- void [set_final_time](#) (const double tf)
Set the file time.

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- void [reset_time](#) ()
Set the simulation time to the initial time.
- void [Runge_Kutta4_Real_time](#) ()
Runge Kutta solver for real time.
- void [Runge_Kutta4](#) ()
Runge Kutta solver.
- virtual void [plot](#) ()
Virtual plot functions.
- ReturnMatrix [xdot](#) (const Matrix &xin)
Obtain state derivative.

Static Public Member Functions

- static [Dynamics](#) * [Instance](#) ()
A pointer to [Dynamics](#) instance. Pointer is 0 if there is no instance (logic done in Constructor).

Public Attributes

- bool [first_pass_Kutta](#)
First time in all Runge_Kutta4 functions.
- int [ndof](#)
Degree of freedom.
- int [dof_fix](#)
Degree of freedom + virtual link.
- int [nsteps](#)
Numbers of iterations between.
- double [h](#)
Runge Kutta temporary variable.
- double [h2](#)
Runge Kutta temporary variable.

- double `time`
Time during simulation.
- double `to`
Initial simulation time.
- double `tf`
Final time used in Runge_Kutta4_Real_time.
- double `tf_cont`
Final time used in Runge_Kutta4.
- double `dt`
Time frame.
- Matrix `k1`
Runge Kutta temporary variable.
- Matrix `k2`
Runge Kutta temporary variable.
- Matrix `k3`
Runge Kutta temporary variable.
- Matrix `k4`
Runge Kutta temporary variable.
- Matrix `x`
Stated vector obtain in Runge Kutta functions.
- Matrix `xd`
Statd vector derivative obtaint in xdot function.
- ColumnVector `q`
Joints positions.
- ColumnVector `qp`
Joints velocities.
- ColumnVector `qpp`
Joints accelerations.

- [ColumnVector qd](#)
Desired joints positions.
- [ColumnVector qpd](#)
Desired joints velocities.
- [ColumnVector qppd](#)
Desired joints accelerations.
- [ColumnVector tau](#)
Controller output torque.
- [ColumnVector pd](#)
Desired end effector cartesian position.
- [ColumnVector ppd](#)
Desired end effector cartesian velocity.
- [ColumnVector pppd](#)
Desired end effector cartesian acceleration.
- [ColumnVector wd](#)
Desired end effector cartesian angular velocity.
- [ColumnVector wpd](#)
Desired end effector cartesian angular acceleration.
- [Quaternion quatd](#)
Desired orientation express by a quaternion.
- [Control_Select control](#)
Instance of [Control_Select](#) class.
- [Trajectory_Select path_select](#)
Instance of [Trajectory_Select](#) class.
- [Robot_basic * robot](#)
Pointer on [Robot_basic](#) class.

Static Public Attributes

- static [Dynamics](#) * [instance](#)
Static pointer on [Dynamics](#) class.

4.6.2 Member Function Documentation

4.6.2.1 void Dynamics::set_dof ([Robot_basic](#) * robot_)

Set the degree of freedom.

Obtain the degree of freedom from [Robot_basic](#) pointer. Some vectors will be resize with new current dof value.

Definition at line 109 of file dynamics_sim.cpp.

References dof_fix, first_pass_Kutta, Robot_basic::get_dof(), Robot_basic::get_fix(), ndof, q, qd, qp, qpd, qpp, qppd, robot, and tau.

4.6.2.2 ReturnMatrix Dynamics::set_robot_on_first_point_of_splines ()

Set the robot on first point of trajectory.

Assigned the robot joints position to the first point of the trajectory if the latter is expressed in joint space, or assigned the robot joints position via inverse kinematics if the trajectory is expressed in cartesian space. The function return a message on the console if the format of the trajectory file is incorrect.

Definition at line 190 of file dynamics_sim.cpp.

References CARTESIAN_SPACE, Spl_path::get_final_time(), Robot_basic::get_q(), Robot_basic::inv_kin(), JOINT_SPACE, ndof, Spl_path::p_pdot(), Spl_path::p_pdot_pddot(), Trajectory_Select::path, Trajectory_Select::path_quat, path_select, pd, ppd, pppd, q, qd, qpd, Spl_Quaternion::quat_w(), quatd, Quaternion::R(), robot, Robot_basic::set_q(), tf_cont, Trajectory_Select::type, and wd.

Referenced by Runge_Kutta4(), and Runge_Kutta4_Real_time().

4.6.2.3 ReturnMatrix Dynamics::xdot (const Matrix & x)

Obtain state derivative.

Parameters:

- x : state vector (joint speed and joint velocity).

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The controller torque is applied if any controller has been selected, then the joint acceleration is obtained.

Definition at line 252 of file dynamics_sim.cpp.

References Robot_basic::acceleration(), CARTESIAN_SPACE, control, Control_Select::ctm, CTM, dof_fix, dt, JOINT_SPACE, ndof, Spl_path::p_pdot(), Spl_path::p_pdot_pddot(), Trajectory_Select::path, Trajectory_Select::path_quat, path_select, pd, Control_Select::pd, PD, plot(), ppd, pppd, q, qd, qp, qpd, qpp, qppd, Spl_Quaternion::quat_w(), quatd, robot, Control_Select::rra, RRA, Robot_basic::set_q(), Robot_basic::set_qp(), tau, time, Resolved_acc::torque_cmd(), Computed_torque_method::torque_cmd(), Proportional_Derivative::torque_cmd(), Trajectory_Select::type, Control_Select::type, wd, wpd, and xd.

Referenced by Runge_Kutta4(), and Runge_Kutta4_Real_time().

4.7 GNUcurve Class Reference

```
#include <gnugraph.h>
```

4.7.1 Detailed Description

Object for one curve.

Definition at line 127 of file gnugraph.h.

Public Member Functions

- **GNUcurve** (const std::vector< double > &x, std::vector< double > &y, const std::string &label="", [LineType_en](#) enLineType=LINES)
- [GNUcurve](#) (void)
Constructor.
- void [dump](#) (void)
Method to dump the content of a curve to stdout.

Public Attributes

- std::vector< double > [vdX](#)
- std::vector< double > [vdY](#)
- std::string [clabel](#)
string defining the curve label for the legend
- [LineType_en](#) enLineType
Line type.

4.8 Impedance Class Reference

```
#include <controller.h>
```

4.8.1 Detailed Description

[Impedance](#) controller class.

The implementation of the impedance controller is made of two sections: the first one is the generation of a compliance trajectory and the second one uses a position controller to ensure the end effector follows the compliance trajectory (We recommend to use the resolved acceleration controller scheme, implemented in the class [Resolved_acc](#)).

This class generates a compliance path given by the translational and the rotational impedance.

$$M_p \ddot{\tilde{p}} + D_p \dot{\tilde{p}} + K_p \tilde{p} = f$$

$$M_o \dot{\tilde{\omega}} + D_o \tilde{\omega} + K_o' \tilde{v} = n$$

where $\tilde{x} = x_c - x_d$ and v is the vector part of the quaternion representing the orientation error between the compliant and desired frame. The orientation error can also be expressed by rotation matrix, $\tilde{R} = R_d^T R_c$. The quaternion mathematics are implemented in the [Quaternion](#) class. The index c and d denote the compliance and the desired respectively.

The impedance parameters M_p , D_p , K_p , M_o , D_o and K_o are 3×3 diagonal positive definite matrices.

Definition at line 91 of file controller.h.

Public Member Functions

- [Impedance](#) ()
Constructor.
- [Impedance](#) (const [Robot_basic](#) &robot, const DiagonalMatrix &Mp_, const DiagonalMatrix &Dp_, const DiagonalMatrix &Kp_, const DiagonalMatrix &Mo_, const DiagonalMatrix &Do_, const DiagonalMatrix &Ko_)
Constructor.
- short [set_Mp](#) (const DiagonalMatrix &Mp_)
Assign the translational impedance inertia matrix M_p .
- short [set_Mp](#) (const Real MP_i, const short i)
Assign the translational impedance inertia term $M_p(i, i)$.

- short [set_Dp](#) (const DiagonalMatrix &Dp_)
Assign the translational impedance damping matrix D_p .
- short [set_Dp](#) (const Real Dp_i, const short i)
Assign the translational impedance damping term $D_p(i, i)$.
- short [set_Kp](#) (const DiagonalMatrix &Kp_)
Assign the translational impedance stiffness matrix K_p .
- short [set_Kp](#) (const Real Kp_i, const short i)
Assign the translational impedance stiffness term $K_p(i, i)$.
- short [set_Mo](#) (const DiagonalMatrix &Mo_)
Assign the rotational impedance inertia matrix M_o .
- short [set_Mo](#) (const Real Mo_i, const short i)
Assign the rotational impedance inertia term $M_o(i, i)$.
- short [set_Do](#) (const DiagonalMatrix &Do_)
Assign the rotational impedance damping matrix D_o .
- short [set_Do](#) (const Real Do_i, const short i)
Assign the rotational impedance damping term $D_o(i, i)$.
- short [set_Ko](#) (const DiagonalMatrix &Ko_)
Assign the rotational impedance stiffness matrix K_o .
- short [set_Ko](#) (const Real Ko_i, const short i)
Assign the rotational impedance stiffness term $K_o(i, i)$.
- short [control](#) (const ColumnVector &pdp, const ColumnVector &pdp, const ColumnVector &pd, const ColumnVector &wdp, const ColumnVector &wd, const [Quaternion](#) &qd, const ColumnVector &f, const ColumnVector &n, const Real dt)
Generation of a compliance trajectory.

Public Attributes

- [Quaternion](#) qc
Compliant frame quaternion.

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- [Quaternion qcp](#)
Compliant frame quaternion derivative.
- [Quaternion qcp_prev](#)
Previous value of qcp.
- [Quaternion qcd](#)
Orientation error (between compliant and desired frame) quaternion.
- [Quaternion quat](#)
Temporary quaternion.
- [ColumnVector pc](#)
Compliant position.
- [ColumnVector pcp](#)
Compliant velocity.
- [ColumnVector pcpp](#)
Compliant acceleration.
- [ColumnVector pcp_prev](#)
Previous value of pcp.
- [ColumnVector pcpp_prev](#)
Previous value of pcpp.
- [ColumnVector pcd](#)
Difference between pc and desired position.
- [ColumnVector pcdp](#)
Difference between pcp and desired velocity.
- [ColumnVector wc](#)
Compliant angular velocity.
- [ColumnVector wcp](#)
Compliant angular acceleration.
- [ColumnVector wcp_prev](#)
Previous value of wcp.

- ColumnVector [wcd](#)
Difference between w_c and desired angular velocity.

Private Attributes

- DiagonalMatrix [Mp](#)
Translational impedance inertia matrix.
- DiagonalMatrix [Dp](#)
Translational impedance damping matrix.
- DiagonalMatrix [Kp](#)
Translational impedance stiffness matrix.
- DiagonalMatrix [Mo](#)
Rotational impedance inertia matrix.
- DiagonalMatrix [Do](#)
Rotational impedance damping matrix.
- DiagonalMatrix [Ko](#)
Rotational impedance stiffness matrix.
- Matrix [Ko_prime](#)
Modified rotational impedance stiffness matrix.

4.8.2 Member Function Documentation

4.8.2.1 short Impedance::set_Mp (const DiagonalMatrix & Mp_)

Assign the translational impedance inertia matrix M_p .

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 100 of file controller.cpp.

References [Mp](#), and [WRONG_SIZE](#).

Referenced by [Impedance\(\)](#).

4.8.2.2 `short Impedance::set_Mp (const Real M_p _i, const short i)`

Assign the translational impedance inertia term $M_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 117 of file controller.cpp.

References Mp, and WRONG_SIZE.

4.8.2.3 `short Impedance::set_Dp (const DiagonalMatrix & D_p _)`

Assign the translational impedance damping matrix D_p .

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 133 of file controller.cpp.

References Dp, and WRONG_SIZE.

Referenced by Impedance().

4.8.2.4 `short Impedance::set_Dp (const Real D_p _i, const short i)`

Assign the translational impedance damping term $D_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 150 of file controller.cpp.

References Dp, and WRONG_SIZE.

4.8.2.5 `short Impedance::set_Kp (const DiagonalMatrix & K_p _)`

Assign the translational impedance stiffness matrix K_p .

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 166 of file controller.cpp.

References Kp, and WRONG_SIZE.

Referenced by Impedance().

4.8.2.6 short Impedance::set_Kp (const Real Kp_i, const short i)

Assign the translational impedance stiffness term $K_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 183 of file controller.cpp.

References Kp, and WRONG_SIZE.

4.8.2.7 short Impedance::set_Mo (const DiagonalMatrix & Mo_)

Assign the rotational impedance inertia matrix M_o .

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 199 of file controller.cpp.

References Mo, and WRONG_SIZE.

Referenced by Impedance().

4.8.2.8 short Impedance::set_Mo (const Real Mo_i, const short i)

Assign the rotational impedance inertia term $M_o(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 216 of file controller.cpp.

References Mo, and WRONG_SIZE.

4.8.2.9 short Impedance::set_Do (const DiagonalMatrix & Do_)

Assign the rotational impedance damping matrix D_o .

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Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 232 of file controller.cpp.

References Do, and WRONG_SIZE.

Referenced by Impedance().

4.8.2.10 short Impedance::set_Do (const Real Do_i, const short i)

Assign the rotational impedance damping term $D_o(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 249 of file controller.cpp.

References Do, and WRONG_SIZE.

4.8.2.11 short Impedance::set_Ko (const DiagonalMatrix & Ko_)

Assign the rotational impedance stiffness matrix K_o .

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 265 of file controller.cpp.

References Ko, and WRONG_SIZE.

Referenced by Impedance().

4.8.2.12 short Impedance::set_Ko (const Real Ko_i, const short i)

Assign the rotational impedance stiffness term $K_o(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not 3×3 .

Definition at line 282 of file controller.cpp.

References Ko, and WRONG_SIZE.

4.8.2.13 `short Impedance::control (const ColumnVector & pdpp, const ColumnVector & pdp, const ColumnVector & pd, const ColumnVector & wdp, const ColumnVector & wd, const Quaternion & qd, const ColumnVector & f, const ColumnVector & n, const Real dt)`

Generation of a compliance trajectory.

Parameters:

pdpp,: desired end effector acceleration.
pdp,: desired end effector velocity.
pd,: desired end effector position.
wdp,: desired end effector angular acceleration.
wd,: desired end effector angular velocity.
qd,: desired quaternion.
f,: end effector contact force.
n,: end effector contact moment.
dt,: time frame.

Returns:

short: 0 or WRONG_SIZE if one of the vector input is not 3×1 .

The translational and rotational impedance equations are integrated, with input *f* and *n* to computed \ddot{p}_c and $\dot{\omega}_c$, \dot{p}_c and ω_c , and then *p_c* and *q_c*. The compliant quaternion *q_c* is obtained with the quaternion propagation equations (see [Quaternion](#) class).

The quaternion -q represents exactly the same rotation as the quaternion q. The temporary quaternion, quat, is quatd plus a sign correction. It is customary to choose the sign G on q1 so that $q_0 \cdot q_1 \geq 0$ (the angle between *q₀* and *q₁* is acute). This choice avoids extra spinning caused by the interpolated rotations.

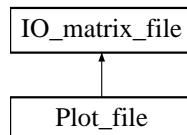
Definition at line 298 of file controller.cpp.

References BASE_FRAME, Do, Quaternion::dot(), Quaternion::dot_prod(), Dp, Quaternion::E(), Quaternion::i(), Integ_quat(), Integ_Trap(), Ko, Ko_prime, Kp, Mo, Mp, pc, pcd, pcdp, pcp, pcp_prev, pcpp, pcpp_prev, qc, qcd, qcp, qcp_prev, quat, Quaternion::v(), wc, wcd, wcp, wcp_prev, and WRONG_SIZE.

4.9 IO_matrix_file Class Reference

```
#include <gnugraph.h>
```

Inheritance diagram for IO_matrix_file::



4.9.1 Detailed Description

Read and write data at every iterations in a file.

Definition at line 201 of file gnugraph.h.

Public Member Functions

- **IO_matrix_file** (const std::string &filename)
- short **write** (const std::vector< Matrix > &data)
- short **write** (const std::vector< Matrix > &data, const std::vector< std::string > &title)
- short **read** (std::vector< Matrix > &data)
- short **read** (std::vector< Matrix > &data, std::vector< std::string > &title)
- short **read_all** (std::vector< Matrix > &data, std::vector< std::string > &data_title)

Private Attributes

- int **position_read**
Position to read the file.
- int **nb_iterations_write**
Number of iterations in writing mode.
- int **nb_iterations_read**
Number of iterations in reading mode.
- int **nb_element**
Number of elements to read or write.

- `std::string filename`

File name.

4.10 Link Class Reference

```
#include <robot.h>
```

4.10.1 Detailed Description

[Link](#) definitions.

A n degree of freedom (dof) serial manipulator is composed of n links. This class describe the property of a link. A n dof robot has n instance of the class [Link](#).

Definition at line 137 of file robot.h.

Public Member Functions

- [Link](#) (const int jt=0, const Real it=0.0, const Real id=0.0, const Real ia=0.0, const Real ial=0.0, const Real [theta_min](#)=-M_PI/2, const Real [theta_max](#)=M_PI/2, const Real it_off=0.0, const Real mass=1.0, const Real cmx=0.0, const Real cmy=0.0, const Real cmz=0.0, const Real ixx=0.0, const Real ixy=0.0, const Real ixz=0.0, const Real iyy=0.0, const Real iyz=0.0, const Real izz=0.0, const Real iIm=0.0, const Real iGr=0.0, const Real iB=0.0, const Real iCf=0.0, const bool dh=true, const bool min_inertial_para=false, const bool [immobile](#)=false)

Constructor.

- [~Link](#) ()

Destructor.

- void [transform](#) (const Real q)

Set the rotation matrix R and the vector p.

- bool [get_DH](#) (void) const

Return DH value.

- int [get_joint_type](#) (void) const

Return the joint type.

- Real [get_theta](#) (void) const

Return theta.

- Real [get_d](#) (void) const

Return d.

- Real [get_a](#) (void) const

Return a.

- Real `get_alpha` (void) const
Return alpha.
- Real `get_q` (void) const
Return joint position (theta if joint type is rotoide, d otherwise).
- Real `get_theta_min` (void) const
Return theta_min.
- Real `get_theta_max` (void) const
Return theta_max.
- Real `get_joint_offset` (void) const
Return joint_offset.
- ReturnMatrix `get_mc` (void)
Return mc.
- ReturnMatrix `get_r` (void)
Return r.
- ReturnMatrix `get_p` (void) const
Return p.
- Real `get_m` (void) const
Return m.
- Real `get_Im` (void) const
Return Im.
- Real `get_Gr` (void) const
Return Gr.
- Real `get_B` (void) const
Return B.
- Real `get_Cf` (void) const
Return Cf.
- ReturnMatrix `get_I` (void) const

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Return I.

- bool `get_immobile` (void) const
Return immobile.
- void `set_m` (const Real m_)
Set m.
- void `set_mc` (const ColumnVector &mc_)
Set mc.
- void `set_r` (const ColumnVector &r_)
Set r.
- void `set_Im` (const Real Im_)
Set Im.
- void `set_B` (const Real B_)
Set B.
- void `set_Cf` (const Real Cf_)
Set Cf.
- void `set_I` (const Matrix &I)
Set I.
- void `set_immobile` (bool im)
Set immobile.

Public Attributes

- Matrix `R`
Orientation matrix of actual link w.r.t to previous link.
- Real `qp`
Joint velocity.
- Real `qpp`
Joint acceleration.

Private Attributes

- int `joint_type`
Joint type.
- Real `theta`
theta DH parameter.
- Real `d`
d DH parameter.
- Real `a`
a DH parameter.
- Real `alpha`
alpha DH parameter.
- Real `theta_min`
Min joint angle.
- Real `theta_max`
Max joint angle.
- Real `joint_offset`
Offset in joint angle (rotoide and prismatic).
- bool `DH`
DH notation(true) or DH modified notation.
- bool `min_para`
Minimum inertial parameter.
- ColumnVector `r`
Position of center of mass w.r.t. link coordinate system (min_para=F).
- ColumnVector `p`
Position vector of actual link w.r.t to previous link.
- Real `m`
Mass of the link.
- Real `Im`
Motor Inertia.

- Real [Gr](#)
Gear Ratio.
- Real [B](#)
Viscous coefficient.
- Real [Cf](#)
Coulomb fiction coefficient.
- ColumnVector [mc](#)
Mass \times center of gravity (used if `min_para = true`).
- Matrix [I](#)
Inertia matrix w.r.t. center of mass and link coordinate system orientation.
- bool [immobile](#)
true if the joint is to be considered locked - ignored for inverse kinematics, but can still be reassigned through transform

Friends

- class [Robot_basic](#)
- class [Robot](#)
- class [mRobot](#)
- class [mRobot_min_para](#)

4.10.2 Member Function Documentation

4.10.2.1 Real Link::get_q (void) const

Return joint position (theta if joint type is rotoide, d otherwise).

The joint offset is removed from the value.

Definition at line 299 of file robot.cpp.

References `d`, `joint_offset`, `joint_type`, and `theta`.

4.11 LinkStewart Class Reference

```
#include <stewart.h>
```

4.11.1 Detailed Description

[LinkStewart](#) definitions.

A [Stewart](#) platform is composed 6 links. This class describe the proprieties of each of the platform's link.

Definition at line 53 of file `stewart.h`.

Public Member Functions

- [LinkStewart](#) (const ColumnVector &InitLink, const Matrix wRp, const ColumnVector q)
Constructor.
- [LinkStewart](#) (const [LinkStewart](#) &x)
Copy constructor.
- [LinkStewart](#) ()
Default Constructor.
- [~LinkStewart](#) ()
Destructor.
- const [LinkStewart](#) & operator= (const [LinkStewart](#) &x)
- void [set_ap](#) (const ColumnVector NewAp)
Set the position vector of platform attachment point.
- void [set_b](#) (const ColumnVector Newb)
Set the position vector of the base attachment point.
- void [set_I1aa](#) (const Real NewI1aa)
Set the value of inertia along the coaxial axis of part 1.
- void [set_I1nn](#) (const Real NewI1nn)
Set the value of inertia along the tangent axis of part 1.
- void [set_I2aa](#) (const Real NewI2aa)
Set the value of inertia along the coaxial axis of part 2.

- void [set_I2nn](#) (const Real NewI2nn)
Set the value of inertia along the tangent axis of part 2.
- void [set_m1](#) (const Real Newm1)
Set the mass of part 1.
- void [set_m2](#) (const Real Newm2)
Set the mass of part 2.
- void [set_Lenght1](#) (const Real NewLenght1)
Set the lenght between platform attachment point and center of mass of part 1.
- void [set_Lenght2](#) (const Real NewLenght2)
Set the lenght between base attachment point and center of mass of part 2.
- ReturnMatrix [get_ap](#) () const
Return the position vector of platform attachment point.
- ReturnMatrix [get_b](#) () const
Return the position vector of base attachment point.
- Real [get_I1aa](#) () const
Return the value of inertia along the coaxial axis of part 1.
- Real [get_I1nn](#) () const
Return the value of inertia along the tangent axis of part 1.
- Real [get_I2aa](#) () const
Return the value of inertia along the coaxial axis of part 2.
- Real [get_I2nn](#) () const
Return the value of inertia along the tangent axis of part 2.
- Real [get_m1](#) () const
Return the mass of part 1.
- Real [get_m2](#) () const
Return the mass of part 2.
- Real [get_Lenght1](#) () const
Return the lenght between platform attachment point and center of mass of part 1.

- Real `get_Lenght2 ()` const
Return the lenght between base attachment point and center of mass of part 2.
- void `LTransform` (const Matrix wRp, const ColumnVector q)
Recalculate the link's parameters related to the platform position.
- void `d_LTransform` (const ColumnVector dq, const ColumnVector Omega, const Real dl, const Real ddl)
Recalculate the link's parameters related to the platform speed.
- void `dd_LTransform` (const ColumnVector ddq, const ColumnVector Omega, const ColumnVector Alpha, const Real dl, const Real ddl)
Recalculate the link's parameters related to the platform acceleration.
- void `tau_LTransform` (const Real dl, const Real ddl, const Real Gravity)
Recalculate the link's parameters related to the platform dynamics.
- ReturnMatrix `Find_UnitV ()`
Return the unit vector of the link direction.
- ReturnMatrix `Find_a` (const Matrix _wRp, const ColumnVector _q)
Return the position of the attachment point on the platform.
- ReturnMatrix `Find_da` (const ColumnVector dq, const ColumnVector Omega)
Return the speed of the attachment point of the link on the platform.
- ReturnMatrix `Find_dda` (const ColumnVector ddq, const ColumnVector Omega, const ColumnVector Alpha)
Return the acceleration of the attachment point of the link on the platform.
- Real `Find_Lenght ()`
Return the lenght of the link.
- ReturnMatrix `Find_VctU ()`
Return the unit vector of the universal joint along the first axis of the fixed revolute joint.
- ReturnMatrix `Find_VctV ()`
Return the unit vector of the universal joint along the second axis of the fixed revolute joint.
- ReturnMatrix `Find_VctC ()`

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Return the unit vector of the universal joint along the third axis of the fixed revolute joint.

- ReturnMatrix [Find_AngularKin](#) (const Real dl, const Real ddl)
Return the angular speed (Column 1) and angular acceleration (Column 2) of the link.
- ReturnMatrix [NormalForce](#) ()
Return the normal component of the reaction force of the platform acting on the link.
- ReturnMatrix [AxialForce](#) (const Matrix J1, const ColumnVector C, const int Index)
Return the axial component of the reaction force of the platform acting on the link.
- ReturnMatrix [Find_N](#) (const Real Gravity=GRAVITY)
Return the intermediate matrix N for force calculation.
- ReturnMatrix [Moment](#) ()
Return the moment component transmitted to the link from the base or the platform (depending where is the universal joint).
- Real [ActuationForce](#) (const Matrix J1, const ColumnVector C, const int Index, const Real Gravity=GRAVITY)
Return the actuation force that power the prismatic joint.
- ReturnMatrix [Find_ACM1](#) (const Real dl, const Real ddl)
Return the acceleration of the center of mass of the first part of the link.

Public Attributes

- ColumnVector [UnitV](#)
Unit Vector of the link.
- ColumnVector [aPos](#)
Position of the platform attachment point.
- ColumnVector [Vu](#)
Unit Vector of the universal joint (Rotational).
- ColumnVector [Vc](#)
Unit Vector of the universal joint (Rotational).

- ColumnVector [Vv](#)
Unit Vector of the universal joint (Rotational).
- ColumnVector [da](#)
Speed of the platform attachment point .
- ColumnVector [dda](#)
Acceleration of the platform attachment point.
- ColumnVector [LOmega](#)
Angular speed of the link.
- ColumnVector [LAlpha](#)
Angular acceleration of the link.
- ColumnVector [ACM1](#)
Acceleration of the first center of mass.
- ColumnVector [M](#)
Moment vector of the link.
- ColumnVector [N](#)
Intermediate vector for dynamics calculations .
- ColumnVector [gravity](#)
Gravity vector.
- Real [L](#)
Lenght of the link.

Private Attributes

- ColumnVector [ap](#)
Platform coordinates of the link in the local frame.
- ColumnVector [b](#)
Base coordinates of the link int the global frame.
- Real [I1aa](#)
Inertia along the coaxial axis for part 1.

- Real [I1nn](#)
Inertia along the tangent axis for part 1.
- Real [I2aa](#)
Inertia along the coaxial axis for part 2.
- Real [I2nn](#)
Inertia along the tangent axis for part 2.
- Real [m1](#)
Mass of part 1.
- Real [m2](#)
Mass of part 2.
- Real [Lenght1](#)
Lenght between the mass center (part 1) and the platform attachment.
- Real [Lenght2](#)
Lenght between the mass center (part 2) and the base attachment.

Friends

- class [Stewart](#)

4.11.2 Constructor & Destructor Documentation

4.11.2.1 [LinkStewart::LinkStewart](#) (const [ColumnVector](#) & *InitLink*, const [Matrix](#) *wRp*, const [ColumnVector](#) *q*)

Constructor.

Parameters:

- InitLink*,: [LinkStewart](#) initialization matrix.
- wRp*,: Rotation matrix
- q*,: Position of the platform

Definition at line 87 of file [stewart.cpp](#).

References [ACM1](#), [ap](#), [aPos](#), [b](#), [da](#), [dda](#), [Find_a\(\)](#), [Find_Lenght\(\)](#), [Find_UnitV\(\)](#), [Find_VctU\(\)](#), [gravity](#), [I1aa](#), [I1nn](#), [I2aa](#), [I2nn](#), [L](#), [LAlpha](#), [Lenght1](#), [Lenght2](#), [LOmega](#), [m1](#), [m2](#), [N](#), [UnitV](#), [Vc](#), [Vu](#), and [Vv](#).

4.11.3 Member Function Documentation

4.11.3.1 `const LinkStewart & LinkStewart::operator= (const LinkStewart & x)`

Definition at line 159 of file `stewart.cpp`.

References `ACM1`, `ap`, `aPos`, `b`, `da`, `dda`, `gravity`, `I1aa`, `I1nn`, `I2aa`, `I2nn`, `L`, `LAlpha`, `Lenght1`, `Lenght2`, `LOmega`, `m1`, `m2`, `N`, `UnitV`, `Vc`, `Vu`, and `Vv`.

4.11.3.2 `void LinkStewart::LTransform (const Matrix wRp, const ColumnVector q)`

Recalculate the link's parameters related to the platform position.

Parameters:

wRp,: rotation matrix.

q,: Position of the platform.

Definition at line 315 of file `stewart.cpp`.

References `aPos`, `Find_a()`, `Find_Lenght()`, `Find_UnitV()`, `Find_VctC()`, `Find_VctV()`, `L`, `UnitV`, `Vc`, and `Vv`.

4.11.3.3 `void LinkStewart::d_LTransform (const ColumnVector dq, const ColumnVector Omega, const Real dl, const Real ddl)`

Recalculate the link's parameters related to the platform speed.

Parameters:

dq,: Speed of the platform.

Omega,: Angular speed of the platform.

dl,: Extension rate of the link.

ddl,: Extension acceleration of the link.

Definition at line 329 of file `stewart.cpp`.

References `da`, `Find_AngularKin()`, `Find_da()`, `LAlpha`, and `LOmega`.

4.11.3.4 `void LinkStewart::dd_LTransform (const ColumnVector ddq, const ColumnVector Omega, const ColumnVector Alpha, const Real dl, const Real ddl)`

Recalculate the link's parameters related to the platform acceleration.

Parameters:

- ddq*,: Acceleration of the platform.
- Omega*,: Angular speed of the platform.
- Alpha*,: Angular acceleration of the platform.
- dl*,: Extension rate of the link.
- ddl*,: Extension acceleration of the link.

Definition at line 347 of file stewart.cpp.

References dda, Find_AngularKin(), Find_dda(), LAlpha, and LOmega.

4.11.3.5 void LinkStewart::tau_LTransform (const Real *dl*, const Real *ddl*, const Real *Gravity*)

Recalculate the link's parameters related to the platform dynamics.

Parameters:

- dl*,: Extension rate of the link.
- ddl*,: Extension acceleration of the link.
- Gravity*,: Gravity (9.81).

Definition at line 366 of file stewart.cpp.

References ACM1, Find_ACM1(), Find_N(), and N.

4.11.3.6 ReturnMatrix LinkStewart::Find_UnitV ()

Return the unit vector of the link direction.

The unit vector representing the orientation of the link is equal to:

$$n = \frac{a_w - b}{Lenght}$$

where:

- A is the position of the attachment point on the platform (world referential).
- B is the position of the attachment point on the base (world referential).
- Lenght is the lenght of the link.

Definition at line 416 of file stewart.cpp.

References aPos, b, and L.

Referenced by LinkStewart(), and LTransform().

4.11.3.7 ReturnMatrix LinkStewart::Find_a (const Matrix *wRp*, const ColumnVector *q*)

Return the position of the attachment point on the platform.

Parameters:

wRp,: Rotation matrix.

q,: Position of the platform.

The position of the attachment point on the platform is equal to the position of the center of the platform plus the position of the attach (in the local referencial) multiplied by the rotation matrix:

$$a = (x, y, z)_q + wRp \cdot a_l$$

where:

- a_l is the position of the attach in the local referencial
- $(x, y, z)_q$ is the position of the platform center (first 3 elements of the q vector)

Definition at line 378 of file stewart.cpp.

References ap.

Referenced by LinkStewart(), and LTransform().

4.11.3.8 ReturnMatrix LinkStewart::Find_da (const ColumnVector *dq*, const ColumnVector *Omega*)

Return the speed of the attachment point of the link on the platform.

Parameters:

dq,: Speed of the platform

Omega,: Angular speed of the platform

This function represent the equation: $\dot{a} = (\dot{x}, \dot{y}, \dot{z})_p + \omega \times a_w$

Where:

- $(\dot{x}, \dot{y}, \dot{z})_p$ is the speed of the platform center (first 3 elements of dq vector)
- ω is the angular speed of the platform
- a_w is the position of the attachment point of the link to the platform in the world referential

Definition at line 438 of file stewart.cpp.

References aPos, and da.

Referenced by d_LTransform().

4.11.3.9 ReturnMatrix LinkStewart::Find_dda (const ColumnVector *ddq*, const ColumnVector *Omega*, const ColumnVector *Alpha*)

Return the acceleration of the attachment point of the link on the platform.

Parameters:

ddq,: Acceleration of the platform.

Omega,: Angular speed of the platform.

Alpha,: Angular acceleration of the platform

This function represent the equation: $\ddot{a} = (\ddot{x}, \ddot{y}, \ddot{z})_p + \alpha \times a_w + \omega \times (\omega \times a_w)$

Where:

- $(\ddot{x}, \ddot{y}, \ddot{z})_p$ is the acceleration of the platform center (first 3 elements of *ddq* vector)
- α is the angular acceleration of the platform
- ω is the angular speed of the platform
- a_w is the position of the attachment point of the link to the platform in the world referential

Definition at line 464 of file stewart.cpp.

References aPos, and dda.

Referenced by dd_LTransform().

4.11.3.10 Real LinkStewart::Find_Lenght ()

Return the lenght of the link.

$$l = \sqrt{(a_w - b) \cdot (a_w - b)}$$

where:

- a_w is the position of the attachment point of the link to the platform in the world referential
- b is the attachment point of the link to the base

Definition at line 486 of file stewart.cpp.

References aPos, and b.

Referenced by LinkStewart(), and LTransform().

4.11.3.11 ReturnMatrix LinkStewart::Find_VctU ()

Return the unit vector of the universal joint along the first axis of the fixed revolute joint.

This vector is equal to the unitary projection of the link unit vector on the X-Z plane:

$$u_x = \frac{n_x}{\sqrt{n_x^2 + n_z^2}}; u_y = 0; u_z = \frac{n_z}{\sqrt{n_x^2 + n_z^2}}$$

where:

- u_x , u_y and u_z are the elements of the vector
- n_x and n_z are the x component and the z component of the link unit vector

Definition at line 503 of file stewart.cpp.

References UnitV.

Referenced by LinkStewart().

4.11.3.12 ReturnMatrix LinkStewart::Find_VctV ()

Return the unit vector of the universal joint along the second axis of the fixed revolute joint.

Eq:

$$v = \frac{u \times n}{\|u \times n\|}$$

Where:

- u is the unit vector of the universal joint along the first axis of the fixed revolute joint
- n is the unit vector of the link

Definition at line 527 of file stewart.cpp.

References UnitV, and Vu.

Referenced by LTransform().

4.11.3.13 ReturnMatrix LinkStewart::Find_VctC ()

Return the unit vector of the universal joint along the third axis of the fixed revolute joint.

Eq:

$$c = u \times v$$

Where:

- u is the unit vector of the universal joint along the first axis of the fixed revolute joint
- v is the unit vector of the universal joint along the second axis of the fixed revolute joint

Definition at line 548 of file stewart.cpp.

References Vu , and Vv .

Referenced by `LTransform()`.

4.11.3.14 ReturnMatrix LinkStewart::Find_AngularKin (const Real dl , const Real ddl)

Return the angular speed (Column 1) and angular acceleration (Column 2) of the link.

Parameters:

dl ,: Extention rate of the link

ddl ,: Extention acceleration of the link

Eqs for angular speed:

$$\omega_u = -(\dot{a} - \dot{l}n) \cdot v / (ln \cdot c)$$

$$\omega_v = (\dot{a} - \dot{l}n) \cdot u / (ln \cdot c)$$

$$\omega = \omega_u u + \omega_v v$$

Eqs for angular acceleration:

$$\ddot{a}t = \ddot{a} - \omega_u \omega_v l c \times n - \ddot{l}n - 2\dot{l}\omega \times n - l\omega \times (\omega \times n)$$

$$\alpha_u = -\ddot{a}t \cdot v / (ln \cdot c)$$

$$\alpha_v = \ddot{a}t \cdot u / (ln \cdot c)$$

$$\alpha = \alpha_u u + \alpha_v v + \omega_u \omega_v c$$

where:

- \dot{a} is the speed of the attachment point of the link to the platform
- \dot{l} is the extension rate of the link
- \mathbf{n} is the unit vector of the link
- l is the lenght of the link
- $\mathbf{u}, \mathbf{v}, \mathbf{c}$ are the rot. vectors of the universal joint

Definition at line 585 of file `stewart.cpp`.

References `da`, `dda`, `L`, `UnitV`, `Vc`, `Vu`, and `Vv`.

Referenced by `d_LTransform()`, and `dd_LTransform()`.

4.11.3.15 ReturnMatrix LinkStewart::NormalForce ()

Return the normal component of the reaction force of the platform acting on the link.

Eq:

$$F^n = (N \times \mathbf{n} - M \times \mathbf{n})/l$$

Where:

- N is an intermediate matrix ([Find_N\(\)](#))
- \mathbf{n} is the unit vector of the link
- M is the reaction moment on the link ([Moment\(\)](#))
- l is the lenght of the link

Definition at line 687 of file `stewart.cpp`.

References `L`, `Moment()`, `N`, and `UnitV`.

4.11.3.16 ReturnMatrix LinkStewart::AxialForce (const Matrix *Jl*, const ColumnVector *C*, const int *Index*)

Return the axial component of the reaction force of the platform acting on the link.

Parameters:

Jl,: First intermediate jacobian matrix (find with [Stewart::Find_InvJacob1\(\)](#))

C,: Intermediate matrix in the dynamics calculation (find with [Stewart::Find_C\(\)](#))

Index,: Number of the link (1 to 6)

Eq:

$$\begin{pmatrix} f_1^a \\ \vdots \\ f_6^a \end{pmatrix} = J_1^T C$$

Where:

- J_q^T is the jacobian matrix
- C is an intermediate matrix ([Stewart::Find_C\(\)](#))

Definition at line 727 of file stewart.cpp.

References UnitV.

Referenced by ActuationForce().

4.11.3.17 ReturnMatrix LinkStewart::Find_N (const Real Gravity = GRAVITY)

Return the intermediate matrix N for force calculation.

Parameters:

Gravity,: Gravity (9.81)

Eqs:

$$I_1 = I_{1aa}nn^T + I_{1nn}(I_{3 \times 3} - nn^T)$$

$$I_2 = I_{2aa}nn^T + I_{2nn}(I_{3 \times 3} - nn^T)$$

$$N = -m_1(l-l_1)n \times G - m_2l_2(n \times G) + (I_1 + I_2)\alpha - (I_1 + I_2)\omega \times \omega + m_1(l-l_1)n \times a_1 + m_2l_2n \times a_2$$

Eq for a_2 (a_1 is found with the Find_ACM1 function):

$$a_2 = l_2\omega \times (\omega \times n) + l_2\alpha \times n$$

Where:

- I_{1aa} and I_{2aa} are the mass moment of inertia component about the main axis of the two parts of the link
- I_{1nn} and I_{2nn} are the mass moment of inertia component about the normal axis of the two parts of the link
- n is the unit vector of the link
- $I_{3 \times 3}$ is a identity matrix

- m_1 is the mass of the first part of the link
- l is the length of the link
- l_1 is the distance between the center of mass of the first part of the link and the base
- G is the gravity
- m_2 is the mass of the second part of the link
- l_2 is the distance between the center of mass of the second part of the link and the platform
- α is the angular acceleration of the link
- ω is the angular speed of the link
- a_1 and a_2 are the acceleration of the center of mass of the two parts of the links

Definition at line 641 of file `stewart.cpp`.

References `ACM1`, `gravity`, `I1aa`, `I1nn`, `I2aa`, `I2nn`, `L`, `LAlpha`, `Lenght1`, `Lenght2`, `LOmega`, `m1`, `m2`, and `UnitV`.

Referenced by `tau_LTransform()`.

4.11.3.18 ReturnMatrix LinkStewart::Moment ()

Return the moment component transmitted to the link from the base or the platform (depending where is the universal joint).

Eq:

$$M = N \cdot n / c \cdot n$$

Where:

- N is an intermediate matrix (`Find_N`)
- n is the unit vector of the link
- c is the rot. vector along the normal axis of the universal joint

Definition at line 666 of file `stewart.cpp`.

References `M`, `N`, `UnitV`, and `Vc`.

Referenced by `Stewart::Find_C()`, and `NormalForce()`.

4.11.3.19 Real LinkStewart::ActuationForce (const Matrix *Jl*, const ColumnVector *C*, const int *Index*, const Real *Gravity* = GRAVITY)

Return the actuation force that power the prismatic joint.

Parameters:

- Jl*,: First intermediate jacobian matrix (find with [Stewart::Find_InvJacob1\(\)](#))
- C*,: Intermediate matrix in the dynamics calculation (find with [Stewart::Find_C\(\)](#))
- Index*,: Number of the link (1 to 6)
- Gravity*,: Gravity (9.81)

Eq:

$$f = m_1 a_1 \cdot n - f^a - m_1 G \cdot n$$

Where:

- *m_1* is the mass of the first part of the link
- *a_1* is the acceleration of the center of mass of the first part of the link
- *n* is the unit vector of the link
- f^a is from [LinkStewart::AxialForce](#)
- *G* is gravity

Definition at line 759 of file `stewart.cpp`.

References `ACM1`, `AxialForce()`, `gravity`, `m1`, and `UnitV`.

4.11.3.20 ReturnMatrix LinkStewart::Find_ACM1 (const Real *dl*, const Real *ddl*)

Return the acceleration of the center of mass of the first part of the link.

Parameters:

- dl*,: Extention rate of the link
- ddl*,: Extention acceleration of the link

Eq:

$$a_1 = (l - l_1)\omega \times (\omega \times n) + (l - l_1)\alpha \times n + 2\omega \times \dot{l}n + \ddot{l}n$$

Where:

- l is the length of the link
- l_1 is the distance between the center of mass of the first part of the link to the base
- ω is the angular speed of the link
- α is the angular acceleration of the link
- \mathbf{n} is the unit vector of the link
- \dot{l} is the extension rate of the link
- \ddot{l} is the extension acceleration of the link

Definition at line 802 of file `stewart.cpp`.

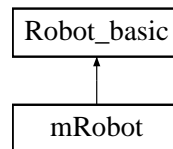
References `L`, `LAlpha`, `Length1`, `LOmega`, and `UnitV`.

Referenced by `tau_LTransform()`.

4.12 mRobot Class Reference

```
#include <robot.h>
```

Inheritance diagram for mRobot::



4.12.1 Detailed Description

Modified DH notation robot class.

Definition at line 389 of file robot.h.

Public Member Functions

- **mRobot** (const int ndof=1)
Constructor.
- **mRobot** (const Matrix &initrobot_motor)
Constructor.
- **mRobot** (const Matrix &initrobot, const Matrix &initmotor)
Constructor.
- **mRobot** (const **mRobot** &x)
Copy constructor.
- **mRobot** (const std::string &filename, const std::string &robotName)
- virtual **~mRobot** ()
Destructor.
- virtual void **robotType_inv_kin** ()
Identify inverse kinematics family.
- ReturnMatrix **inv_kin** (const Matrix &Tobj, const int mj=0)
Overload inv_kin function.

- virtual ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj, const int endlink, bool &converge)
Inverse kinematics solutions.
- virtual ReturnMatrix [inv_kin_rhino](#) (const Matrix &Tobj, bool &converge)
Analytic Rhino inverse kinematics.
- virtual ReturnMatrix [inv_kin_puma](#) (const Matrix &Tobj, bool &converge)
Analytic Puma inverse kinematics.
- virtual ReturnMatrix [inv_kin_schilling](#) (const Matrix &Tobj, bool &converge)
Analytic Schilling inverse kinematics.
- virtual void [kine_pd](#) (Matrix &Rot, ColumnVector &pos, ColumnVector &pos_dot, const int ref) const
Direct kinematics with velocity.
- virtual ReturnMatrix [jacobian](#) (const int ref=0) const
Jacobian of mobile links expressed at frame ref.
- virtual ReturnMatrix [jacobian](#) (const int endlink, const int ref) const
Jacobian of mobile joints up to endlink expressed at frame ref.
- virtual ReturnMatrix [jacobian_dot](#) (const int ref=0) const
Jacobian derivative of mobile joints expressed at frame ref.
- virtual void [dTdqj](#) (Matrix &dRot, ColumnVector &dp, const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [dTdqj](#) (const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp)
Joint torque, without contact force, based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &Fext_, const ColumnVector &Next_)
Joint torque based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque_novelocity](#) (const ColumnVector &qpp)
Joint torque. when joint velocity is 0, based on Recursive Newton-Euler formulation.

- virtual void [delta_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, const ColumnVector &dqp, const ColumnVector &dqpp, ColumnVector &torque, ColumnVector &dtorque)

Delta torque dynamics.

- virtual void [dq_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint position.

- virtual void [dqp_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &dqp, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint velocity.

- virtual ReturnMatrix [G](#) ()

Joint torque due to gravity based on Recursive Newton-Euler formulation.

- virtual ReturnMatrix [C](#) (const ColumnVector &qp)

Joint torque due to centrifugal and Coriolis based on Recursive Newton-Euler formulation.

4.12.2 Member Function Documentation

4.12.2.1 void mRobot::robotType_inv_kin () [virtual]

Identify inverse kinematics family.

Identify the inverse kinematics analytic solution based on the similarity of the robot DH parameters and the DH parameters of know robots (ex: Puma, Rhino, ...). The inverse kinematics will be based on a numerical algorithm if there is no match .

Implements [Robot_basic](#).

Definition at line 1354 of file robot.cpp.

References [Robot_basic::DEFAULT](#), [Robot_basic::PUMA](#), [Puma_mDH\(\)](#), [Robot_basic::RHINO](#), [Rhino_mDH\(\)](#), [Robot_basic::robotType](#), [Robot_basic::SCHILLING](#), and [Schilling_mDH\(\)](#).

Referenced by [mRobot\(\)](#).

4.12.2.2 ReturnMatrix mRobot::inv_kin (const Matrix & *Tobj*, const int *mj*, const int *endlink*, bool & *converge*) [virtual]

Inverse kinematics solutions.

The solution is based on the analytic inverse kinematics if robot type (family) is Rhino or Puma, otherwise used the numerical algorithm defined in [Robot_basic](#) class.

Reimplemented from [Robot_basic](#).

Definition at line 603 of file invkine.cpp.

References [Robot_basic::inv_kin\(\)](#), [inv_kin_puma\(\)](#), [inv_kin_rhino\(\)](#), [inv_kin_schilling\(\)](#), [Robot_basic::PUMA](#), [Robot_basic::RHINO](#), [Robot_basic::robotType](#), and [Robot_basic::SCHILLING](#).

4.12.2.3 ReturnMatrix mRobot::inv_kin_rhino (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Rhino inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 628 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [Link::d](#), [G\(\)](#), [Robot_basic::get_q\(\)](#), [K](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.12.2.4 ReturnMatrix mRobot::inv_kin_puma (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Puma inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 733 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.12.2.5 ReturnMatrix mRobot::inv_kin_schilling (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Schilling inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 893 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [K](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.12.2.6 void mRobot::kine_pd (Matrix & *Rot*, ColumnVector & *pos*, ColumnVector & *pos_dot*, const int *j*) const [virtual]

Direct kinematics with velocity.

Parameters:

Rot,: Frame *j* rotation matrix w.r.t to the base frame.

pos,: Frame *j* position vector wr.t to the base frame.

pos_dot,: Frame *j* velocity vector w.r.t to the base frame.

j,: Frame *j*. Print an error on the console if *j* is out of range.

Implements [Robot_basic](#).

Definition at line 552 of file kinemat.cpp.

4.12.2.7 ReturnMatrix mRobot::jacobian (const int *endlink*, const int *ref*) const [virtual]

Jacobian of mobile joints up to endlink expressed at frame ref.

See [Robot::jacobian](#) for equations.

Implements [Robot_basic](#).

Definition at line 682 of file kinemat.cpp.

4.12.2.8 ReturnMatrix mRobot::jacobian_dot (const int *ref* = 0) const [virtual]

Jacobian derivative of mobile joints expressed at frame ref.

See [Robot::jacobian_dot](#) for equations.

Implements [Robot_basic](#).

Definition at line 736 of file kinemat.cpp.

4.12.2.9 void mRobot::dTdq (Matrix & dRot, ColumnVector & dp, const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

This function computes the partial derivatives:

$$\frac{\partial^0 T_n}{\partial q_i} = {}^0 T_i Q_i {}^i T_n$$

with

$$Q_i = \begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

for a revolute joint and

$$Q_i = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

for a prismatic joint.

dRot and dp are modified on output.

Implements [Robot_basic](#).

Definition at line 582 of file kinemat.cpp.

References [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::links](#), [Robot_basic::p](#), [Link::p](#), [Link::R](#), [Robot_basic::R](#), and [threebythreeident](#).

Referenced by [dTdq\(\)](#).

4.12.2.10 ReturnMatrix mRobot::dTdq (const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

See [mRobot::dTdq\(Matrix & dRot, ColumnVector & dp, const int i\)](#) for equations.

Implements [Robot_basic](#).

Definition at line 664 of file kinemat.cpp.

References [dTdq\(\)](#).

4.12.2.11 ReturnMatrix `mRobot::torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & Fext_, const ColumnVector & Next_)` [virtual]

Joint torque based on Recursive Newton-Euler formulation.

In order to apply the RNE, let us define the following variables (referenced in the i^{th} coordinate frame if applicable):

σ_i is the joint type; $\sigma_i = 1$ for a revolute joint and $\sigma_i = 0$ for a prismatic joint.

$$z_0 = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^T$$

$p_i = \begin{bmatrix} a_{i-1} & -d_i \sin \alpha_{i-1} & d_i \cos \alpha_{i-1} \end{bmatrix}^T$ is the position of the i^{th} with respect to the $(i-1)^{th}$ frame.

Forward Iterations for $i = 1, 2, \dots, n$. Initialize: $\omega_0 = \dot{\omega}_0 = 0$ and $\dot{v}_0 = -g$.

$$\omega_i = R_i^T \omega_{i-1} + \sigma_i z_0 \dot{\theta}_i$$

$$\dot{\omega}_i = R_i^T \dot{\omega}_{i-1} + \sigma_i R_i^T \omega_{i-1} \times z_0 \dot{\theta}_i + \sigma_i z_0 \ddot{\theta}_i$$

$$\dot{v}_i = R_i^T (\dot{\omega}_{i-1} \times p_i + \omega_{i-1} \times (\omega_{i-1} \times p_i) + \dot{v}_{i-1}) + (1 - \sigma_i)(2\omega_i \times z_0 \dot{d}_i + z_0 \ddot{d}_i)$$

Backward Iterations for $i = n, n-1, \dots, 1$. Initialize: $f_{n+1} = n_{n+1} = 0$.

$$\dot{v}_{ci} = \dot{\omega}_i \times r_i + \omega_i \times (\omega_i \times r_i) + v_i$$

$$F_i = m_i \dot{v}_{ci}$$

$$N_i = I_{ci} \ddot{\omega}_i + \omega_i \times I_{ci} \omega_i$$

$$f_i = R_{i+1} f_{i+1} + F_i$$

$$n_i = N_i + R_{i+1} n_{i+1} + r_i \times F_i + p_{i+1} \times R_{i+1} f_{i+1}$$

$$\tau_i = \sigma_i n_i^T z_0 + (1 - \sigma_i) f_i^T z_0$$

Implements [Robot_basic](#).

Definition at line 422 of file dynamics.cpp.

References `Robot_basic::a`, `Link::B`, `Link::Cf`, `Robot_basic::dof`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::fix`, `Link::Gr`, `Robot_basic::gravity`, `Link::I`, `Link::Im`, `Robot_basic::links`, `Robot_basic::n`, `Robot_basic::N`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::set_qp()`, `sign()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.12.2.12 void mRobot::delta_torque (const ColumnVector & *q*, const ColumnVector & *qp*, const ColumnVector & *qpp*, const ColumnVector & *dq*, const ColumnVector & *dqp*, const ColumnVector & *dqpp*, ColumnVector & *ltorque*, ColumnVector & *dtorque*) [virtual]

Delta torque dynamics.

This function computes

$$\delta\tau = D(q)\delta\ddot{q} + S_1(q, \dot{q})\delta\dot{q} + S_2(q, \dot{q}, \ddot{q})\delta q$$

Murray and Neuman Cite_: Murray86 have developed an efficient recursive linearized Newton-Euler formulation. In order to apply the RNE as presented in let us define the following variables

$$p_{di} = \frac{\partial p_i}{\partial d_i} = \begin{bmatrix} 0 & \sin \alpha_i & \cos \alpha_i \end{bmatrix}^T$$

$$Q = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Forward Iterations for $i = 1, 2, \dots, n$. Initialize: $\delta\omega_0 = \delta\dot{\omega}_0 = \delta\dot{v}_0 = 0$.

$$\delta\omega_i = R_i^T \delta\omega_{i-1} + \sigma_i(z_0\delta\dot{\theta}_i - QR_i^T\omega_i\delta\theta_i)$$

$$\delta\dot{\omega}_i = R_i^T \delta\dot{\omega}_{i-1} + \sigma_i[R_i^T \delta\omega_{i-1} \times z_0\dot{\theta}_i + R_i^T \omega_{i-1} \times z_0\delta\dot{\theta}_i + z_0\ddot{\theta}_i - (QR_i^T\dot{\omega}_{i-1} + QR_i^T\omega_{i-1} \times \omega z_0\dot{\theta}_i)\delta\theta_i]$$

$$\delta\dot{v}_i = R_i^T \left(\delta\dot{\omega}_{i-1} \times p_i + \delta\omega_{i-1} \times (\omega_{i-1} \times p_i) + \omega_{i-1} \times (\delta\omega_{i-1} \times p_i) + \delta\dot{v}_i \right) + (1 - \sigma_i) \left(2\delta\omega_i \times z_0\dot{d}_i + 2\omega_i \times z_0\delta\dot{d}_i + z_0\delta\ddot{d}_i \right) - \sigma_i QR_i^T \left(\dot{\omega}_i \times p_i + \omega_i \times (\dot{\omega}_i \times p_i) + \dot{\omega}_i \times (\omega_i \times p_i) + \omega_i \times (\dot{\omega}_i \times p_i) \right)$$

Backward Iterations for $i = n, n - 1, \dots, 1$. Initialize: $\delta f_{n+1} = \delta n_{n+1} = 0$.

$$\delta\dot{v}_{ci} = \delta\dot{v}_i + \delta\dot{\omega}_i \times r_i + \delta\omega_i \times (\omega_i \times r_i) + \omega_i \times (\delta\omega_i \times r_i)$$

$$\delta F_i = m_i \delta\dot{v}_{ci}$$

$$\delta N_i = I_{ci} \delta\dot{\omega}_i + \delta\omega_i \times (I_{ci} \omega_i) + \omega_i \times (I_{ci} \delta\omega_i)$$

$$\delta f_i = R_{i+1} \delta f_{i+1} + \delta F_i + \sigma_{i+1} R_{i+1} Q f_{i+1} \delta\theta_{i+1}$$

$$\delta n_i = \delta N_i + R_{i+1} \delta n_{i+1} + r_i \times \delta F_i + p_{i+1} \times R_{i+1} \delta f_{i+1} + \sigma_{i+1} \left(R_{i+1} Q n_{i+1} + p_{i+1} \times R_{i+1} Q f_{i+1} \right) \delta\theta_{i+1} + (1 - \sigma_{i+1}) p_{di+1} p_{di+1} \times \delta\theta_{i+1}$$

$$\delta\tau_i = \sigma \delta n_i^T z_0 + (1 - \sigma_i) \delta f_i^T z_0$$

Implements [Robot_basic](#).

Definition at line 291 of file delta_t.cpp.

References `Robot_basic::a`, `Robot_basic::da`, `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Link::p`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.12.2.13 `void mRobot::dq_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & dq, ColumnVector & ltorque, ColumnVector & dtorque)`
[virtual]

Delta torque due to delta joint position.

This function computes $S_2(q, \dot{q}, \ddot{q})\delta q$. See [mRobot::delta_torque](#) for equations.

Implements [Robot_basic](#).

Definition at line 205 of file `comp_dq.cpp`.

References `Robot_basic::a`, `Robot_basic::da`, `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Link::p`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.12.2.14 `void mRobot::dqp_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & dqp, ColumnVector & ltorque, ColumnVector & dtorque)` [virtual]

Delta torque due to delta joint velocity.

This function computes $S_1(q, \dot{q}, \ddot{q})\delta \dot{q}$. See [mRobot::delta_torque](#) for equations.

Implements [Robot_basic](#).

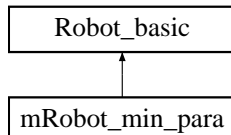
Definition at line 188 of file `comp_dqp.cpp`.

References `Robot_basic::a`, `Robot_basic::da`, `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Link::p`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.13 mRobot_min_para Class Reference

```
#include <robot.h>
```

Inheritance diagram for mRobot_min_para:



4.13.1 Detailed Description

Modified DH notation and minimal inertial parameters robot class.

Definition at line 437 of file robot.h.

Public Member Functions

- [mRobot_min_para](#) (const int ndof=1)
Constructor.
- [mRobot_min_para](#) (const Matrix &dhinit)
Constructor.
- [mRobot_min_para](#) (const Matrix &initrobot, const Matrix &initmotor)
Constructor.
- [mRobot_min_para](#) (const [mRobot_min_para](#) &x)
Copy constructor.
- [mRobot_min_para](#) (const std::string &filename, const std::string &robotName)
- virtual [~mRobot_min_para](#) ()
Destructor.
- virtual void [robotType_inv_kin](#) ()
Identify inverse kinematics familly.
- ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj=0)
Overload inv_kin function.

- virtual ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj, const int endlink, bool &converge)
Inverse kinematics solutions.
- virtual ReturnMatrix [inv_kin_rhino](#) (const Matrix &Tobj, bool &converge)
Analytic Rhino inverse kinematics.
- virtual ReturnMatrix [inv_kin_puma](#) (const Matrix &Tobj, bool &converge)
Analytic Puma inverse kinematics.
- virtual ReturnMatrix [inv_kin_schilling](#) (const Matrix &Tobj, bool &converge)
Analytic Schilling inverse kinematics.
- virtual void [kine_pd](#) (Matrix &Rot, ColumnVector &pos, ColumnVector &pos_dot, const int ref=0) const
Direct kinematics with velocity.
- virtual ReturnMatrix [jacobian](#) (const int ref=0) const
Jacobian of mobile links expressed at frame ref.
- virtual ReturnMatrix [jacobian](#) (const int endlink, const int ref) const
Jacobian of mobile joints up to endlink expressed at frame ref.
- virtual ReturnMatrix [jacobian_dot](#) (const int ref=0) const
Jacobian derivative of mobile joints expressed at frame ref.
- virtual void [dTdqj](#) (Matrix &dRot, ColumnVector &dp, const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [dTdqj](#) (const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp)
Joint torque without contact force based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &Fext_, const ColumnVector &Next_)
Joint torque based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque_novelocity](#) (const ColumnVector &qpp)

Joint torque. when joint velocity is 0, based on Recursive Newton-Euler formulation.

- virtual void [delta_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, const ColumnVector &dqp, const ColumnVector &dqpp, ColumnVector &torque, ColumnVector &dtorque)

Delta torque dynamics.

- virtual void [dq_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint position.

- virtual void [dqp_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &dqp, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint velocity.

- virtual ReturnMatrix [G](#) ()

Joint torque due to gravity based on Recursive Newton-Euler formulation.

- virtual ReturnMatrix [C](#) (const ColumnVector &qp)

Joint torque due to centrifugal and Coriolis based on Recursive Newton-Euler formulation.

4.13.2 Member Function Documentation

4.13.2.1 void mRobot_min_para::robotType_inv_kin () [virtual]

Identify inverse kinematics family.

Identify the inverse kinematics analytic solution based on the similarity of the robot DH parameters and the DH parameters of know robots (ex: Puma, Rhino, ...). The inverse kinematics will be based on a numerical alogorithm if there is no match .

Implements [Robot_basic](#).

Definition at line 1423 of file robot.cpp.

References [Robot_basic::DEFAULT](#), [Robot_basic::PUMA](#), [Puma_mDH\(\)](#), [Robot_basic::RHINO](#), [Rhino_mDH\(\)](#), [Robot_basic::robotType](#), [Robot_basic::SCHILLING](#), and [Schilling_mDH\(\)](#).

Referenced by [mRobot_min_para\(\)](#).

4.13.2.2 ReturnMatrix mRobot_min_para::inv_kin (const Matrix & *Tobj*, const int *mj*, const int *endlink*, bool & *converge*) [virtual]

Inverse kinematics solutions.

The solution is based on the analytic inverse kinematics if robot type (family) is Rhino or Puma, otherwise used the numerical algorithm defined in [Robot_basic](#) class.

Reimplemented from [Robot_basic](#).

Definition at line 1009 of file invkine.cpp.

References [Robot_basic::inv_kin\(\)](#), [inv_kin_puma\(\)](#), [inv_kin_rhino\(\)](#), [Robot_basic::PUMA](#), [Robot_basic::RHINO](#), and [Robot_basic::robotType](#).

4.13.2.3 ReturnMatrix mRobot_min_para::inv_kin_rhino (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Rhino inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 1031 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [Link::d](#), [G\(\)](#), [Robot_basic::get_q\(\)](#), [K](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.13.2.4 ReturnMatrix mRobot_min_para::inv_kin_puma (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Puma inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 1128 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.13.2.5 ReturnMatrix mRobot_min_para::inv_kin_schilling (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Schilling inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 1289 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [K](#), [Robot_basic::links](#), and [M_PI](#).

4.13.2.6 void mRobot_min_para::kine_pd (Matrix & Rot, ColumnVector & pos, ColumnVector & pos_dot, const int j = 0) const [virtual]

Direct kinematics with velocity.

Parameters:

- Rot*,: Frame j rotation matrix w.r.t to the base frame.
- pos*,: Frame j position vector wr.r.t to the base frame.
- pos_dot*,: Frame j velocity vector w.r.t to the base frame.
- j*,: Frame j. Print an error on the console if j is out of range.

Implements [Robot_basic](#).

Definition at line 799 of file kinemat.cpp.

4.13.2.7 ReturnMatrix mRobot_min_para::jacobian (const int endlink, const int ref) const [virtual]

Jacobian of mobile joints up to endlink expressed at frame ref.

See [Robot::jacobian](#) for equations.

Implements [Robot_basic](#).

Definition at line 905 of file kinemat.cpp.

4.13.2.8 ReturnMatrix mRobot_min_para::jacobian_dot (const int ref = 0) const [virtual]

Jacobian derivative of mobile joints expressed at frame ref.

See [Robot::jacobian_dot](#) for equations.

Implements [Robot_basic](#).

Definition at line 961 of file kinemat.cpp.

4.13.2.9 void mRobot_min_para::dTdq (Matrix & dRot, ColumnVector & dp, const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

This function computes the partial derivatives:

$$\frac{\partial^0 T_n}{\partial q_i} = {}^0 T_i Q_i {}^i T_n$$

See [mRobot::dTdq\(Matrix & dRot, ColumnVector & dp, const int i\)](#) for equations.

Implements [Robot_basic](#).

Definition at line 829 of file kinemat.cpp.

References [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::links](#), [Robot_basic::p](#), [Link::p](#), [Link::R](#), [Robot_basic::R](#), and [threebythreeident](#).

Referenced by [dTdq\(\)](#).

4.13.2.10 ReturnMatrix mRobot_min_para::dTdq (const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

See [mRobot::dTdq\(Matrix & dRot, ColumnVector & dp, const int i\)](#) for equations.

Implements [Robot_basic](#).

Definition at line 887 of file kinemat.cpp.

References [dTdq\(\)](#).

4.13.2.11 ReturnMatrix mRobot_min_para::torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & Fext_, const ColumnVector & Next_) [virtual]

Joint torque based on Recursive Newton-Euler formulation.

See ReturnMatrix [mRobot::torque](#)(const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & Fext, const ColumnVector & Next) for the Recursive Newton-Euler formulation.

Implements [Robot_basic](#).

Definition at line 697 of file dynamics.cpp.

References [Link::B](#), [Link::Cf](#), [Robot_basic::dof](#), [Robot_basic::f](#), [Robot_basic::F](#), [Robot_basic::fix](#), [Link::Gr](#), [Robot_basic::gravity](#), [Link::I](#), [Link::Im](#), [Robot_basic::links](#), [Robot_basic::n](#), [Robot_basic::N](#), [Robot_basic::p](#), [Link::R](#), [Robot_basic::R](#), [Robot_basic::set_q\(\)](#), [Robot_basic::set_qp\(\)](#), [sign\(\)](#), [Robot_basic::vp](#), [Robot_basic::w](#), [Robot_basic::wp](#), and [Robot_basic::z0](#).

4.13.2.12 `void mRobot_min_para::delta_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & dq, const ColumnVector & dqp, const ColumnVector & dqpp, ColumnVector & ltorque, ColumnVector & dtorque)` [virtual]

Delta torque dynamics.

See [mRobot::delta_torque](#) for equations.

Implements [Robot_basic](#).

Definition at line 511 of file delta_t.cpp.

References [Robot_basic::df](#), [Robot_basic::dF](#), [Robot_basic::dn](#), [Robot_basic::dN](#), [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::dvp](#), [Robot_basic::dw](#), [Robot_basic::dwp](#), [Robot_basic::f](#), [Robot_basic::F](#), [Robot_basic::gravity](#), [Link::I](#), [Robot_basic::links](#), [Link::m](#), [Robot_basic::n](#), [Robot_basic::N](#), [Link::p](#), [Robot_basic::p](#), [Link::R](#), [Robot_basic::R](#), [Robot_basic::set_q\(\)](#), [Robot_basic::vp](#), [Robot_basic::w](#), [Robot_basic::wp](#), and [Robot_basic::z0](#).

4.13.2.13 `void mRobot_min_para::dq_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & dq, ColumnVector & ltorque, ColumnVector & dtorque)` [virtual]

Delta torque due to delta joint position.

This function computes $S_2(q, \dot{q}, \ddot{q})\delta q$. See [mRobot::delta_torque](#) for equations.

Implements [Robot_basic](#).

Definition at line 335 of file comp_dq.cpp.

References [Robot_basic::df](#), [Robot_basic::dF](#), [Robot_basic::dn](#), [Robot_basic::dN](#), [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::dvp](#), [Robot_basic::dw](#), [Robot_basic::dwp](#), [Robot_basic::f](#), [Robot_basic::F](#), [Robot_basic::gravity](#), [Link::I](#), [Robot_basic::links](#), [Link::m](#), [Robot_basic::n](#), [Robot_basic::N](#), [Link::p](#), [Robot_basic::p](#), [Link::R](#), [Robot_basic::R](#), [Robot_basic::set_q\(\)](#), [Robot_basic::vp](#), [Robot_basic::w](#), [Robot_basic::wp](#), and [Robot_basic::z0](#).

4.13.2.14 `void mRobot_min_para::dqp_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & dqp, ColumnVector & ltorque, ColumnVector & dtorque)` [virtual]

Delta torque due to delta joint velocity.

This function computes $S_1(q, \dot{q}, \ddot{q})\delta \dot{q}$. See [mRobot::delta_torque](#) for equations.

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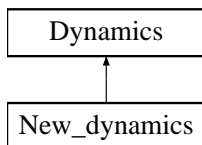
Implements [Robot_basic](#).

Definition at line 303 of file comp_dqp.cpp.

References `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Link::p`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.14 New_dynamics Class Reference

Inheritance diagram for New_dynamics::



4.14.1 Detailed Description

This is an example of customize [Dynamics](#) class.

This class enherite from [Dynamics](#) class. At every time frame the new virtual plot functions record the current time and the robot joints positions. The data can then be used to create a plot.

Definition at line 63 of file demo_2dof_pd.cpp.

Public Member Functions

- [New_dynamics](#) ([Robot_basic](#) *robot_)
Constructor.
- virtual void [plot](#) ()
Customize plot function.

Public Attributes

- [Robot_basic](#) * [robot](#)
- bool [first_pass_plot](#)
- RowVector [tout](#)
- Matrix [xout](#)
- int [i](#)

4.14.2 Member Function Documentation

4.14.2.1 void New_dynamics::plot () [virtual]

Customize plot function.

Record the time (tout) and the joints positions (xout). This member function is call by the member function xdot.

Reimplemented from [Dynamics](#).

Definition at line 94 of file demo_2dof_pd.cpp.

References [first_pass_plot](#), [i](#), [Dynamics::nsteps](#), [robot](#), [Dynamics::tf_cont](#), [Dynamics::time](#), [Dynamics::to](#), [tout](#), [Dynamics::x](#), and [xout](#).

4.14.3 Member Data Documentation

4.14.3.1 [Robot_basic*](#) [New_dynamics::robot](#)

[Robot_basic](#) pointer.

Reimplemented from [Dynamics](#).

Definition at line 69 of file demo_2dof_pd.cpp.

Referenced by [New_dynamics\(\)](#), and [plot\(\)](#).

4.14.3.2 [bool](#) [New_dynamics::first_pass_plot](#)

First time in plot function.

Definition at line 70 of file demo_2dof_pd.cpp.

Referenced by [New_dynamics\(\)](#), and [plot\(\)](#).

4.14.3.3 [RowVector](#) [New_dynamics::tout](#)

Output time vector.

Definition at line 71 of file demo_2dof_pd.cpp.

Referenced by [main\(\)](#), and [plot\(\)](#).

4.14.3.4 [Matrix](#) [New_dynamics::xout](#)

Output state vector.

Definition at line 72 of file demo_2dof_pd.cpp.

Referenced by [main\(\)](#), and [plot\(\)](#).

4.14.3.5 `int New_dynamics::i`

Temporary index.

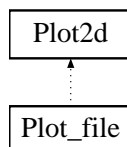
Definition at line 73 of file demo_2dof_pd.cpp.

Referenced by `New_dynamics()`, and `plot()`.

4.15 Plot2d Class Reference

```
#include <gnugraph.h>
```

Inheritance diagram for Plot2d::



4.15.1 Detailed Description

2d plot object.

Definition at line 149 of file gnugraph.h.

Public Member Functions

- [Plot2d](#) (void)
Constructor.
- void [dump](#) (void)
Method to dump the content of [Plot2d](#) to stdout.
- void **settitle** (const std::string &t)
- void **setxlabel** (const std::string &t)
- void **setylabel** (const std::string &t)
- void **addcurve** (const Matrix &data, const std::string &label="", [LineType_en](#) enLineType=DATAPOINTS)
- void [gnuplot](#) (void)
Creates a GNUplot graphic.
- void **addcommand** (const std::string &gcom)

Private Attributes

- std::string [title](#)
Graph title.
- std::string [xlabel](#)

Graph x axis.

- `std::string ylabel`
Graph y axis.
- `std::string gnucommand`
GNU plot command.
- `VectorCurves vCurves`

4.16 Plot3d Class Reference

```
#include <gnugraph.h>
```

4.16.1 Detailed Description

3d plot object.

Definition at line 174 of file gnugraph.h.

Public Member Functions

- [Plot3d](#) ()
Default constructor.
- void **settitle** (const std::string &t)
- void **setxlabel** (const std::string &t)
- void **setylabel** (const std::string &t)
- void **setzlabel** (const std::string &t)
- void [gnuplot](#) (const Matrix &xyz)

Creates a GNUplot graphic.

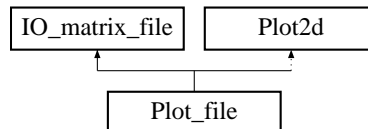
Private Attributes

- std::string [title](#)
Graph title.
- std::string [xlabel](#)
Graph x axis.
- std::string [ylabel](#)
Graph y axis.
- std::string [zlabel](#)
Graph z axis.

4.17 Plot_file Class Reference

```
#include <gnugraph.h>
```

Inheritance diagram for Plot_file::



4.17.1 Detailed Description

Creates a graphic from a data file.

Definition at line 223 of file gnugraph.h.

Public Member Functions

- **Plot_file** (const std::string &filename)
- short **graph** (const std::string &title_graph, const std::string &label, const short x, const short y, const short x_start, const short y_start, const short y_end)

Private Attributes

- std::vector< Matrix > [data_from_file](#)
Data file.
- std::vector< std::string > [data_title](#)
Data file title.

4.18 Proportional_Derivative Class Reference

```
#include <controller.h>
```

4.18.1 Detailed Description

Proportional derivative controller class.

The driving torques can be expressed as

$$\tau = K_p(q_d - q) + K_d(\dot{q}_d - \dot{q})$$

where K_p , K_d are diagonal positive definite matrix.

Definition at line 252 of file controller.h.

Public Member Functions

- [Proportional_Derivative](#) (const short dof=1)
Constructor.
- [Proportional_Derivative](#) (const [Robot_basic](#) &robot, const DiagonalMatrix &Kp, const DiagonalMatrix &Kd)
Constructor.
- ReturnMatrix [torque_cmd](#) ([Robot_basic](#) &robot, const ColumnVector &qd, const ColumnVector &qpd)
Output torque.
- short [set_Kd](#) (const DiagonalMatrix &Kd)
Assign the velocity error gain matrix $K_p(i, i)$.
- short [set_Kp](#) (const DiagonalMatrix &Kp)
Assign the position error gain matrix $K_p(i, i)$.

Private Attributes

- int [dof](#)
Degree of freedom.
- ColumnVector [q](#)
Robot joints positions.

- ColumnVector [qp](#)
Robot joints velocity.
- ColumnVector [qpp](#)
Robot joints acceleration.
- ColumnVector [tau](#)
Output torque.
- ColumnVector [zero3](#)
 3×1 zero vector.
- DiagonalMatrix [Kp](#)
Position error gain.
- DiagonalMatrix [Kd](#)
Velocity error gain.

4.18.2 Member Function Documentation

4.18.2.1 short Proportional_Derivative::set_Kd (const DiagonalMatrix & Kd_)

Assign the velocity error gain matrix $K_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not $dof \times dof$.

Definition at line 657 of file controller.cpp.

References [dof](#), [Kd](#), and [WRONG_SIZE](#).

Referenced by [Proportional_Derivative\(\)](#).

4.18.2.2 short Proportional_Derivative::set_Kp (const DiagonalMatrix & Kp_)

Assign the position error gain matrix $K_p(i, i)$.

Returns:

short: 0 or WRONG_SIZE if the matrix is not $dof \times dof$.

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Definition at line 674 of file controller.cpp.

References dof, Kp, and WRONG_SIZE.

Referenced by Proportional_Derivative().

4.19 Quaternion Class Reference

```
#include <quaternion.h>
```

4.19.1 Detailed Description

[Quaternion](#) class definition.

Definition at line 92 of file quaternion.h.

Public Member Functions

- [Quaternion](#) ()
Constructor.
- [Quaternion](#) (const Real angle_in_rad, const ColumnVector &axis)
Constructor.
- [Quaternion](#) (const Real s, const Real v1, const Real v2, const Real v3)
Constructor.
- [Quaternion](#) (const Matrix &R)
Constructor.
- [Quaternion operator+](#) (const [Quaternion](#) &q) const
Overload + operator.
- [Quaternion operator-](#) (const [Quaternion](#) &q) const
Overload - operator.
- [Quaternion operator *](#) (const [Quaternion](#) &q) const
*Overload * operator.*
- [Quaternion operator/](#) (const [Quaternion](#) &q) const
Overload / operator.
- [Quaternion conjugate](#) () const
Conjugate.
- [Quaternion i](#) () const

Quaternion inverse.

$$q^{-1} = \frac{q^*}{N(q)}$$

where q^* and $N(q)$ are the quaternion conjugate and the quaternion norm respectively.

- **Quaternion & unit ()**
Normalize a quaternion.
- **Quaternion exp () const**
Exponential of a quaternion.
- **Quaternion power (const Real t) const**
- **Quaternion Log () const**
Logarithm of a unit quaternion.
- **Quaternion dot (const ColumnVector &w, const short sign) const**
Quaternion time derivative.
- **ReturnMatrix E (const short sign) const**
Matrix E.
- **Real norm () const**
Return the quaternion norm.
- **Real dot_prod (const Quaternion &q) const**
Quaternion dot product.
- **Real s () const**
Return scalar part.
- **void set_s (const Real s)**
Set scalar part.
- **ReturnMatrix v () const**
Return vector part.
- **void set_v (const ColumnVector &v)**
Set vector part.
- **ReturnMatrix R () const**
Rotation matrix from a unit quaternion.

- ReturnMatrix [T\(\)](#) const
Transformation matrix from a quaternion.

Private Attributes

- Real [s_](#)
Quaternion scalar part.
- ColumnVector [v_](#)
Quaternion vector part.

4.19.2 Constructor & Destructor Documentation

4.19.2.1 Quaternion::Quaternion (const Matrix & R)

Constructor.

Cite_: Dam. The unit quaternion obtained from a matrix (see [Quaternion::R\(\)](#))

$$R(s, v) = \begin{bmatrix} s^2 + v_1^2 - v_2^2 - v_3^2 & 2v_1v_2 + 2sv_3 & 2v_1v_3 - 2sv_2 \\ 2v_1v_2 - 2sv_3 & s^2 - v_1^2 + v_2^2 - v_3^2 & 2v_2v_3 + 2sv_1 \\ 2v_1v_3 + 2sv_2 & 2v_2v_3 - 2sv_1 & s^2 - v_1^2 - v_2^2 + v_3^2 \end{bmatrix}$$

First we find s :

$$R_{11} + R_{22} + R_{33} + R_{44} = 4s^2$$

Now the other values are:

$$s = \pm \frac{1}{2} \sqrt{R_{11} + R_{22} + R_{33} + R_{44}}$$

$$v_1 = \frac{R_{32} - R_{23}}{4s}$$

$$v_2 = \frac{R_{13} - R_{31}}{4s}$$

$$v_3 = \frac{R_{21} - R_{12}}{4s}$$

The sign of s cannot be determined. Depending on the choice of the sign for s the sign of v change as well. Thus the quaternions q and $-q$ represent the same rotation, but the interpolation curve changed with the choice of the sign. A positive sign has been chosen.

Definition at line 120 of file quaternion.cpp.

References [EPSILON](#), [i\(\)](#), [R\(\)](#), [s_](#), and [v_](#).

4.19.3 Member Function Documentation

4.19.3.1 `Quaternion` `Quaternion::operator+ (const Quaternion & rhs) const`

Overload + operator.

The quaternion addition is

$$q_1 + q_2 = [s_1, v_1] + [s_2, v_2] = [s_1 + s_2, v_1 + v_2]$$

The result is not necessarily a unit quaternion even if q_1 and q_2 are unit quaternions.

Definition at line 203 of file quaternion.cpp.

References `s_`, and `v_`.

4.19.3.2 `Quaternion` `Quaternion::operator- (const Quaternion & rhs) const`

Overload - operator.

The quaternion soustraction is

$$q_1 - q_2 = [s_1, v_1] - [s_2, v_2] = [s_1 - s_2, v_1 - v_2]$$

The result is not necessarily a unit quaternion even if q_1 and q_2 are unit quaternions.

Definition at line 223 of file quaternion.cpp.

References `s_`, and `v_`.

4.19.3.3 `Quaternion` `Quaternion::operator * (const Quaternion & rhs) const`

Overload * operator.

The multiplication of two quaternions is

$$q = q_1 q_2 = [s_1 s_2 - v_1 \cdot v_2, v_1 \times v_2 + s_1 v_2 + s_2 v_1]$$

where \cdot and \times denote the scalar and vector product in R^3 respectively.

If q_1 and q_2 are unit quaternions, then q will also be a unit quaternion.

Definition at line 243 of file quaternion.cpp.

References `s_`, and `v_`.

4.19.3.4 `Quaternion` `Quaternion::conjugate () const`

Conjugate.

The conjugate of a quaternion $q = [s, v]$ is $q^* = [s, -v]$

Definition at line 283 of file quaternion.cpp.

References `s_`, and `v_`.

Referenced by `i()`.

4.19.3.5 `Quaternion Quaternion::exp () const`

Exponential of a quaternion.

Let a quaternion of the form $q = [0, \theta v]$, q is not necessarily a unit quaternion. Then the exponential function is defined by $q = [\cos(\theta), v \sin(\theta)]$.

Definition at line 336 of file quaternion.cpp.

References `EPSILON`, `s_`, and `v_`.

Referenced by `power()`.

4.19.3.6 `Quaternion Quaternion::Log () const`

Logarithm of a unit quaternion.

The logarithm function of a unit quaternion $q = [\cos(\theta), v \sin(\theta)]$ is defined as $\log(q) = [0, v\theta]$. The result is not necessary a unit quaternion.

Definition at line 365 of file quaternion.cpp.

References `EPSILON`, `s_`, and `v_`.

Referenced by `power()`.

4.19.3.7 `Quaternion Quaternion::dot (const ColumnVector & w, const short sign) const`

`Quaternion` time derivative.

The quaternion time derivative, quaternion propagation equation, is

$$\begin{aligned}\dot{s} &= -\frac{1}{2}v^T w_o \\ \dot{v} &= \frac{1}{2}E(s, v)w_o \\ E &= sI - S(v)\end{aligned}$$

where w_o is the angular velocity vector expressed in the base frame. If the vector is expressed in the object frame, w_b , the time derivative becomes

$$\dot{s} = -\frac{1}{2}v^T w_b$$

$$\dot{v} = \frac{1}{2}E(s, v)w_b$$

$$E = sI + S(v)$$

Definition at line 388 of file quaternion.cpp.

References `s_`, `sign()`, and `v_`.

Referenced by `Impedance::control()`.

4.19.3.8 ReturnMatrix Quaternion::E (const short *sign*) const

Matrix `E`.

See [Quaternion::dot](#) for explanation.

Definition at line 426 of file quaternion.cpp.

References `BODY_FRAME`, `sign()`, `threebythreeident`, and `x_prod_matrix()`.

Referenced by `Impedance::control()`, and `Omega()`.

4.19.3.9 Real Quaternion::norm () const

Return the quaternion norm.

The norm of quaternion is defined by

$$N(q) = s^2 + v \cdot v$$

Definition at line 298 of file quaternion.cpp.

References `s_`, and `v_`.

Referenced by `i()`, and `unit()`.

4.19.3.10 Real Quaternion::dot_prod (const [Quaternion](#) & *q*) const

[Quaternion](#) dot product.

The dot product of quaternion is defined by

$$q_1 \cdot q_2 = s_1 s_2 + v_1 \cdot v_2$$

Definition at line 445 of file quaternion.cpp.

Referenced by `Impedance::control()`, and `Resolved_acc::torque_cmd()`.

4.19.3.11 ReturnMatrix Quaternion::R () const

Rotation matrix from a unit quaternion.

$p' = qpq^{-1} = Rp$ where p is a vector, R a rotation matrix and q a quaternion. The rotation matrix obtained from a quaternion is then

$$R(s, v) = (s^2 - v^T v)I + 2vv^T - 2sS(v)$$

$$R(s, v) = \begin{bmatrix} s^2 + v_1^2 - v_2^2 - v_3^2 & 2v_1v_2 + 2sv_3 & 2v_1v_3 - 2sv_2 \\ 2v_1v_2 - 2sv_3 & s^2 - v_1^2 + v_2^2 - v_3^2 & 2v_2v_3 + 2sv_1 \\ 2v_1v_3 + 2sv_2 & 2v_2v_3 - 2sv_1 & s^2 - v_1^2 - v_2^2 + v_3^2 \end{bmatrix}$$

where $S(\cdot)$ is the cross product matrix defined by

$$S(u) = \begin{bmatrix} 0 & -u_3 & u_2 \\ u_3 & 0 & -u_1 \\ -u_2 & u_1 & 0 \end{bmatrix}$$

Definition at line 458 of file quaternion.cpp.

References `s_`, `threebythreeident`, `v_`, and `x_prod_matrix()`.

Referenced by `homogen_demo()`, `main()`, `Quaternion()`, and `Dynamics::set_robot_on_first_point_of_splines()`.

4.19.3.12 ReturnMatrix Quaternion::T () const

Transformation matrix from a quaternion.

See [Quaternion::R\(\)](#) for equations.

Definition at line 499 of file quaternion.cpp.

References `fourbyfourident`, `s_`, `v_`, and `x_prod_matrix()`.

Referenced by `homogen_demo()`, and `main()`.

4.20 Resolved_acc Class Reference

```
#include <controller.h>
```

4.20.1 Detailed Description

Resolved rate acceleration controller class.

The dynamic model of a robot manipulator can be expressed in joint space as

$$B(q)\ddot{q} + C(q, \dot{q})\dot{q} + D\dot{q} + g(q) = \tau - J^T(q)f$$

According to the concept of inverse dynamics, the driving torques can be chosen as

$$\tau = B(q)J^{-1}(q)(a - \dot{J}(q, \dot{q})\dot{q}) + C(q, \dot{q})\dot{q} + D\dot{q} + g(q) - J^T(q)f$$

where a is the a new control input defined by

$$a_p = \ddot{p}_d + k_{vp}\dot{\tilde{p}} + k_{pp}\tilde{p}$$

$$a_o = \dot{\omega}_d + k_{vo}\dot{\tilde{\omega}} + k_{po}\tilde{\omega}$$

where $\tilde{x} = x_c - x_d$ and v is the vector par of the quaternion representing the orientation error between the desired and end effector frame. k_{vp} , k_{pp} , k_{vo} and k_{po} are positive gains.

Up to now this class has been tested only with a 6 dof robot.

Definition at line 171 of file controller.h.

Public Member Functions

- [Resolved_acc](#) (const short dof=1)

Constructor.

- [Resolved_acc](#) (const [Robot_basic](#) &robot, const Real [Kvp](#), const Real [Kpp](#), const Real [Kvo](#), const Real [Kpo](#))

Constructor.

- void [set_Kvp](#) (const Real [Kvp](#))

Assign the gain k_{vp} .

- void [set_Kpp](#) (const Real [Kpp](#))

Assign the gain k_{pp} .

- void [set_Kvo](#) (const Real [Kvo](#))

Assign the gain k_{vo} .

- void `set_Kpo` (const Real `Kpo`)

Assign the gain k_{po} .

- ReturnMatrix `torque_cmd` (Robot_basic &robot, const ColumnVector &pdpp, const ColumnVector &pdp, const ColumnVector &pd, const ColumnVector &wdp, const ColumnVector &wd, const Quaternion &qd, const short link_pc, const Real dt)

Output torque.

Private Attributes

- double `Kvp`

Controller gains.

- double `Kpp`
- double `Kvo`
- double `Kpo`
- Matrix `Rot`

Temporay rotation matrix.

- ColumnVector `zero3`

3×1 zero vector.

- ColumnVector `qp`

Robot joints velocity.

- ColumnVector `qpp`

Robot joints acceleration.

- ColumnVector `a`

Control input.

- ColumnVector `p`

End effector position.

- ColumnVector `pp`

End effector velocity.

- ColumnVector `quat_v_error`

Vector part of error quaternion.

- [Quaternion quat](#)

Temporary quaternion.

4.20.2 Member Function Documentation

4.20.2.1 ReturnMatrix Resolved_acc::torque_cmd ([Robot_basic](#) & robot, const ColumnVector & pdpp, const ColumnVector & pdp, const ColumnVector & pd, const ColumnVector & wdp, const ColumnVector & wd, const [Quaternion](#) & quatd, const short link_pc, const Real dt)

Output torque.

For more robustess the damped least squares inverse Jacobian is used instead of the inverse Jacobian.

The quaternion -q represents exactly the same rotation as the quaternion q. The temporary quaternion, quat, is quatd plus a sign correction. It is customary to choose the sign G on q1 so that $q_0 \cdot Gq_1 \geq 0$ (the angle between q_0 and Gq_1 is acute). This choice avoids extra spinning caused by the interpolated rotations.

Definition at line 471 of file controller.cpp.

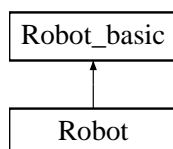
References [a](#), [Quaternion::dot_prod\(\)](#), [Robot_basic::get_dof\(\)](#), [Robot_basic::get_-q\(\)](#), [Robot_basic::get_qp\(\)](#), [Robot_basic::jacobian_DLS_inv\(\)](#), [Robot::jacobian_dot\(\)](#), [Robot::kine_pd\(\)](#), [Kpo](#), [Kpp](#), [Kvo](#), [Kvp](#), [p](#), [pp](#), [qp](#), [qpp](#), [quat](#), [quat_v_error](#), [robot](#), [Rot](#), [Quaternion::s\(\)](#), [Robot::torque\(\)](#), [Quaternion::v\(\)](#), [Robot_basic::w](#), [x_prod_matrix\(\)](#), and [zero3](#).

Referenced by [Dynamics::xdot\(\)](#).

4.21 Robot Class Reference

```
#include <robot.h>
```

Inheritance diagram for Robot::



4.21.1 Detailed Description

DH notation robot class.

Definition at line 340 of file robot.h.

Public Member Functions

- [Robot](#) (const int ndof=1)
Constructor.
- [Robot](#) (const Matrix &initrobot)
Constructor.
- [Robot](#) (const Matrix &initrobot, const Matrix &initmotor)
Constructor.
- [Robot](#) (const [Robot](#) &x)
Copy constructor.
- **Robot** (const std::string &filename, const std::string &robotName)
- virtual [~Robot](#) ()
Destructor.
- virtual void [robotType_inv_kin](#) ()
Identify inverse kinematics family.
- virtual void [kine_pd](#) (Matrix &Rot, ColumnVector &pos, ColumnVector &pos_dot, const int ref) const
Direct kinematics with velocity.

- ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj=0)
Overload inv_kin function.
- virtual ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj, const int endlink, bool &converge)
Inverse kinematics solutions.
- virtual ReturnMatrix [inv_kin_rhino](#) (const Matrix &Tobj, bool &converge)
Analytic Rhino inverse kinematics.
- virtual ReturnMatrix [inv_kin_puma](#) (const Matrix &Tobj, bool &converge)
Analytic Puma inverse kinematics.
- virtual ReturnMatrix [inv_kin_schilling](#) (const Matrix &Tobj, bool &converge)
Analytic Schilling inverse kinematics.
- virtual ReturnMatrix [jacobian](#) (const int ref=0) const
Jacobian of mobile links expressed at frame ref.
- virtual ReturnMatrix [jacobian](#) (const int endlink, const int ref) const
Jacobian of mobile links up to endlink expressed at frame ref.
- virtual ReturnMatrix [jacobian_dot](#) (const int ref=0) const
Jacobian derivative of mobile joints expressed at frame ref.
- virtual void [dTdqj](#) (Matrix &dRot, ColumnVector &dp, const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [dTdqj](#) (const int i)
Partial derivative of the robot position (homogeneous transf.).
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp)
Joint torque, without contact force, based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &Fext_, const ColumnVector &Next_)
Joint torque based on Recursive Newton-Euler formulation.
- virtual ReturnMatrix [torque_novelocity](#) (const ColumnVector &qpp)
Joint torque. when joint velocity is 0, based on Recursive Newton-Euler formulation.

- virtual void [delta_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, const ColumnVector &dqp, const ColumnVector &dqpp, ColumnVector <orque, ColumnVector &dtorque)

Delta torque dynamics.

- virtual void [dq_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint position.

- virtual void [dqp_torque](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &dqp, ColumnVector &torque, ColumnVector &dtorque)

Delta torque due to delta joint velocity.

- virtual ReturnMatrix [G](#) ()

Joint torque due to gravity based on Recursive Newton-Euler formulation.

- virtual ReturnMatrix [C](#) (const ColumnVector &qp)

Joint torque due to centrifugal and Coriolis based on Recursive Newton-Euler formulation.

4.21.2 Member Function Documentation

4.21.2.1 void Robot::robotType_inv_kin () [virtual]

Identify inverse kinematics family.

Identify the inverse kinematics analytic solution based on the similarity of the robot DH parameters and the DH parameters of know robots (ex: Puma, Rhino, ...). The inverse kinematics will be based on a numerical alogorithm if there is no match .

Implements [Robot_basic](#).

Definition at line 1284 of file robot.cpp.

References [Robot_basic::DEFAULT](#), [Robot_basic::PUMA](#), [Puma_DH\(\)](#), [Robot_basic::RHINO](#), [Rhino_DH\(\)](#), [Robot_basic::robotType](#), [Robot_basic::SCHILLING](#), and [Schilling_DH\(\)](#).

Referenced by [Robot\(\)](#).

4.21.2.2 `void Robot::kine_pd (Matrix & Rot, ColumnVector & pos, ColumnVector & pos_dot, const int j) const` [virtual]

Direct kinematics with velocity.

Parameters:

Rot,: Frame *j* rotation matrix w.r.t to the base frame.

pos,: Frame *j* position vector wr.r.t to the base frame.

pos_dot,: Frame *j* velocity vector w.r.t to the base frame.

j,: Frame *j*. Print an error on the console if *j* is out of range.

Implements [Robot_basic](#).

Definition at line 219 of file kinemat.cpp.

Referenced by `Resolved_acc::torque_cmd()`.

4.21.2.3 `ReturnMatrix Robot::inv_kin (const Matrix & Tobj, const int mj, const int endlink, bool & converge)` [virtual]

Inverse kinematics solutions.

The solution is based on the analytic inverse kinematics if robot type (family) is Rhino or Puma, otherwise used the numerical algorithm defined in [Robot_basic](#) class.

Reimplemented from [Robot_basic](#).

Definition at line 204 of file invkine.cpp.

References `Robot_basic::inv_kin()`, `inv_kin_puma()`, `inv_kin_rhino()`, `inv_kin_schilling()`, `Robot_basic::PUMA`, `Robot_basic::RHINO`, `Robot_basic::robotType`, and `Robot_basic::SCHILLING`.

4.21.2.4 `ReturnMatrix Robot::inv_kin_rhino (const Matrix & Tobj, bool & converge)` [virtual]

Analytic Rhino inverse kinematics.

`converge` will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 229 of file invkine.cpp.

References `Robot_basic::a`, `Link::a`, `Link::d`, `G()`, `Robot_basic::get_q()`, `K`, `Robot_basic::links`, and `M_PI`.

Referenced by `inv_kin()`.

4.21.2.5 ReturnMatrix Robot::inv_kin_puma (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Puma inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 326 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.21.2.6 ReturnMatrix Robot::inv_kin_schilling (const Matrix & *Tobj*, bool & *converge*) [virtual]

Analytic Schilling inverse kinematics.

converge will be false if the desired end effector pose is outside robot range.

Implements [Robot_basic](#).

Definition at line 486 of file invkine.cpp.

References [Robot_basic::a](#), [Link::a](#), [C\(\)](#), [Link::d](#), [Robot_basic::get_q\(\)](#), [K](#), [Robot_basic::links](#), and [M_PI](#).

Referenced by [inv_kin\(\)](#).

4.21.2.7 ReturnMatrix Robot::jacobian (const int *endlink*, const int *ref*) const [virtual]

Jacobian of mobile links up to *endlink* expressed at frame *ref*.

The Jacobian expressed in based frame is

$${}^0J(q) = \begin{bmatrix} {}^0J_1(q) & {}^0J_2(q) & \cdots & {}^0J_n(q) \end{bmatrix}$$

where ${}^0J_i(q)$ is defined by

$${}^0J_i(q) = \begin{bmatrix} z_i \times^i p_n \\ z_i \end{bmatrix} \quad \text{rotoid joint}$$

$${}^0J_i(q) = \begin{bmatrix} z_i \\ 0 \end{bmatrix} \quad \text{prismatic joint}$$

Expressed in a different frame the Jacobian is obtained by

$${}^iJ(q) = \begin{bmatrix} {}^0_iR^T & 0 \\ 0 & {}^0_iR^T \end{bmatrix} {}^0J(q)$$

Implements [Robot_basic](#).

Definition at line 352 of file kinemat.cpp.

4.21.2.8 ReturnMatrix Robot::jacobian_dot (const int ref = 0) const [virtual]

Jacobian derivative of mobile joints expressed at frame ref.

The Jacobian derivative expressed in based frame is

$${}^0\dot{J}(q, \dot{q}) = \begin{bmatrix} {}^0\dot{J}_1(q, \dot{q}) & {}^0\dot{J}_2(q, \dot{q}) & \cdots & {}^0\dot{J}_n(q, \dot{q}) \end{bmatrix}$$

where ${}^0\dot{J}_i(q, \dot{q})$ is defined by

$${}^0\dot{J}_i(q, \dot{q}) = \begin{bmatrix} \omega_{i-1} \times z_i \\ \omega_{i-1} \times^{i-1} p_n + z_i \times^{i-1} \dot{p}_n \end{bmatrix} \quad \text{rotoid joint}$$

$${}^0\dot{J}_i(q, \dot{q}) = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \quad \text{prismatic joint}$$

Expressed in a different frame the Jacobian derivative is obtained by

$${}^iJ(q) = \begin{bmatrix} {}^0R^T & 0 \\ 0 & {}^0R^T \end{bmatrix} {}^0J(q)$$

Implements [Robot_basic](#).

Definition at line 449 of file kinemat.cpp.

Referenced by Resolved_acc::torque_cmd().

4.21.2.9 void Robot::dTdq (Matrix & dRot, ColumnVector & dp, const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

This function computes the partial derivatives:

$$\frac{\partial {}^0T_n}{\partial q_i} = {}^0T_{i-1} Q_i {}^{i-1}T_n$$

in standard notation and

$$\frac{\partial {}^0T_n}{\partial q_i} = {}^0T_i Q_i {}^iT_n$$

in modified notation,

with

$$Q_i = \begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

for a revolute joint and

$$Q_i = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

for a prismatic joint.

dRot and *dp* are modified on output.

Implements [Robot_basic](#).

Definition at line 249 of file kinemat.cpp.

References [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::links](#), [Robot_basic::p](#), [Link::p](#), [Robot_basic::R](#), [Link::R](#), and [threebythreeident](#).

Referenced by [dTdq\(i\)](#), and [kinematics_demo\(\)](#).

4.21.2.10 ReturnMatrix Robot::dTdq (const int i) [virtual]

Partial derivative of the robot position (homogeneous transf.).

See [Robot::dTdq\(Matrix & dRot, ColumnVector & dp, const int i\)](#) for equations.

Implements [Robot_basic](#).

Definition at line 334 of file kinemat.cpp.

References [dTdq\(i\)](#).

4.21.2.11 ReturnMatrix Robot::torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & Fext, const ColumnVector & Next) [virtual]

Joint torque based on Recursive Newton-Euler formulation.

In order to apply the RNE as presented in Murray 86, let us define the following variables (referenced in the i^{th} coordinate frame if applicable):

σ_i is the joint type; $\sigma_i = 1$ for a revolute joint and $\sigma_i = 0$ for a prismatic joint.

$$z_0 = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^T$$

$p_i = \begin{bmatrix} a_i & d_i \sin \alpha_i & d_i \cos \alpha_i \end{bmatrix}^T$ is the position of the i^{th} with respect to the $i-1^{th}$ frame.

Forward Iterations for $i = 1, 2, \dots, n$. Initialize: $\omega_0 = \dot{\omega}_0 = 0$ and $\dot{v}_0 = -g$.

$$\omega_i = R_i^T [\omega_{i-1} + \sigma_i z_0 \dot{\theta}_i]$$

$$\dot{\omega}_i = R_i^T \{ \dot{\omega}_{i-1} + \sigma_i [z_0 \ddot{\theta}_i + \omega_{i-1} \times (z_0 \dot{\theta}_i)] \}$$

$$\dot{v}_i = R_i^T \{ \dot{v}_{i-1} + (1 - \sigma_i) [z_0 \ddot{d}_i + 2\omega_{i-1} \times (z_0 \dot{d}_i)] \} + \dot{\omega}_i \times p_i + \omega_i \times (\omega_i \times p_i)$$

Backward Iterations for $i = n, n-1, \dots, 1$. Initialize: $\$f_{n+1} = \mathbf{n}_{n+1} = \mathbf{0}$.

$$\dot{v}_{ci} = v_i + \omega_i \times r_i + \omega_i \times (\omega_i \times r_i)$$

$$F_i = m_i \dot{v}_{ci}$$

$$N_i = I_{ci} \dot{\omega}_i + \omega_i \times (I_{ci} \omega_i)$$

$$f_i = R_{i+1} [f_{i+1}] + F_i$$

$$n_i = R_{i+1} [n_{i+1}] + p_i \times f_i + N_i + r_i \times F_i$$

$$\tau_i = \sigma_i n_i^T (R_i^T z_0) + (1 - \sigma_i) f_i^T (R_i^T z_0)$$

Implements [Robot_basic](#).

Definition at line 148 of file dynamics.cpp.

References `Robot_basic::a`, `Link::B`, `Link::Cf`, `Robot_basic::dof`, `Robot_basic::f`, `Robot_basic::F`, `Link::Gr`, `Robot_basic::gravity`, `Link::I`, `Link::Im`, `Robot_basic::links`, `Robot_basic::n`, `Robot_basic::N`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::set_qp()`, `sign()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.21.2.12 void Robot::delta_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & dq, const ColumnVector & dqp, const ColumnVector & dqpp, ColumnVector & ltorque, ColumnVector & dtorque) [virtual]

Delta torque dynamics.

This function computes

$$\delta \tau = D(q) \delta \ddot{q} + S_1(q, \dot{q}) \delta \dot{q} + S_2(q, \dot{q}, \ddot{q}) \delta q$$

Murray and Neuman Cite_: Murray86 have developed an efficient recursive linearized Newton-Euler formulation. In order to apply the RNE as presented in let us define the following variables

$$p_{di} = \frac{\partial p_i}{\partial d_i} = \begin{bmatrix} 0 & \sin \alpha_i & \cos \alpha_i \end{bmatrix}^T$$

$$Q = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Forward Iterations for $i = 1, 2, \dots, n$. Initialize: $\delta \omega_0 = \delta \dot{\omega}_0 = \delta \dot{v}_0 = 0$.

$$\delta \omega_i = R_i^T \{ \delta \omega_{i-1} + \sigma_i [z_0 \delta \dot{\theta}_i - Q(\omega_{i-1} + \dot{\theta}_i) \delta \theta_i] \}$$

$$\delta\dot{\omega}_i = R_i^T \{ \delta\dot{\omega}_{i-1} + \sigma_i [z_0 \delta\ddot{\theta}_i + \delta\omega_{i-1} \times (z_0 \dot{\theta}_i) + \omega_{i-1} \times (z_0 \delta\dot{\theta}_i)] - \sigma_i Q [\omega_{i-1} + z_0 \ddot{\theta}_i + \omega_{i-1} \times (z_0 \dot{\theta}_i)] \delta\theta_i \}$$

$$\delta\dot{v}_i = R_i^T \{ \delta\dot{v}_{i-1} - \sigma_i Q \dot{v}_{i-1} \delta\theta_i + (1 - \sigma_i) [z_0 \delta\ddot{d}_i + 2\delta\omega_{i-1} \times (z_0 \dot{d}_i) + 2\omega_{i-1} \times (z_0 \delta\dot{d}_i)] \} + \delta\dot{\omega}_i \times p_i + \delta\omega_i \times (\omega_i \times p_i) + \omega_i \times (\delta\omega_i \times p_i) +$$

Backward Iterations for $i = n, n-1, \dots, 1$. Initialize: $\delta f_{n+1} = \delta n_{n+1} = 0$.

$$\delta\dot{v}_{ci} = \delta v_i + \delta\omega_i \times r_i + \delta\omega_i \times (\omega_i \times r_i) + \omega_i \times (\delta\omega_i \times r_i)$$

$$\delta F_i = m_i \delta\dot{v}_{ci}$$

$$\delta N_i = I_{ci} \delta\dot{\omega}_i + \delta\omega_i \times (I_{ci} \omega_i) + \omega_i \times (I_{ci} \delta\omega_i)$$

$$\delta f_i = R_{i+1} [\delta f_{i+1}] + \delta F_i + \sigma_{i+1} Q R_{i+1} [f_{i+1}] \delta\theta_{i+1}$$

$$\delta n_i = R_{i+1} [\delta n_{i+1}] + \delta N_i + p_i \times \delta f_i + r_i \times \delta F_i + (1 - \sigma_i) (p_{di} \times f_i) \delta d_i + \sigma_{i+1} Q R_{i+1} [n_{i+1}] \delta\theta_{i+1}$$

$$\delta\tau_i = \sigma_i [\delta n_i^T (R_i^T z_0) - n_i^T (R_i^T Q z_0) \delta\theta_i] + (1 - \sigma_i) [\delta f_i^T (R_i^T z_0)]$$

Implements [Robot_basic](#).

Definition at line 65 of file delta_t.cpp.

References `Robot_basic::a`, `Robot_basic::da`, `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.21.2.13 void Robot::dq_torque (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp, const ColumnVector & dq, ColumnVector & ltorque, ColumnVector & dtorque)
[virtual]

Delta torque due to delta joint position.

This function computes $S_2(q, \dot{q}, \ddot{q})\delta q$. See [Robot::delta_torque](#) for equations.

Implements [Robot_basic](#).

Definition at line 65 of file comp_dq.cpp.

References `Robot_basic::a`, `Robot_basic::da`, `Robot_basic::df`, `Robot_basic::dF`, `Robot_basic::dn`, `Robot_basic::dN`, `Robot_basic::dof`, `Robot_basic::dp`, `Robot_basic::dvp`, `Robot_basic::dw`, `Robot_basic::dwp`, `Robot_basic::f`, `Robot_basic::F`, `Robot_basic::gravity`, `Link::I`, `Robot_basic::links`, `Link::m`, `Robot_basic::n`, `Robot_basic::N`, `Robot_basic::p`, `Link::R`, `Robot_basic::R`, `Robot_basic::set_q()`, `Robot_basic::vp`, `Robot_basic::w`, `Robot_basic::wp`, and `Robot_basic::z0`.

4.21.2.14 void Robot::dqp_torque (const ColumnVector & *q*, const ColumnVector & *qp*, const ColumnVector & *dqp*, ColumnVector & *ltorque*, ColumnVector & *dtorque*) [virtual]

Delta torque due to delta joint velocity.

This function computes $S_1(q, \dot{q}, \ddot{q})\delta\dot{q}$. See [Robot::delta_torque](#) for equations.

Implements [Robot_basic](#).

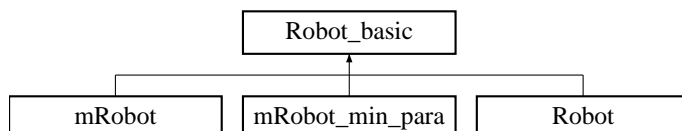
Definition at line 63 of file comp_dqp.cpp.

References [Robot_basic::a](#), [Robot_basic::da](#), [Robot_basic::df](#), [Robot_basic::dF](#), [Robot_basic::dn](#), [Robot_basic::dN](#), [Robot_basic::dof](#), [Robot_basic::dp](#), [Robot_basic::dvp](#), [Robot_basic::dw](#), [Robot_basic::dwp](#), [Robot_basic::f](#), [Robot_basic::F](#), [Robot_basic::gravity](#), [Link::I](#), [Robot_basic::links](#), [Link::m](#), [Robot_basic::n](#), [Robot_basic::N](#), [Robot_basic::p](#), [Link::R](#), [Robot_basic::R](#), [Robot_basic::set_q\(\)](#), [Robot_basic::vp](#), [Robot_basic::w](#), [Robot_basic::wp](#), and [Robot_basic::z0](#).

4.22 Robot_basic Class Reference

```
#include <robot.h>
```

Inheritance diagram for Robot_basic::



4.22.1 Detailed Description

Virtual base robot class.

Definition at line 216 of file robot.h.

Public Member Functions

- [Robot_basic](#) (const int ndof=1, const bool dh_parameter=false, const bool min_inertial_para=false)

Constructor.

- [Robot_basic](#) (const Matrix &initrobot_motor, const bool dh_parameter=false, const bool min_inertial_para=false)

Constructor.

- [Robot_basic](#) (const Matrix &initrobot, const Matrix &initmotor, const bool dh_parameter=false, const bool min_inertial_para=false)

Constructor.

- **Robot_basic** (const std::string &filename, const std::string &robotName, const bool dh_parameter=false, const bool min_inertial_para=false)

- [Robot_basic](#) (const [Robot_basic](#) &x)

Copy constructor.

- virtual [~Robot_basic](#) ()

Destructor.

- [Robot_basic](#) & [operator=](#) (const [Robot_basic](#) &x)

Overload = operator.

- Real `get_q` (const int i) const
- bool `get_DH` () const
Return true if in DH notation, false otherwise.
- int `get_dof` () const
Return dof.
- int `get_available_dof` () const
Counts number of currently non-immobile links.
- int `get_available_dof` (const int endlink) const
Counts number of currently non-immobile links up to and including endlink.
- int `get_fix` () const
Return fix.
- ReturnMatrix `get_q` (void) const
Return the joint position vector.
- ReturnMatrix `get_qp` (void) const
Return the joint velocity vector.
- ReturnMatrix `get_qpp` (void) const
Return the joint acceleration vector.
- ReturnMatrix `get_available_q` (void) const
Return the joint position vector of available (non-immobile) joints.
- ReturnMatrix `get_available_qp` (void) const
Return the joint velocity vector of available (non-immobile) joints.
- ReturnMatrix `get_available_qpp` (void) const
Return the joint acceleration vector of available (non-immobile) joints.
- ReturnMatrix `get_available_q` (const int endlink) const
Return the joint position vector of available (non-immobile) joints up to and including endlink.
- ReturnMatrix `get_available_qp` (const int endlink) const
Return the joint velocity vector of available (non-immobile) joints up to and including endlink.
- ReturnMatrix `get_available_qpp` (const int endlink) const

Return the joint acceleration vector of available (non-immobile) joints up to and including endlink.

- void [set_q](#) (const ColumnVector &q)
Set the joint position vector.
- void [set_q](#) (const Matrix &q)
Set the joint position vector.
- void [set_q](#) (const Real q, const int i)
- void [set_qp](#) (const ColumnVector &qp)
Set the joint velocity vector.
- void [set_qpp](#) (const ColumnVector &qpp)
Set the joint acceleration vector.
- void [kine](#) (Matrix &Rot, ColumnVector &pos) const
Direct kinematics at end effector.
- void [kine](#) (Matrix &Rot, ColumnVector &pos, const int j) const
Direct kinematics at end effector.
- ReturnMatrix [kine](#) (void) const
Return the end effector direct kinematics transform matrix.
- ReturnMatrix [kine](#) (const int j) const
Return the frame j direct kinematics transform matrix.
- ReturnMatrix [kine_pd](#) (const int ref=0) const
Direct kinematics with velocity.
- virtual void [kine_pd](#) (Matrix &Rot, ColumnVector &pos, ColumnVector &pos_dot, const int ref) const=0
- virtual void [robotType_inv_kin](#) ()=0
- virtual ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj=0)
Numerical inverse kinematics. See [inv_kin\(const Matrix & Tobj, const int mj, const int endlink, bool & converge\)](#).
- ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj, bool &converge)
- virtual ReturnMatrix [inv_kin](#) (const Matrix &Tobj, const int mj, const int endlink, bool &converge)
Numerical inverse kinematics.

- virtual ReturnMatrix **inv_kin_rhino** (const Matrix &Tobj, bool &converge)=0
- virtual ReturnMatrix **inv_kin_puma** (const Matrix &Tobj, bool &converge)=0
- virtual ReturnMatrix **inv_kin_schilling** (const Matrix &Tobj, bool &converge)=0
- virtual ReturnMatrix **jacobian** (const int ref=0) const

Jacobian of mobile links expressed at frame ref.

- virtual ReturnMatrix **jacobian** (const int endlink, const int ref) const=0
- virtual ReturnMatrix **jacobian_dot** (const int ref=0) const=0
- ReturnMatrix **jacobian_DLS_inv** (const double eps, const double lambda_max, const int ref=0) const

Inverse Jacobian based on damped least squares inverse.

- virtual void **dTdqi** (Matrix &dRot, ColumnVector &dp, const int i)=0
- virtual ReturnMatrix **dTdqi** (const int i)=0
- ReturnMatrix **acceleration** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &tau)

Joints acceleration without contact force.

- ReturnMatrix **acceleration** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &tau, const ColumnVector &Fext, const ColumnVector &Next)

Joints acceleration.

- ReturnMatrix **inertia** (const ColumnVector &q)

Inertia of the manipulator.

- virtual ReturnMatrix **torque_novelocity** (const ColumnVector &qpp)=0
- virtual ReturnMatrix **torque** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp)=0
- virtual ReturnMatrix **torque** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &Fext_, const ColumnVector &Next_)=0
- virtual void **delta_torque** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, const ColumnVector &dqp, const ColumnVector &dqpp, ColumnVector &torque, ColumnVector &dtorque)=0
- virtual void **dq_torque** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp, const ColumnVector &dq, ColumnVector &torque, ColumnVector &dtorque)=0
- virtual void **dqp_torque** (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &dqp, ColumnVector &torque, ColumnVector &dtorque)=0

- ReturnMatrix [dtau_dq](#) (const ColumnVector &q, const ColumnVector &qp, const ColumnVector &qpp)
Sensitivity of the dynamics with respect to q .
- ReturnMatrix [dtau_dqp](#) (const ColumnVector &q, const ColumnVector &qp)
Sensitivity of the dynamics with respect to \dot{q} .
- virtual ReturnMatrix **G** ()=0
- virtual ReturnMatrix **C** (const ColumnVector &qp)=0
- void **error** (const std::string &msg1) const

Public Attributes

- ColumnVector * [w](#)
- ColumnVector * [wp](#)
- ColumnVector * [vp](#)
- ColumnVector * [a](#)
- ColumnVector * [f](#)
- ColumnVector * [f_nv](#)
- ColumnVector * [n](#)
- ColumnVector * [n_nv](#)
- ColumnVector * [F](#)
- ColumnVector * [N](#)
- ColumnVector * [p](#)
- ColumnVector * [pp](#)
- ColumnVector * [dw](#)
- ColumnVector * [dwp](#)
- ColumnVector * [dvp](#)
- ColumnVector * [da](#)
- ColumnVector * [df](#)
- ColumnVector * [dn](#)
- ColumnVector * [dF](#)
- ColumnVector * [dN](#)
- ColumnVector * [dp](#)
- ColumnVector [z0](#)
Axis vector at each joint.
- ColumnVector [gravity](#)
Gravity vector.
- Matrix * [R](#)
Temporary rotation matrix.

- [Link](#) * [links](#)

Pointer on [Link](#) cclass.

Private Types

- enum [EnumRobotType](#) { [DEFAULT](#) = 0, [RHINO](#) = 1, [PUMA](#) = 2, [SCHILLING](#) = 3 }

enum EnumRobotType

Private Member Functions

- void [cleanUpPointers](#) ()

Free all vectors and matrix memory.

Private Attributes

- [EnumRobotType](#) [robotType](#)

Robot type.

- int [dof](#)

Degree of freedom.

- int [fix](#)

Virtual link, used with modified DH notation.

Friends

- class [Robot](#)
- class [mRobot](#)
- class [mRobot_min_para](#)
- class [Robotgl](#)
- class [mRobotgl](#)

4.22.2 Member Enumeration Documentation

4.22.2.1 enum Robot_basic::EnumRobotType [private]

enum EnumRobotType

Enumerator:

DEFAULT Default robot family.

RHINO Rhino family.

PUMA Puma family.

SCHILLING Schilling family.

Definition at line 324 of file robot.h.

4.22.3 Constructor & Destructor Documentation

4.22.3.1 Robot_basic::Robot_basic (const int *ndof* = 1, const bool *dh_parameter* = false, const bool *min_inertial_para* = false)

Constructor.

Parameters:

ndof,: Robot degree of freedom.

dh_parameter,: true if DH notation, false if modified DH notation.

min_inertial_para,: true inertial parameter are in minimal form.

Allocate memory for vectors and matrix pointers. Initialize all the Links instance.

Definition at line 573 of file robot.cpp.

References a, cleanUpPointers(), da, dF, df, dN, dn, dof, dp, dvp, dw, dwp, F, f, f_nv, fix, GRAVITY, gravity, links, N, n, n_nv, p, pp, R, threebythreeident, vp, w, wp, and z0.

4.22.3.2 Robot_basic::Robot_basic (const Matrix & *dhinit*, const bool *dh_parameter* = false, const bool *min_inertial_para* = false)

Constructor.

Parameters:

dhinit,: Robot initialization matrix.

dh_parameter,: true if DH notation, false if modified DH notation.

min_inertial_para,: true inertial parameter are in minimal form.

Allocate memory for vectors and matrix pointers. Initialize all the Links instance.

Definition at line 343 of file robot.cpp.

References a, cleanUpPointers(), da, dF, df, dN, dn, dof, dp, dvp, dw, dwp, F, f, f_nv, fix, GRAVITY, gravity, links, N, n, n_nv, p, pp, R, threebythreeident, vp, w, wp, and z0.

4.22.3.3 Robot_basic::Robot_basic (const Matrix & *initrobot*, const Matrix & *initmotor*, const bool *dh_parameter* = false, const bool *min_inertial_para* = false)

Constructor.

Parameters:

initrobot,: [Robot](#) initialization matrix.

initmotor,: Motor initialization matrix.

dh_parameter,: true if DH notation, false if modified DH notation.

min_inertial_para,: true inertial parameter are in minimal form.

Allocate memory for vectors and matrix pointers. Initialize all the Links instance.

Definition at line 451 of file robot.cpp.

References a, cleanUpPointers(), da, dF, df, dN, dn, dof, dp, dvp, dw, dwp, F, f, f_nv, fix, GRAVITY, gravity, links, N, n, n_nv, p, pp, R, threebythreeident, vp, w, wp, and z0.

4.22.3.4 Robot_basic::~~Robot_basic () [virtual]

Destructor.

Free all vectors and matrix memory.

Definition at line 879 of file robot.cpp.

References cleanUpPointers().

4.22.4 Member Function Documentation

4.22.4.1 Real Robot_basic::get_q (const int *i*) const [inline]

Definition at line 235 of file robot.h.

Referenced by `Clik::Clik()`, `dynamics_demo()`, `kinematics_demo()`, `Dynamics::set_robot_on_first_point_of_splines()`, `Proportional_Derivative::torque_cmd()`, `Computed_torque_method::torque_cmd()`, and `Resolved_acc::torque_cmd()`.

4.22.4.2 void Robot_basic::set_q (const ColumnVector & q)

Set the joint position vector.

Set the joint position vector and recalculate the orientation matrix R and the position vector p (see [Link](#) class). Print an error if the size of q is incorrect.

Definition at line 1137 of file `robot.cpp`.

References `dof`, `get_available_dof()`, `links`, `Link::p`, `p`, and `R`.

Referenced by `mRobot_min_para::delta_torque()`, `mRobot::delta_torque()`, `Robot::delta_torque()`, `mRobot_min_para::dq_torque()`, `mRobot::dq_torque()`, `Robot::dq_torque()`, `mRobot_min_para::dqp_torque()`, `mRobot::dqp_torque()`, `Robot::dqp_torque()`, `dynamics_demo()`, `Clik::endeff_pos_ori_err()`, `inertia()`, `inv_kin()`, `kinematics_demo()`, `main()`, `Clik::q_qdot()`, `Dynamics::set_robot_on_first_point_of_splines()`, `mRobot_min_para::torque()`, `mRobot::torque()`, `Robot::torque()`, and `Dynamics::xdot()`.

4.22.4.3 void Robot_basic::set_q (const Matrix & q)

Set the joint position vector.

Set the joint position vector and recalculate the orientation matrix R and the position vector p (see [Link](#) class). Print an error if the size of q is incorrect.

Definition at line 1070 of file `robot.cpp`.

References `dof`, `get_available_dof()`, `links`, `Link::p`, `p`, and `R`.

4.22.4.4 void Robot_basic::set_q (const Real q, const int i) [inline]

Definition at line 255 of file `robot.h`.

4.22.4.5 void Robot_basic::kine (Matrix & Rot, ColumnVector & pos) const

Direct kinematics at end effector.

Parameters:

Rot,: End effector orientation.

pos,: End effector position.

Definition at line 92 of file kinemat.cpp.

Referenced by `Clik::endeff_pos_ori_err()`, `Impedance::Impedance()`, `kinematics_demo()`, and `main()`.

4.22.4.6 `void Robot_basic::kine (Matrix & Rot, ColumnVector & pos, const int j) const`

Direct kinematics at end effector.

Parameters:

Rot,: Frame j orientation.

pos,: Frame j position.

j,: Selected frame.

Definition at line 102 of file kinemat.cpp.

4.22.4.7 `ReturnMatrix Robot_basic::kine_pd (const int j = 0) const`

Direct kinematics with velocity.

Return a 3×5 matrix. The first three columns are the frame j to the base rotation, the fourth column is the frame j w.r.t to the base position vector and the last column is the frame j w.r.t to the base translational velocity vector. Print an error on the console if j is out of range.

Definition at line 142 of file kinemat.cpp.

4.22.4.8 `ReturnMatrix Robot_basic::inv_kin (const Matrix & Tobj, const int mj, const int endlink, bool & converge) [virtual]`

Numerical inverse kinematics.

Parameters:

Tobj,: Transformation matrix expressing the desired end effector pose.

mj,: Select algorithm type, 0: based on Jacobian, 1: based on derivative of T.

converge,: Indicate if the algorithm converge.

endlink,: the link to pretend is the end effector

The joint position vector before the inverse kinematics is returned if the algorithm does not converge.

Reimplemented in [Robot](#), [mRobot](#), and [mRobot_min_para](#).

Definition at line 91 of file invkine.cpp.

References dof, get_available_dof(), get_available_q(), ITOL, jacobian(), kine(), links, M_PI, NITMAX, and set_q().

4.22.4.9 ReturnMatrix Robot_basic::jacobian_DLS_inv (const double *eps*, const double *lambda_max*, const int *ref* = 0) const

Inverse Jacobian based on damped least squares inverse.

Parameters:

eps,: Range of singular region.

lambda_max,: Value to obtain a good solution in singular region.

ref,: Selected frame (ex: joint 4).

The Jacobian inverse, based on damped least squares, is

$$J^{-1}(q) = (J^T(q)J(q) + \lambda^2 I)^{-1} J^T(q)$$

where λ and I is a damping factor and the identity matrix respectively. Based on SVD (Singular Value Decomposition) the Jacobian is $J = \sum_{i=1}^m \sigma_i u_i v_i^T$, where u_i , v_i and σ_i are respectively the input vector, the output vector and the singular values ($\sigma_1 \geq \sigma_2 \geq \dots \geq \sigma_r \geq 0$, r is the rank of J). Using the previous equations we obtain

$$J^{-1}(q) = \sum_{i=1}^m \frac{\sigma_i}{\sigma_i^2 + \lambda_i^2} v_i u_i$$

A singular region, based on the smallest singular value, can be defined by

$$\lambda^2 = \begin{cases} 0 & \text{si } \sigma_6 \geq \epsilon \\ \left(1 - \left(\frac{\sigma_6}{\epsilon}\right)^2\right) \lambda_{max}^2 & \text{sinon} \end{cases}$$

Definition at line 169 of file kinemat.cpp.

Referenced by Clik::q_qdot(), and Resolved_acc::torque_cmd().

4.22.4.10 ReturnMatrix Robot_basic::acceleration (const ColumnVector & *q*, const ColumnVector & *qp*, const ColumnVector & *tau_cmd*, const ColumnVector & *Fext*, const ColumnVector & *Next*)

Joints acceleration.

The robot dynamics is

$$B(q)\ddot{q} + C(q, \dot{q})\dot{q} + D\dot{q} + g(q) = \tau - J^T(q)f$$

then the joint acceleration is

$$\ddot{q} = B^{-1}(q)(\tau - J^T(q)f - C(q, \dot{q})\dot{q} - D\dot{q} - g(q))$$

Definition at line 112 of file dynamics.cpp.

References dof, and inertia().

4.22.4.11 ReturnMatrix Robot_basic::dtau_dq (const ColumnVector & q, const ColumnVector & qp, const ColumnVector & qpp)

Sensitivity of the dynamics with respect to q .

This function computes $S_2(q, \dot{q}, \ddot{q})$.

Definition at line 58 of file sensitiv.cpp.

References dof.

4.22.4.12 ReturnMatrix Robot_basic::dtau_dqp (const ColumnVector & q, const ColumnVector & qp)

Sensitivity of the dynamics with respect to \dot{q} .

This function computes $S_1(q, \dot{q})$.

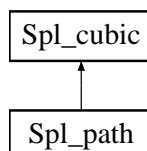
Definition at line 84 of file sensitiv.cpp.

References dof.

4.23 Spl_cubic Class Reference

```
#include <trajectory.h>
```

Inheritance diagram for Spl_cubic::



4.23.1 Detailed Description

Natural cubic splines class.

Definition at line 91 of file trajectory.h.

Public Member Functions

- [Spl_cubic](#) ()
- [Spl_cubic](#) (const Matrix &pts)
Constructor.
- short [interpolating](#) (const Real t, ColumnVector &s)
Interpolating the spline at time t. Extrapolating is not allowed.
- short [first_derivative](#) (const Real t, ColumnVector &ds)
Spline first derivative at time t.
- short [second_derivative](#) (const Real t, ColumnVector &dds)
Spline second derivative at time t.

Private Attributes

- int [nb_path](#)
Number of path, i.e: path in x,y,z nb_path=3.
- Matrix [Ak](#)
- Matrix [Bk](#)
- Matrix [Ck](#)

- Matrix [Dk](#)
- RowVector [tk](#)

Time at control points.

- bool [bad_data](#)

Status flag.

4.23.2 Constructor & Destructor Documentation

4.23.2.1 Spl_cubic::Spl_cubic (const Matrix & *pts*)

Constructor.

Parameters:

pts,: Matrix containing the spline data.

The first line of the Matrix contain the sampling time Second line contain data (sk) to create spline i. Third " " i+1. on Nth line i+N.

The spline has the following form:

$$s = A_k(t - t_k)^3 + B_k(t - t_k)^2 + C_k(t - t_k) + D_k$$

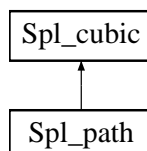
Definition at line 58 of file trajectory.cpp.

References [Ak](#), [bad_data](#), [Bk](#), [Ck](#), [Dk](#), [nb_path](#), and [tk](#).

4.24 Spl_path Class Reference

```
#include <trajectory.h>
```

Inheritance diagram for Spl_path::



4.24.1 Detailed Description

Cartesian or joint space trajectory.

Definition at line 120 of file trajectory.h.

Public Member Functions

- [Spl_path](#) ()
- **Spl_path** (const std::string &filename)
- [Spl_path](#) (const Matrix &x)
Constructor.
- short [p](#) (const Real time, ColumnVector &p)
Position vector at time t.
- short [p_pdot](#) (const Real time, ColumnVector &p, ColumnVector &pdot)
Position and velocity vector at time t.
- short [p_pdot_pddot](#) (const Real time, ColumnVector &p, ColumnVector &pdot, ColumnVector &pddot)
Position, velocity and acceleration vector at time t.
- short [get_type](#) ()
- double [get_final_time](#) ()

Private Attributes

- short [type](#)
Cartesian space or joint space.

- double [final_time](#)
Spline final time.

4.25 Spl_Quaternion Class Reference

```
#include <trajectory.h>
```

4.25.1 Detailed Description

Cubic quaternions spline.

Definition at line 147 of file trajectory.h.

Public Member Functions

- [Spl_Quaternion](#) ()
- [Spl_Quaternion](#) (const std::string &filename)
- [Spl_Quaternion](#) (const [quat_map](#) &quat)
Constructor.
- short [quat](#) (const Real t, [Quaternion](#) &s)
Quaternion interpolation.
- short [quat_w](#) (const Real t, [Quaternion](#) &s, ColumnVector &w)
Quaternion interpolation and angular velocity.

Private Attributes

- [quat_map](#) [quat_data](#)
Data at control points.

4.25.2 Member Function Documentation

4.25.2.1 short Spl_Quaternion::quat (const Real t, [Quaternion](#) & s)

[Quaternion](#) interpolation.

$$S_n(t) = Squad(q_n, a_n, a(n+1), q(n+1), t)$$

Definition at line 503 of file trajectory.cpp.

References NOT_IN_RANGE, [quat_data](#), [Slerp\(\)](#), and [Squad\(\)](#).

4.26 Stewart Class Reference

```
#include <stewart.h>
```

4.26.1 Detailed Description

[Stewart](#) definitions.

Definition at line 143 of file `stewart.h`.

Public Member Functions

- [Stewart](#) ()
Default Constructor.
- [Stewart](#) (const Matrix InitPlat, bool Joint=true)
Constructor.
- [Stewart](#) (const [Stewart](#) &x)
Copy Constructor.
- **Stewart** (const std::string &filename, const std::string &PlatformName)
- [~Stewart](#) ()
Destructor.
- const [Stewart](#) & [operator=](#) (const [Stewart](#) &x)
- void [set_Joint](#) (const bool _Joint)
Set the position of the universal joint on the links.
- void [set_q](#) (const ColumnVector _q)
Set the position of the platform.
- void [set_dq](#) (const ColumnVector _dq)
Set the platform's speed.
- void [set_ddq](#) (const ColumnVector _ddq)
Set the platform's acceleration.
- void [set_pR](#) (const ColumnVector _pR)
Set the position of the center of mass of the platform.
- void [set_pIp](#) (const Matrix _pIp)

Set the inertia matrix of the platform.

- void `set_mp` (const Real `_mp`)
Set the mass of the platform.
- bool `get_Joint` () const
Return the position of the universal joint (true if at base, false if at platform).
- ReturnMatrix `get_q` () const
Return the position of the platform.
- ReturnMatrix `get_dq` () const
Return the speed of the platform.
- ReturnMatrix `get_ddq` () const
Return the acceleration of the platform.
- ReturnMatrix `get_pR` () const
Return the position of the center of mass of the platform.
- ReturnMatrix `get_pIp` () const
Return the inertia matrix of the platform.
- Real `get_mp` () const
Return the mass of the platform.
- void `Transform` ()
Call the functions corresponding to the basic parameters when q changes.
- ReturnMatrix `Find_wRp` ()
Return the rotation matrix wRp .
- ReturnMatrix `Find_Omega` ()
Return the angular speed of the platform.
- ReturnMatrix `Find_Alpha` ()
Return the angular acceleration of the platform.
- ReturnMatrix `jacobian` ()
Return the jacobian matrix of the platform.
- ReturnMatrix `Find_InvJacob1` ()

Return the first intermediate jacobian matrix (reverse) of the platform.

- ReturnMatrix [Find_InvJacob2](#) ()

Return the second intermediate jacobian matrix (reverse) of the platform.

- ReturnMatrix [jacobian_dot](#) ()

Return time derivative of the inverse jacobian matrix of the platform.

- ReturnMatrix [Find_dl](#) ()

Return the extension rate of the links in a vector.

- ReturnMatrix [Find_ddl](#) ()

Return the extension acceleration of the links in a vector.

- ReturnMatrix [Find_C](#) (const Real Gravity=GRAVITY)

Return intermediate matrix C for the dynamics calculations.

- ReturnMatrix [Torque](#) (const Real Gravity=GRAVITY)

Return the torque vector of the platform.

- ReturnMatrix [JointSpaceForceVct](#) (const Real Gravity=GRAVITY)

Return a vector containing the six actuation force components.

- ReturnMatrix [InvPosKine](#) ()

Return the length of the links in a vector.

- ReturnMatrix [ForwardKine](#) (const ColumnVector guess_q, const ColumnVector l_given, const Real tolerance=0.001)

Return the position vector of the platform (vector q).

- ReturnMatrix [Find_h](#) (const Real Gravity=GRAVITY)

Return the intermediate matrix corresponding to the Coriolis and centrifugal + gravity force/torque components.

- ReturnMatrix [Find_M](#) ()

Return the intermediate matrix corresponding to the inertia matrix of the machine.

- ReturnMatrix [ForwardDyn](#) (const ColumnVector Torque, const Real Gravity=GRAVITY)

Return the acceleration vector of the platform (ddq).

- void [Find_Mc_Nc_Gc](#) (Matrix &Mc, Matrix &Nc, Matrix &Gc)

Return(!) the intermediates matrix for forward dynamics with actuator dynamics.

- ReturnMatrix [ForwardDyn_AD](#) (const ColumnVector Command, const Real t)
Return the acceleration of the platform ([Stewart](#) platform mechanism dynamics including actuator dynamics).

Public Attributes

- Matrix [wRp](#)
Rotation matrix describing the orientation of the platform.
- Matrix [Jacobian](#)
Jacobian matrix.
- Matrix [IJ1](#)
Inverse of the first intermediate Jacobian matrix.
- Matrix [IJ2](#)
Inverse of the second intermediate Jacobian matrix.
- ColumnVector [dl](#)
Rate of expansion vector.
- ColumnVector [ddl](#)
Acceleration of expansion vector.
- ColumnVector [Alpha](#)
Angular speed of the platform.
- ColumnVector [Omega](#)
Angular acceleration of the platform.

Private Attributes

- bool [UJointAtBase](#)
Gives the position of the universal joint (true if at base, false if at platform).
- ColumnVector [q](#)
Platform position (xyz + euler angles).
- ColumnVector [dq](#)

Platform speed.

- ColumnVector [ddq](#)

Platform acceleration.

- ColumnVector [pR](#)

Platform center of mass (in its own referential).

- ColumnVector [gravity](#)

Gravity vector.

- Matrix [pIp](#)

Platform Inertia (local ref.).

- Real [mp](#)

Platform mass.

- Real [p](#)

Pitch of the ballscrew (links).

- Real [n](#)

Gear ratio (links motor).

- Real [Js](#)

Moment of inertia (ballscrew).

- Real [Jm](#)

Moment of inertia (motor).

- Real [bs](#)

Viscous damping coefficient of the ballscrew.

- Real [bm](#)

Viscous damping coefficient of the motor.

- Real [Kb](#)

Motor back EMF.

- Real [L](#)

Motor Inductance.

- Real [R](#)

Motor armature resistance.

- Real [Kt](#)

Motor torque.

- [LinkStewart Links](#) [6]

Platform links.

4.26.2 Constructor & Destructor Documentation

4.26.2.1 `Stewart::Stewart (const Matrix InitPlatt, bool Joint = true)`

Constructor.

Parameters:

InitPlatt,: Platform initialization matrix.

Joint,: bool indicating where is the universal joint

Definition at line 853 of file `stewart.cpp`.

References `bm`, `bs`, `ddq`, `dq`, `Find_wRp()`, `gravity`, `Jm`, `Js`, `Kb`, `Kt`, `L`, `Links`, `M_PI`, `mp`, `n`, `p`, `pIp`, `pR`, `q`, `R`, `UJointAtBase`, and `wRp`.

4.26.3 Member Function Documentation

4.26.3.1 `const Stewart & Stewart::operator= (const Stewart & x)`

Definition at line 1004 of file `stewart.cpp`.

References `bm`, `bs`, `ddq`, `dq`, `gravity`, `Jm`, `Js`, `Kb`, `Kt`, `L`, `Links`, `mp`, `n`, `p`, `pIp`, `pR`, `q`, `R`, and `UJointAtBase`.

4.26.3.2 `void Stewart::Transform ()`

Call the functions corresponding to the basic parameters when `q` changes.

These functions are called by `Transform`:

- [Find_wRp\(\)](#)
- [LinkStewart::LTransform\(\)](#) for each link
- [Find_InvJacob1\(\)](#)

- [Find_InvJacob2\(\)](#)
- [jacobian\(\)](#)

Definition at line 1160 of file `stewart.cpp`.

References `Find_InvJacob1()`, `Find_InvJacob2()`, `Find_wRp()`, `IJ1`, `IJ2`, `jacobian()`, `Jacobian`, `Links`, `q`, and `wRp`.

Referenced by `set_q()`.

4.26.3.3 ReturnMatrix Stewart::Find_wRp ()

Return the rotation matrix `wRp`.

Eq of the matrix:

$$wRp = \begin{pmatrix} \cos(\psi) \cos(\phi) - \cos(\theta) \sin(\phi) \sin(\psi) & -\sin(\psi) \cos(\phi) - \cos(\theta) \sin(\phi) \cos(\psi) & \sin(\theta) \sin(\phi) \\ \cos(\psi) \sin(\phi) + \cos(\theta) \cos(\phi) \sin(\psi) & -\sin(\psi) \sin(\phi) + \cos(\theta) \cos(\phi) \cos(\psi) & -\sin(\theta) \cos(\phi) \\ \sin(\psi) \sin(\theta) & \cos(\psi) \sin(\theta) & \cos(\theta) \end{pmatrix}$$

Where:

- ψ, θ, ϕ , are the three Euler angles of the platform.

Definition at line 1186 of file `stewart.cpp`.

References `q`.

Referenced by `Stewart()`, and `Transform()`.

4.26.3.4 ReturnMatrix Stewart::Find_Omega ()

Return the angular speed of the platform.

Eq:

$$\omega = \begin{pmatrix} 0 & \cos(\phi) & \cos(\theta) \sin(\phi) \\ 0 & \sin(\phi) & -\sin(\theta) \cos(\phi) \\ 1 & 0 & \cos(\theta) \end{pmatrix} \begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix}$$

Where:

- ψ, θ, ϕ are the three Euler angles of the platform.
- $\dot{\psi}, \dot{\theta}, \dot{\phi}$ are the three Euler angle speed of the platform.

Definition at line 1223 of file `stewart.cpp`.

References `dq`, and `q`.

Referenced by `set_ddq()`, and `set_dq()`.

4.26.3.5 ReturnMatrix Stewart::Find_Alpha ()

Return the angular acceleration of the platform.

Eq:

$$\alpha = \begin{pmatrix} 0 & \cos(\phi) & \cos(\theta) \sin(\phi) \\ 0 & \sin(\phi) & -\sin(\theta) \cos(\phi) \\ 1 & 0 & \cos(\theta) \end{pmatrix} \begin{pmatrix} \ddot{\phi} \\ \ddot{\theta} \\ \ddot{\psi} \end{pmatrix} + \begin{pmatrix} 0 & -\dot{\phi} \sin(\phi) & \dot{\phi} \cos(\phi) \sin(\theta) + \dot{\theta} \sin(\phi) \cos(\theta) \\ 0 & \dot{\phi} \cos(\phi) & \dot{\phi} \sin(\phi) \sin(\theta) - \dot{\theta} \cos(\phi) \cos(\theta) \\ 0 & 0 & -\dot{\theta} \sin(\theta) \end{pmatrix} \begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix}$$

Where:

- ψ, θ, ϕ are the three Euler angles of the platform.
- $\dot{\psi}, \dot{\theta}, \dot{\phi}$ are the three Euler angle speed of the platform.
- $\ddot{\psi}, \ddot{\theta}, \ddot{\phi}$ are the three Euler angle acceleration of the platform.

Definition at line 1261 of file stewart.cpp.

References ddq, dq, and q.

Referenced by set_ddq().

4.26.3.6 ReturnMatrix Stewart::jacobian ()

Return the jacobian matrix of the platform.

Eq:

$$J = J_1^{-1} J_2^{-1}$$

Where:

- J_1 and J_2 are intermediate matrix([Find_InvJacob1\(\)](#), [Find_InvJacob2\(\)](#))

Definition at line 1290 of file stewart.cpp.

References IJ1, and IJ2.

Referenced by Transform().

4.26.3.7 ReturnMatrix Stewart::Find_InvJacob1 ()

Return the first intermediate jacobian matrix (reverse) of the platform.

Eq:

$$J_1^{-1} = \begin{pmatrix} n_1^T & (a_{w1} \times n_1)^T \\ \vdots & \vdots \\ n_6^T & (a_{w6} \times n_6)^T \end{pmatrix}$$

Where:

- n_1 to n_6 are the unit vector of the links
- a_{w1} to a_{w6} are the attachment point of the links to the platform in the world referential

Definition at line 1316 of file stewart.cpp.

References Links, LinkStewart::UnitV, and wRp.

Referenced by JointSpaceForceVct(), and Transform().

4.26.3.8 ReturnMatrix Stewart::Find_InvJacob2 ()

Return the second intermediate jacobian matrix (reverse) of the platform.

Eq:

$$J_2^{-1} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \cos \phi & \sin \phi \sin \theta \\ 0 & 0 & 0 & 0 & \sin \phi & -\cos \phi \sin \theta \\ 0 & 0 & 0 & 1 & 0 & \cos \theta \end{pmatrix}$$

Where:

- ϕ and θ are two of the euler angle of the platform (vector q)

Definition at line 1344 of file stewart.cpp.

References q.

Referenced by Transform().

4.26.3.9 ReturnMatrix Stewart::jacobian_dot ()

Return time deriative of the inverse jacobian matrix of the platform.

Eq:

$$\frac{dJ^{-1}}{dt} = \frac{dJ_1^{-1}}{dt} J_2^{-1} + J_1^{-1} \frac{dJ_2^{-1}}{dt}$$

$$\frac{dJ_1^{-1}}{dt} = \begin{pmatrix} (\omega_1 \times n_1)^T & ((\omega \times a_{w1}) \times n_1 + a_{w1} \times (\omega_1 \times n_1))^T \\ \vdots & \vdots \\ (\omega_6 \times n_6)^T & ((\omega \times a_{w6}) \times n_6 + a_{w6} \times (\omega_6 \times n_6))^T \end{pmatrix}$$

$$\frac{dJ_2^{-1}}{dt} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\dot{\phi} \sin \phi & \dot{\phi} \cos \phi \sin \theta + \dot{\theta} \sin \phi \cos \theta \\ 0 & 0 & 0 & 0 & \dot{\phi} \cos \phi & \dot{\phi} \sin \phi \sin \theta + \dot{\theta} \cos \phi \cos \theta \\ 0 & 0 & 0 & 0 & 0 & -\dot{\theta} \sin \theta \end{pmatrix}$$

Where:

- ω_i is the angular speed vector of each link
- n is the unit vector of the link
- ω is the angular speed vector of the platform
- a_{wi} is the position vector of the attachment point of the link to the platform
- ϕ and θ are two of the Euler angle (vector q)
- $\dot{\phi}$ and $\dot{\theta}$ are two of the Euler angle speed (vector dq)

Definition at line 1389 of file stewart.cpp.

References dl, dq, IJ1, IJ2, L, LinkStewart::L, Links, Omega, q, and LinkStewart::Unit-V.

Referenced by Find_ddl(), and Find_Mc_Nc_Gc().

4.26.3.10 ReturnMatrix Stewart::Find_dl ()

Return the extension rate of the links in a vector.

Eq:

$$\dot{l} = J^{-1} \dot{q}$$

Where:

- J^{-1} is the inverse Jacobian matrix of the platform
- \dot{q} is the dq vector

Definition at line 1451 of file stewart.cpp.

References dq, and Jacobian.

Referenced by set_dq().

4.26.3.11 ReturnMatrix Stewart::Find_ddl ()

Return the extension acceleration of the links in a vector.

Eq:

$$\ddot{l} = J^{-1}\ddot{q} + \frac{dJ^{-1}}{dt}\dot{q}$$

Where:

- J^{-1} is the inverse jacobian matrix of the platform
- \ddot{q} is the ddq vector

Definition at line 1472 of file stewart.cpp.

References ddq, dq, Jacobian, and jacobian_dot().

Referenced by set_ddq(), and set_dq().

4.26.3.12 ReturnMatrix Stewart::Find_C (const Real Gravity = GRAVITY)

Return intermediate matrix C for the dynamics calculations.

Eqs:

$$\ddot{x}_g = \ddot{x} + \alpha \times \bar{r} + \omega(\omega \times \bar{r})$$

$$\bar{r} = {}^w R_p \cdot {}^p \bar{r}$$

$$\bar{I}_p = {}^w R_p {}^p \bar{I}_p {}^w R_p^T$$

$$C = \begin{pmatrix} m_p G - m_p \ddot{x}_g - \sum F_i^n \\ m_p \bar{r} \times G - m_p (\bar{r} \times \ddot{x}_g - \bar{I}_p \alpha + \bar{I}_p \omega \times \omega - \sum a_{wi} \times F_i^n - \sum M_i) \end{pmatrix}$$

Where:

- \ddot{x}_g is the acceleration of the platform center of mass.
- \ddot{x} is the acceleration of the platform center (first three elements of the ddq vector).
- α is the angular acceleration of the platform.
- \bar{r} is the platform center of mass in the world referential.
- ω is the angular speed of the platform.
- ${}^w R_p$ is the rotational matrix of the two referentials (world and platform).
- ${}^p \bar{r}$ is the vector of the center of mass of the platform with reference to the local frame (platform).
- ${}^p \bar{I}_p$ is the constant mass moments of inertia of the platform with reference to the local frame (platform).

- m_p is the mass of the platform.
- G is the gravity.
- F_i^n is the normal force transferred from the platform to the link.
- \bar{I}_p is the constant mass moments of inertia of the platform in the world referential.
- a_{wi} is the position of the attachment point of each link to the platform in the world referential.
- M_i is the moment transferred from the platform to the link (not present is the spherical joint is at the platform end).

Definition at line 1512 of file stewart.cpp.

References Alpha, ddq, gravity, Links, LinkStewart::Moment(), mp, Omega, pIp, pR, UJointAtBase, and wRp.

Referenced by JointSpaceForceVct().

4.26.3.13 ReturnMatrix Stewart::Torque (const Real Gravity = GRAVITY)

Return the torque vector of the platform.

Parameters:

Gravity,: Gravity (9.81)

Eq:

$$\tau = J^{-T} F$$

Where:

- J is the Jacobian matrix of the platform.
- F is the joint space force vector ([JointSpaceForceVct\(\)](#)).

Definition at line 1625 of file stewart.cpp.

References ddl, dl, Jacobian, JointSpaceForceVct(), and Links.

Referenced by Find_h(), Find_M(), and stewartmain().

4.26.3.14 ReturnMatrix Stewart::JointSpaceForceVct (const Real *Gravity* = GRAVITY)

Return a vector containing the six actuation force components.

Parameters:

Gravity,: Gravity (9.81)

See the description of [LinkStewart::ActuationForce\(\)](#).

Definition at line 1595 of file stewart.cpp.

References Find_C(), Find_InvJacob1(), IJ1, and Links.

Referenced by Torque().

4.26.3.15 ReturnMatrix Stewart::InvPosKine ()

Return the lenght of the links in a vector.

The goal of the inverse kinematic is to find the lenght of each of the six links from the position of the platform (X,Y,Z, ψ,θ,ϕ).

Definition at line 1429 of file stewart.cpp.

References L, and Links.

Referenced by stewartmain().

4.26.3.16 ReturnMatrix Stewart::ForwardKine (const ColumnVector *guess_q*, const ColumnVector *l_given*, const Real *tolerance* = 0.001)

Return the position vector of the platform (vector q).

Parameters:

guess_q,: Approximation of real position

l_given,: Lenght of the 6 links

tolerance,: Ending criterion

The Newton-Raphson method is used to solve the forward kinematic problem. It is a numerical iterative technic that simplify the solution. An approximation of the answer has to be guess for this method to work.

Eq:

$$q_i = q_{i-1} - J_{q_{i-1}}(l_{q_{i-1}} - l)$$

Where:

- q_i is the position vector of the platform at the i th iteration.
- q_{i-1} is the position vector of the platform at the $(i-1)$ th iteration.
- $J_{q_{i-1}}$ is the Jacobian matrix of the platform at the position of the q_{i-1} vector.
- $l_{q_{i-1}}$ is the length vector of the links at the $(i-1)$ th position of the platform.
- l is the real length vector of the links.

Definition at line 1567 of file stewart.cpp.

References Jacobian, L, Links, q, and set_q().

Referenced by stewartmain().

4.26.3.17 ReturnMatrix Stewart::Find_h (const Real Gravity = GRAVITY)

Return the intermediate matrix corresponding to the Coriolis and centrifugal + gravity force/torque components.

Parameters:

Gravity,: Gravity (9.81)

h is found by setting the ddq vector to zero and then calling the torque routine. The vector returned by [Torque\(\)](#) is equal to h .

Definition at line 1646 of file stewart.cpp.

References set_ddq(), and Torque().

Referenced by Find_Mc_Nc_Gc(), and ForwardDyn().

4.26.3.18 ReturnMatrix Stewart::Find_M ()

Return the intermediate matrix corresponding to the inertia matrix of the machine.

M is found by setting the dq and Gravity vectors to zero and the ddq vector to zero except for the i th element that is set to one. Then, the i th row of M is equal to the matrix returned by [Torque\(\)](#).

Definition at line 1663 of file stewart.cpp.

References dq, set_ddq(), set_dq(), and Torque().

Referenced by Find_Mc_Nc_Gc(), and ForwardDyn().

4.26.3.19 ReturnMatrix Stewart::ForwardDyn (const ColumnVector *T*, const Real *Gravity* = GRAVITY)

Return the acceleration vector of the platform (ddq).

Parameters:

T,: torque vector

Gravity,: Gravity (9.81)

Eq:

$$ddq = M^{-1}(\tau - h)$$

Where:

- M is from [Find_M\(\)](#) routine.
- τ is the torque vector.
- h is from [Find_h\(\)](#) routine.

Definition at line 1701 of file stewart.cpp.

References [Find_h\(\)](#), and [Find_M\(\)](#).

Referenced by [stewartmain\(\)](#).

4.26.3.20 void Stewart::Find_Mc_Nc_Gc (Matrix & *Mc*, Matrix & *Nc*, Matrix & *Gc*)

Return(!) the intermediates matrix for forward dynamics with actuator dynamics.

Parameters:

Mc,: Inertia matrix of the machine

Nc,: Coriolis and centrifugal force/torque component

Gc,: Gravity force/torque component

Eq:

$$K_a = \frac{p}{2\pi n} I_{6 \times 6} \quad M_a = \frac{2\pi}{np} (J_s + n^2 J_m) I_{6 \times 6} \quad V_a = \frac{2\pi}{np} (b_s + n^2 b_m) I_{6 \times 6} \quad M_c = K_a J^T M + M_a J^{-1} \quad N_c = K_a J^T N + (V_a J^{-1} + M_a \frac{dJ^{-1}}{dt}) dq \quad G_c = K_a J^T G \quad \text{Where:}$$

- p is the pitch of the ballscrew.
- n is the gear ratio.

- $I_{6 \times 6}$ is the Identity matrix.
- J_s is the mass moment of inertia of the ballscrew.
- J_m is the mass moment of inertia of the motor.
- b_s is the viscous damping coefficient of the ballscrew.
- b_m is the viscous damping coefficient of the motor.
- J is the Jacobian matrix of the platform.

Definition at line 1736 of file stewart.cpp.

References `bm`, `bs`, `dq`, `Find_h()`, `Find_M()`, `Jacobian`, `jacobian_dot()`, `Jm`, `Js`, `M_PI`, `n`, `p`, and `set_dq()`.

Referenced by `ForwardDyn_AD()`.

4.26.3.21 ReturnMatrix Stewart::ForwardDyn_AD (const ColumnVector Command, const Real t)

Return the acceleration of the platform ([Stewart](#) platform mechanism dynamics including actuator dynamics).

Parameters:

- Command,:** Vector of the 6 motors voltages.
t,: period of time use to find the currents (di/dt)

Voltages with back emf:

$$V' = V - J^{-1} \dot{q} \left(\frac{2\pi}{p} \right) K_b$$

Currents:

$$I = \frac{I_{6 \times 6}}{L} e^{(-R \cdot t / L)} V'$$

Motor torque:

$$\tau_m = I K_t$$

Platform acceleration:

$$\ddot{q} = M_c^{-1} (\tau_m - Nc - Gc)$$

Where:

- J is the Jacobian matrix of the platform.
- \dot{q} is the dq vector.

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- p is the pitch of the ballscrew.
- K_b is the motor back emf constant.
- L is the motor armature inductance.
- R is the motor armature resistance.
- K_t is the motor torque constant.
- M_c , N_c and G_c are from [Find_Mc_Nc_Gc\(\)](#).

Definition at line 1792 of file stewart.cpp.

References dq , [Find_Mc_Nc_Gc\(\)](#), Jacobian, K_b , K_t , L , M_{PI} , p , and R .

Referenced by `stewartmain()`.

4.27 Trajectory_Select Class Reference

```
#include <trajectory.h>
```

4.27.1 Detailed Description

Trajectory class selection.

Definition at line 164 of file trajectory.h.

Public Member Functions

- [Trajectory_Select](#) ()
Constructor.
- [Trajectory_Select](#) (const std::string &filename)
- [Trajectory_Select](#) & [operator=](#) (const [Trajectory_Select](#) &x)
Overload = operator.
- void [set_trajectory](#) (const std::string &filename)

Public Attributes

- short [type](#)
Cartesian or joint space.
- [Spl_path](#) path
Spl_path instance.
- [Spl_Quaternion](#) path_quat
Spl_Quaternion instance.

Private Attributes

- bool [quaternion_active](#)
Using Spl_Quaternion.

Chapter 5

ROBOOP, A Robotics Object Oriented Package in C++ File Documentation

5.1 bench.cpp File Reference

5.1.1 Detailed Description

A benchmark file.

Prints the time, on the console, to perform certain operations.

Definition in file [bench.cpp](#).

```
#include <time.h>
#include "robot.h"
#include "stewart.h"
```

Defines

- `#define` [NTRY](#) 2000

Functions

- `int` [stewartmain](#) (void)
- `int` [main](#) (void)

Variables

- static const char [rcsid](#) [] = "\$Id: bench.cpp,v 1.20 2005/07/01 16:16:35 gourdeau Exp \$"

RCS/CVS version.

- Real [Stewart_Ini](#) []
- Real [Stewart_q](#) []
- Real [Stewart_qg](#) []
- Real [Stewart_l](#) []
- Real [Stewart_dq](#) []
- Real [Stewart_ddq](#) []
- Real [Stewart_tddq](#) []
- Real [Comm](#) []
- Real [Tau](#) []
- const Real [PUMA560_data](#) []

5.1.2 Variable Documentation

5.1.2.1 Real [Comm](#)[]

Initial value:

```
{1, 0, 0, -10, 0, 0}
```

Definition at line 96 of file bench.cpp.

Referenced by stewartmain().

5.1.2.2 const Real [PUMA560_data](#)[]

Initial value:

```
{0, 0, 0, 0, M_PI/2.0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0.35, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0.4318, 0, 0, 0, 0, 17.4, -0.3638, 0.006, 0.2275, 0.13, 0, 0, 0.524, 0, 0.539, 0, 0, 0, 0.15005, 0.0203, -M_PI/2.0, 0, 0, 0, 4.8, -0.0203, -0.0141, 0.07, 0.066, 0, 0, 0.086, 0, 0, 0.4318, 0.0, M_PI/2.0, 0, 0, 0, 0.82, 0, 0.019, 0, 0.0018, 0, 0, 0.0013, 0, 0.0018, 0, 0, 0, 0.0, -M_PI/2.0, 0, 0, 0, 0.34, 0.0, 0.0, 0.0, 0.0003, 0.0, 0.0, 0.0004, 0.0, 0.0003, 0, 0, 0, 0, 0, 0, 0, 0.09, 0.0, 0.0, 0.032, 0.00015, 0.0, 0.0, 0.00015, 0.0, 0.00004, 0,
```

Definition at line 175 of file bench.cpp.

Referenced by dynamics_demo(), and main().

Initial value:

```
{-10.0, -10.0, -10, -10.0, -10, -10}
```

Definition at line 92 of file bench.cpp.

Referenced by `stewartmain()`.

Initial value:

 $\{0.2, 0.3, -0.4, 0.1, -1.4, 0.1\}$

Definition at line 90 of file bench.cpp.

Referenced by `stewartmain()`.

Initial value:

```
{1.758, 2.8, -1.015, 0.225, 0.0, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0, 0.0,  
1.6021, 3.07, -0.925, 0.1125, 0.1949, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0,  
-1.7580, 2.8, -1.015, -0.1125, 0.1949, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0,  
-1.6021, 3.07, -0.925, -0.225, 0.0, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0,  
0.0, 2.8, 2.03, -0.1125, -0.1949, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0, 0.0,  
0.0, 3.07, 1.85, 0.1125, -0.1949, -0.228, 3.358, 0.05, 4.237, 0.1406, 10, 12.5, 0.5, 0.35, 0.0, 0.0, 0.0,  
0.0, 0.0, -0.114, 1.001, 0.59, 0.843, 10, 0.12, 0.04, 0.5, 0.5, 0.5, 1.5, 0.5, 0.005, 5.44, 0.443}
```

Definition at line 75 of file bench.cpp.

Referenced by `stewartmain()`.

Initial value:

 $\{3.0508, 3.2324, 3.2997, 3.4560, 3.5797, 3.6935\}$

Definition at line 88 of file bench.cpp.

Referenced by `stewartmain()`.

5.1.2.7 Real [Stewart_q\[\]](#)

Initial value:

```
{0.2, 0.3, -0.4, 0.1, -1.4, 0.1}
```

Definition at line 84 of file bench.cpp.

Referenced by stewartmain().

5.1.2.8 Real [Stewart_qg\[\]](#)

Initial value:

```
{0.25, 0.25, -0.45, 0.07, -1.7, 0.07}
```

Definition at line 86 of file bench.cpp.

Referenced by stewartmain().

5.1.2.9 Real [Stewart_tddq\[\]](#)

Initial value:

```
{0, 0, 0, 0, 0, 0}
```

Definition at line 94 of file bench.cpp.

Referenced by stewartmain().

5.1.2.10 Real [Tau\[\]](#)

Initial value:

```
{126.219689, 789.968672, 0.708602, 79.122963, 81.806978, -31.61797}
```

Definition at line 98 of file bench.cpp.

Referenced by stewartmain().

5.2 clik.cpp File Reference

5.2.1 Detailed Description

[Clik](#) member functions.

Definition in file [klik.cpp](#).

```
#include "quaternion.h"
```

```
#include "klik.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: klik.cpp,v 1.6 2006/05/16 16:11:15 gourdeau
Exp \$"

RCS/CVS version.

5.3 clik.h File Reference

5.3.1 Detailed Description

Header file for [Clik](#) class definitions.

Definition in file [klik.h](#).

```
#include "robot.h"
```

Classes

- class [Clik](#)
Handle Closed Loop Inverse Kinematics scheme.

Defines

- #define [CLICK_DH](#) 1
Using [Clik](#) under DH notation.
- #define [CLICK_mDH](#) 2
Using [Clik](#) under modified DH notation.
- #define [CLICK_mDH_min_para](#) 3
Using [Clik](#) under modified DH notation with minimum inertial parameters.

Variables

- static const char [header_clik_rcsid](#) [] = "\$Id: klik.h,v 1.6 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/CVS version.

5.4 comp_dq.cpp File Reference

5.4.1 Detailed Description

Delta torque (linearized dynamics).

Definition in file [comp_dq.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: comp_dq.cpp,v 1.17 2004/07/06 02:16:36 gourdeau Exp \$"
RCS/CVS version.

5.5 comp_dqp.cpp File Reference

5.5.1 Detailed Description

Delta torque (linearized dynamics).

Definition in file [comp_dqp.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rsid](#) [] = "\$Id: comp_dqp.cpp,v 1.16 2004/07/06 02:16:36
gourdeau Exp \$"

RCS/CVS version.

5.6 config.cpp File Reference

5.6.1 Detailed Description

Configuration class functions.

Definition in file [config.cpp](#).

```
#include "config.h"
```

Namespaces

- namespace **std**

Variables

- static const char [rcsid](#) [] = "\$Id: config.cpp,v 1.20 2006/05/16 19:24:26 gourdeau Exp \$"

RCS/CVS version.

5.7 config.h File Reference

5.7.1 Detailed Description

Header file for [Config](#) class definitions.

Definition in file [config.h](#).

```
#include <iostream>
#include <string>
#include <iomanip>
#include <fstream>
#include <boost/lexical_cast.hpp>
#include <sstream>
#include <vector>
```

Classes

- struct [Data](#)
Basic data element used in [Config](#) class.
- class [Config](#)
Handle configuration files.

Defines

- #define [CAN_NOT_OPEN_FILE](#) -1
Return when can not open file.
- #define [CAN_NOT_CREATE_FILE](#) -2
Return when can not create a file.

Typedefs

- typedef std::vector< [Data](#) > [Conf_data](#)
Configuration data type.

Variables

- static const char `header_config_resid` [] = "\$Id: config.h,v 1.18 2006/05/16 19:24:26 gourdeau Exp \$"
RCS/CVS version.

5.8 control_select.cpp File Reference

5.8.1 Detailed Description

Controller selection class.

Definition in file [control_select.cpp](#).

```
#include "config.h"
#include "control_select.h"
#include "trajectory.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: control_select.cpp,v 1.7 2006/05/16 19:24:26 gourdeau Exp \$"
RCS/CVS version.

5.9 control_select.h File Reference

5.9.1 Detailed Description

Header file for [Control_Select](#) class definitions.

Definition in file [control_select.h](#).

```
#include <string>
```

```
#include "controller.h"
```

Classes

- class [Control_Select](#)
Select controller class.

Defines

- #define [NONE](#) 0
- #define [PD](#) 1
- #define [CTM](#) 2
- #define [RRA](#) 3
- #define [IMP](#) 4
- #define [CONTROLLER](#) "CONTROLLER"
- #define [PROPORTIONAL_DERIVATIVE](#) "PROPORTIONAL_DERIVATIVE"
- #define [COMPUTED_TORQUE_METHOD](#) "COMPUTED_TORQUE_METHOD"
- #define [RESOLVED_RATE_ACCELERATION](#) "RESOLVED_RATE_ACCELERATION"
- #define [IMPEDANCE](#) "IMPEDANCE"

Variables

- static const char [header_Control_Select_rcsid](#) [] = "\$Id: control_select.h,v 1.4 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/CVS version.

5.10 controller.cpp File Reference

5.10.1 Detailed Description

Differents controllers class.

Definition in file [controller.cpp](#).

```
#include "controller.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: controller.cpp,v 1.3 2005/11/15 19:06:13 gourdeau Exp \$"

RCS/CVS version.

5.11 controller.h File Reference

5.11.1 Detailed Description

Header file for controller class definitions.

Definition in file [controller.h](#).

```
#include "robot.h"
```

```
#include "quaternion.h"
```

Classes

- class [Impedance](#)
Impedance controller class.
- class [Resolved_acc](#)
Resolved rate acceleration controller class.
- class [Computed_torque_method](#)
Computer torque method controller class.
- class [Proportional_Derivative](#)
Proportional derivative controller class.

Defines

- #define [WRONG_SIZE](#) -1
Return value when input vectors or matrix don't have the right size.

Variables

- static const char [header_controller_rcsid](#) [] = "\$Id: controller.h,v 1.5 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/ CVS version.

5.12 delta_t.cpp File Reference

5.12.1 Detailed Description

Delta torque (linearized dynamics).

Definition in file [delta_t.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: delta_t.cpp,v 1.17 2005/07/01 16:11:45 gourdeau Exp \$"

RCS/CVS version.

5.13 demo.cpp File Reference

5.13.1 Detailed Description

A demo file.

Demos for homogeneous transforms, kinematics, etc.

Definition in file [demo.cpp](#).

```
#include "gnugraph.h"
#include "quaternion.h"
#include "robot.h"
#include "utils.h"
```

Functions

- void [homogen_demo](#) (void)
- void [kinematics_demo](#) (void)
- void [dynamics_demo](#) (void)
- int [main](#) (void)
- ReturnMatrix [xdot](#) (Real t, const Matrix &x)

Variables

- static const char [rcsid](#) [] = "\$Id: demo.cpp,v 1.34 2006/05/16 16:27:43 gourdeau Exp \$"
RCS/CVS version.
- const Real [RR_data](#) []
- const Real [RR_data_mdh](#) []
- const Real [RR_data_mdh_min_para](#) []
- const Real [RP_data](#) []
- const Real [PUMA560_data](#) []
- const Real [PUMA560_motor](#) []
- const Real [STANFORD_data](#) []
- [Robot robot](#)
- Matrix [K](#)
- ColumnVector [q0](#)

5.13.2 Variable Documentation

5.13.2.1 const Real PUMA560_data[]

Initial value:

```
{0, 0, 0, 0, M_PI/2.0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0.35, 0, 0, 0,
0, 0, 0, 0.4318, 0, 0, 0, 0, 17.4, -0.3638, 0.006, 0.2275, 0.13, 0, 0, 0.524, 0, 0.539, 0,
0, 0, 0.15005, 0.0203, -M_PI/2.0, 0, 0, 0, 4.8, -0.0203, -0.0141, 0.07, 0.066, 0, 0, 0.086,
0, 0, 0.4318, 0.0, M_PI/2.0, 0, 0, 0, 0.82, 0, 0.019, 0, 0.0018, 0, 0, 0.0013, 0, 0.0018, 0,
0, 0, 0, 0.0, -M_PI/2.0, 0, 0, 0, 0.34, 0.0, 0.0, 0.0, 0.0003, 0.0, 0.0, 0.0004, 0.0, 0.0003,
0, 0, 0, 0, 0, 0, 0, 0, 0.09, 0.0, 0.0, 0.032, 0.00015, 0.0, 0.0, 0.00015, 0.0, 0.00004, 0}
```

Definition at line 204 of file demo.cpp.

5.13.2.2 const Real PUMA560_motor[]

Initial value:

```
{200e-6, -62.6111, 1.48e-3, (.395 +.435)/2,
200e-6, 107.815, .817e-3, (.126 + .071)/2,
200e-6, -53.7063, 1.38e-3, (.132 + .105)/2,
33e-6, 76.0364, 71.2e-6, (11.2e-3 + 16.9e-3)/2,
33e-6, 71.923, 82.6e-6, (9.26e-3 + 14.5e-3)/2,
33e-6, 76.686, 36.7e-6, (3.96e-3 + 10.5e-3)/2}
```

Definition at line 211 of file demo.cpp.

Referenced by dynamics_demo(), and main().

5.13.2.3 const Real RP_data[]

Initial value:

```
{0, 0, 0, 0, -M_PI/2.0, 0, 0, 0, 2.0, 0, 0, 0.0, 1.0, 0, 0, 1.0, 0, 1.0, 0, 0, 0, 0, 0,
1, 0, 0, 0, 0, 0, 0, 0, 1.0, 0, 0, -1.0, 0.0833333, 0, 0, 0.0833333, 0, 0.0833333, 0, 0, 0, 0, 0}
```

Definition at line 201 of file demo.cpp.

Referenced by dynamics_demo(), and kinematics_demo().

5.13.2.4 const Real RR_data[]

Initial value:

```
{0, 0, 0, 1.0, 0, 0, 0, 0, 2.0, -0.5, 0, 0, 0, 0, 0, 0.1666666, 0, 0.1666666, 0, 0, 0, 0, 0,
0, 0, 0, 1.0, 0, 0, 0, 0, 1.0, -0.5, 0, 0, 0, 0, 0, 0.0833333, 0, 0.0833333, 0, 0, 0, 0, 0}
```

Definition at line 191 of file demo.cpp.

Referenced by dynamics_demo(), and kinematics_demo().

5.13.2.5 const Real [RR_data_mdh](#) []

Initial value:

```
{0, 0, 0, 1.0, 0, 0, 0, 0, 2.0, 0.5, 0, 0, 0, 0, 0, 0.16666666, 0, 0.16666666, 0, 0, 0, 0, 0,
0, 0, 0, 1.0, 0, 0, 0, 0, 1.0, 0.5, 0, 0, 0, 0, 0, 0.08333333, 0, 0.08333333, 0, 0, 0, 0, 0}
```

Definition at line 194 of file demo.cpp.

5.13.2.6 const Real [RR_data_mdh_min_para](#) []

Initial value:

```
{0, 0, 0, 1.0, 0, 0, 0, 0, 0, 0.0, 0, 0, 0, 0, 0, 0.0, 1.6666666, 0, 0, 0, 0, 0, 0,
0, 0, 0, 1.0, 0, 0, 0, 0, 0, 0.5, 0, 0, -0.25, 0, 0, 0, 0.0, 0.33333333, 0, 0, 0, 0, 0}
```

Definition at line 197 of file demo.cpp.

5.13.2.7 const Real [STANFORD_data](#) []

Initial value:

```
{0.0, 0.0, 0.4120, 0.0, -M_PI/2, 0,0,0,9.29, 0.0, 0.0175, -0.1105, 0.276, 0.0, 0, 0.255, 0.0, 0.071,0,0,
0.0, 0.0, 0.1540, 0.0, M_PI/2.0, 0,0,0,5.01, 0.0, -1.054, 0.0, 0.108, 0.0, 0.0, 0.018, 0.0, 0.1,0,0,0,0,
1.0, -M_PI/2.0, 0.0, 0.0, 0.0, 0,0,0,4.25, 0.0, 0.0, -6.447, 2.51, 0.0, 0.0, 2.51, 0.0, 0.006,0,0,0,0,0,
0.0, 0.0, 0.0, 0.0, -M_PI/2.0, 0,0,0,1.08, 0.0, 0.092, -0.054, 0.002, 0.0, 0.0, 0.001, 0.0, 0.001,0,0,0,
0.0, 0.0, 0.0, 0.0, M_PI/2.0, 0,0,0,0.63, 0.0, 0.0, 0.566, 0.003, 0.0, 0.0, 0.003, 0.0, 0.0004,0,0,0,0,
0.0, 0.0, 0.2630, 0.0, 0.0, 0,0,0,0.51, 0.0, 0.0, 1.5540, 0.013, 0.0, 0.0, 0.013, 0.0, 0.0003,0,0,0,0,0,0}
```

Definition at line 219 of file demo.cpp.

5.14 demo_2dof_pd.cpp File Reference

5.14.1 Detailed Description

A demo file.

This demo file shows a two degree of freedom robots controller by a pd controller. The robot is define by the file "conf/rr_dh.conf", while the controller is defined by the file "conf/pd_2dof.conf". The desired joint trajectory is defined by the file "conf/q_2dof.dat";

Definition in file [demo_2dof_pd.cpp](#).

```
#include "gnugraph.h"
#include "controller.h"
#include "control_select.h"
#include "dynamics_sim.h"
#include "robot.h"
#include "trajectory.h"
```

Classes

- class [New_dynamics](#)

This is an example of customize [Dynamics](#) class.

Functions

- int [main](#) ()

Variables

- static const char [rcsid](#) [] = "\$Id: demo_2dof_pd.cpp,v 1.2 2006/05/16 16:27:43 gourdeau Exp \$"

RCS/CVS version.

5.15 dynamics.cpp File Reference

5.15.1 Detailed Description

Manipulator dynamics functions.

Definition in file [dynamics.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: dynamics.cpp,v 1.34 2006/05/19 18:32:30 gourdeau Exp \$"
RCS/CVS version.

5.16 dynamics_sim.cpp File Reference

5.16.1 Detailed Description

Basic dynamics simulation class.

Definition in file [dynamics_sim.cpp](#).

```
#include "dynamics_sim.h"
```

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: dynamics_sim.cpp,v 1.6 2006/05/19 21:05:57 gourdeau Exp \$"

RCS/CVS version.

5.17 dynamics_sim.h File Reference

5.17.1 Detailed Description

Header file for [Dynamics](#) definitions.

Definition in file [dynamics_sim.h](#).

```
#include "control_select.h"
#include "quaternion.h"
#include "trajectory.h"
#include "utils.h"
```

Classes

- class [Dynamics](#)
Dynamics simulation handling class.

Variables

- static const char [header_dynamics_sim_rcsid](#) [] = "\$Id: dynamics_sim.h,v 1.4 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/CVS version.

5.18 gnugraph.cpp File Reference

5.18.1 Detailed Description

Graphics functions.

Definition in file [gnugraph.cpp](#).

```
#include "gnugraph.h"
```

Functions

- short [set_plot2d](#) (const char *title_graph, const char *x_axis_title, const char *y_axis_title, const char *label, [LineType_en](#) enLineType, const Matrix &xdata, const Matrix &ydata, int start_y, int end_y)
- short [set_plot2d](#) (const char *title_graph, const char *x_axis_title, const char *y_axis_title, const vector< char * > label, [LineType_en](#) enLineType, const Matrix &xdata, const Matrix &ydata, const vector< int > &data_select)
- short [set_plot3d](#) (const Matrix &xyz, const string &title_graph, const string &x_axis_title, const string &y_axis_title, const string &z_axis_title)

Variables

- static const char [rcsid](#) [] = "\$Id: gnugraph.cpp,v 1.44 2006/05/19 17:49:58 gourdeau Exp \$"
RCS/CVS version.
- char * [curvetype](#) []

5.18.2 Variable Documentation

5.18.2.1 char* [curvetype](#) []

Initial value:

```
{ "lines",
  "points",
  "linespoints",
  "impulses",
  "dots",
  "steps",
  "boxes" }
```

Definition at line 81 of file gnugraph.cpp.

Referenced by GNUcurve::dump(), and Plot2d::gnuplot().

5.19 gnupgraph.h File Reference

5.19.1 Detailed Description

Header file for graphics definitions.

Definition in file [gnupgraph.h](#).

```
#include <sys/types.h>
#include <unistd.h>
#include <stdio.h>
#include <stdexcept>
#include <boost/shared_ptr.hpp>
#include "newmatap.h"
#include "newmatio.h"
#include <sys/stat.h>
#include <sstream>
#include <vector>
```

Classes

- class [GNUcurve](#)
Object for one curve.
- class [Plot2d](#)
2d plot object.
- class [Plot3d](#)
3d plot object.
- class [IO_matrix_file](#)
Read and write data at every iterations in a file.
- class [Plot_file](#)
Creates a graphic from a data file.

Defines

- `#define GNUPLOT "gnuplot"`

- #define WANT_STRING
- #define WANT_STREAM
- #define WANT_FSTREAM
- #define WANT_MATH
- #define OUT_OF_MEMORY -1
- #define X_Y_DATA_NO_MATCH -2
- #define LABELS_NBR_NO_MATCH -3
- #define NCURVESMAX 10
- #define IO_COULD_NOT_OPEN_FILE -1
- #define IO_MISMATCH_SIZE -2
- #define IO_DATA_EMPTY -3
- #define IO_MISMATCH_ELEMENT_NBR -4
- #define PROBLEM_FILE_READING -5

Typedefs

- typedef boost::shared_ptr< GNUcurve > PSHR_Curve
- typedef std::vector< PSHR_Curve > VectorCurves

Enumerations

- enum LineType_en {
 LINES, DATAPOINTS, LINESPOINTS, IMPULSES,
 DOTS, STEPS, BOXES }

Functions

- short set_plot2d (const char *title_graph, const char *x_axis_title, const char *y_axis_title, const char *label, LineType_en enLineType, const Matrix &xdata, const Matrix &ydata, int start_y, int end_y)
- short set_plot2d (const char *title_graph, const char *x_axis_title, const char *y_axis_title, const vector< char * > label, LineType_en enLineType, const Matrix &xdata, const Matrix &ydata, const vector< int > &data_select)
- short set_plot3d (const Matrix &xyz, const std::string &title_graph, const std::string &x_axis_title, const std::string &y_axis_title, const std::string &z_axis_title)

Variables

- static const char `header_gnugraph_rcsid` [] = "\$Id: gnugraph.h,v 1.13 2006/05/16 19:24:26 gourdeau Exp \$"
RCS/CVS version.

5.20 homogen.cpp File Reference

5.20.1 Detailed Description

Homogen transformation functions.

Definition in file [homogen.cpp](#).

```
#include "utils.h"
```

Functions

- ReturnMatrix [trans](#) (const ColumnVector &a)
Translation.
- ReturnMatrix [rotx](#) (const Real alpha)
Rotation around x axis.
- ReturnMatrix [roty](#) (const Real beta)
Rotation around y axis.
- ReturnMatrix [rotz](#) (const Real gamma)
Rotation around z axis.
- ReturnMatrix [rotk](#) (const Real theta, const ColumnVector &k)
Rotation around arbitrary axis.
- ReturnMatrix [rpy](#) (const ColumnVector &a)
Roll Pitch Yaw rotation.
- ReturnMatrix [eulzxz](#) (const ColumnVector &a)
Euler ZXZ rotation.
- ReturnMatrix [rotd](#) (const Real theta, const ColumnVector &k1, const ColumnVector &k2)
Rotation around an arbitrary line.
- ReturnMatrix [irotk](#) (const Matrix &R)
Obtain axis from a rotation matrix.
- ReturnMatrix [irpy](#) (const Matrix &R)
Obtain Roll, Pitch and Yaw from a rotation matrix.

- ReturnMatrix [ieulzxz](#) (const Matrix &R)
Obtain Roll, Pitch and Yaw from a rotation matrix.

Variables

- static const char [rcsid](#) [] = "\$Id: homogen.cpp,v 1.15 2006/11/15 18:35:17 gourdeau Exp \$"
RCS/ CVS version.

5.21 invkine.cpp File Reference

5.21.1 Detailed Description

Inverse kinematics solutions.

Definition in file [invkine.cpp](#).

```
#include <stdexcept>
#include "robot.h"
```

Defines

- #define [NITMAX](#) 1000
def maximum number of iterations in inv_kin
- #define [ITOL](#) 1e-6
def tolerance for the end of iterations in inv_kin

Variables

- static const char [rcsid](#) [] = "\$Id: invkine.cpp,v 1.8 2006/05/16 16:11:15 gourdeau
Exp \$"
RCS/CVS version.

5.22 kinemat.cpp File Reference

5.22.1 Detailed Description

Kinematics functions.

Definition in file [kinemat.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: kinemat.cpp,v 1.31 2004/08/16 00:37:53 gourdeau Exp \$"
RCS/CVS version.

5.23 quaternion.cpp File Reference

5.23.1 Detailed Description

[Quaternion](#) functions.

Definition in file [quaternion.cpp](#).

```
#include "quaternion.h"
```

Functions

- [Quaternion operator *](#) (const Real c, const [Quaternion](#) &q)
*Overload * operator, multiplication by a scalar.*
- [Quaternion operator *](#) (const [Quaternion](#) &q, const Real c)
*Overload * operator, multiplication by a scalar.*
- [Quaternion operator/](#) (const Real c, const [Quaternion](#) &q)
Overload / operator, division by a scalar.
- [Quaternion operator/](#) (const [Quaternion](#) &q, const Real c)
- ReturnMatrix [Omega](#) (const [Quaternion](#) &q, const [Quaternion](#) &q_dot)
Return angular velocity from a quaternion and it's time derivative.
- short [Integ_quat](#) ([Quaternion](#) &dquat_present, [Quaternion](#) &dquat_past, [Quaternion](#) &quat, const Real dt)
Trapezoidal quaternion integration.
- Real [Integ_Trap_quat_s](#) (const [Quaternion](#) &present, [Quaternion](#) &past, const Real dt)
Trapezoidal quaternion scalar part integration.
- ReturnMatrix [Integ_Trap_quat_v](#) (const [Quaternion](#) &present, [Quaternion](#) &past, const Real dt)
Trapezoidal quaternion vector part integration.
- [Quaternion Slerp](#) (const [Quaternion](#) &q0, const [Quaternion](#) &q1, const Real t)
Spherical Linear Interpolation.
- [Quaternion Slerp_prime](#) (const [Quaternion](#) &q0, const [Quaternion](#) &q1, const Real t)
Spherical Linear Interpolation derivative.

- [Quaternion Squad](#) (const [Quaternion](#) &p, const [Quaternion](#) &a, const [Quaternion](#) &b, const [Quaternion](#) &q, const Real t)
Spherical Cubic Interpolation.
- [Quaternion Squad_prime](#) (const [Quaternion](#) &p, const [Quaternion](#) &a, const [Quaternion](#) &b, const [Quaternion](#) &q, const Real t)
Spherical Cubic Interpolation derivative.

Variables

- static const char [rcsid](#) [] = "\$Id: quaternion.cpp,v 1.18 2005/11/15 19:25:58 gourdeau Exp \$"
RCS/CVS version.

5.23.2 Function Documentation

5.23.2.1 ReturnMatrix Omega (const [Quaternion](#) & q, const [Quaternion](#) & q_dot)

Return angular velocity from a quaternion and it's time derivative.

See [Quaternion::dot](#) for explanation.

Definition at line 560 of file quaternion.cpp.

References `BASE_FRAME`, `Quaternion::E()`, and `Quaternion::v()`.

Referenced by `Spl_Quaternion::quat_w()`.

5.23.2.2 [Quaternion](#) operator * (const Real c, const [Quaternion](#) & q)

Overload * operator, multiplication by a scalar.

$q = [s, v]$ and let $r \in R$. Then $rq = qr = [r, 0][s, v] = [rs, rv]$

The result is not necessarily a unit quaternion even if q is a unit quaternions.

Definition at line 516 of file quaternion.cpp.

Referenced by operator `*`().

5.23.2.3 [Quaternion](#) operator / (const Real c, const [Quaternion](#) & q)

Overload / operator, division by a scalar.

Same explanation as multiplication by scalar.

Definition at line 542 of file quaternion.cpp.

Referenced by operator/().

5.23.2.4 Quaternion Slerp (const Quaternion & q0, const Quaternion & q1, const Real t)

Spherical Linear Interpolation.

Cite_:Dam

The quaternion $q(t)$ interpolate the quaternions q_0 and q_1 given the parameter t along the quaternion sphere.

$$q(t) = c_0(t)q_0 + c_1(t)q_1$$

where c_0 and c_1 are real functions with $0 \leq t \leq 1$. As t varies between 0 and 1. the values $q(t)$ varies uniformly along the circular arc from q_0 and q_1 . The angle between $q(t)$ and q_0 is $\cos(t\theta)$ and the angle between $q(t)$ and q_1 is $\cos((1-t)\theta)$. Taking the dot product of $q(t)$ and q_0 yields

$$\cos(t\theta) = c_0(t) + \cos(\theta)c_1(t)$$

and taking the dot product of $q(t)$ and q_1 yields

$$\cos((1-t)\theta) = \cos(\theta)c_0(t) + c_1(t)$$

These are two equations with c_0 and c_1 . The solution is

$$c_0 = \frac{\sin((1-t)\theta)}{\sin(\theta)}$$

$$c_1 = \frac{\sin(t\theta)}{\sin(\theta)}$$

The interpolation is then

$$\text{Slerp}(q_0, q_1, t) = \frac{q_0 \sin((1-t)\theta) + q_1 \sin(t\theta)}{\sin(\theta)}$$

If q_0 and q_1 are unit quaternions the $q(t)$ is also a unit quaternions. For unit quaternions we have

$$\text{Slerp}(q_0, q_1, t) = q_0(q_0^{-1}q_1)^t$$

For $t = 0$ and $t = 1$ we have

$$q_0 = \text{Slerp}(q_0, q_1, 0)$$

$$q_1 = \text{Slerp}(q_0, q_1, 1)$$

It is customary to choose the sign G on q_1 so that $q_0 \cdot Gq_1 \geq 0$ (the angle between q_0 and Gq_1 is acute). This choice avoids extra spinning caused by the interpolated rotations.

Definition at line 631 of file quaternion.cpp.

References q0.

Referenced by Spl_Quaternion::quat(), Spl_Quaternion::quat_w(), Slerp_prime(), Squad(), and Squad_prime().

5.23.2.5 Quaternion Slerp_prime (const Quaternion & q0, const Quaternion & q1, const Real t)

Spherical Linear Interpolation derivative.

Cite_: Dam

The derivative of the function q^t where q is a constant unit quaternion is

$$\frac{d}{dt}q^t = q^t \log(q)$$

Using the preceding equation the Slerp derivative is then

$$Slerp'(q_0, q_1, t) = q_0(q_0^{-1}q_1)^t \log(q_0^{-1}q_1)$$

It is customary to choose the sign G on q1 so that q0.Gq1 >=0 (the angle between q0 and Gq1 is acute). This choice avoids extra spinning caused by the interpolated rotations. The result is not necessarily a unit quaternion.

Definition at line 692 of file quaternion.cpp.

References q0, and Slerp().

Referenced by Spl_Quaternion::quat_w().

5.23.2.6 Quaternion Squad (const Quaternion & p, const Quaternion & a, const Quaternion & b, const Quaternion & q, const Real t)

Spherical Cubic Interpolation.

Cite_: Dam

Let four quaternions be q_i (p), s_i (a), s_{i+1} (b) and q_{i+1} (q) be the ordered vertices of a quadrilateral. Obtain c from q_i to q_{i+1} interpolation. Obtain d from s_i to s_{i+1} interpolation. Obtain e, the final result, from c to d interpolation.

$$Squad(q_i, s_i, s_{i+1}, q_{i+1}, t) = Slerp(Slerp(q_i, q_{i+1}, t), Slerp(s_i, s_{i+1}, t), 2t(1-t))$$

The intermediate quaternion s_i and s_{i+1} are given by

$$s_i = q_i \exp\left(-\frac{\log(q_i^{-1}q_{i+1}) + \log(q_i^{-1}q_{i-1})}{4}\right)$$

Definition at line 725 of file quaternion.cpp.

References Slerp().

Referenced by Spl_Quaternion::quat(), and Spl_Quaternion::quat_w().

5.23.2.7 Quaternion Squad_prime (const Quaternion & p, const Quaternion & a, const Quaternion & b, const Quaternion & q, const Real t)

Spherical Cubic Interpolation derivative.

Cite_: www.magic-software.com

The derivative of the function q^t where q is a constant unit quaternion is

$$\frac{d}{dt}q^t = q^t \log(q)$$

Recalling that $\log(q) = [0, v\theta]$ (see Quaternion::Log()). If the power is a function we have

$$\frac{d}{dt}q^{f(t)} = f'(t)q^{f(t)}\log(q)$$

If q is a function of time and the power is differentiable function of time we have

$$\frac{d}{dt}(q(t))^{f(t)} = f'(t)(q(t))^{f(t)}\log(q) + f(t)(q(t))^{f(t)-1}q'(t)$$

Using these last three equations Squad derivative can be define. Let $U(t) = \text{Slerp}(p, q, t)$, $V(t) = \text{Slerp}(q, b, t)$, $W(t) = U(t)^{-1}V(t)$. We then have $\text{Squad}(p, a, b, q, t) = \text{Slerp}(U(t), V(t), 2t(1-t)) = U(t)W(t)^{2t(1-t)}$

$$\text{Squad}'(p, a, b, q, t) = \frac{d}{dt}[UW^{2t(1-t)}]$$

$$\text{Squad}'(p, a, b, q, t) = U \frac{d}{dt}[W^{2t(1-t)}] + U' [W^{2t(1-t)}]$$

$$\text{Squad}'(p, a, b, q, t) = U \left[(2-4t)W^{2t(1-t)}\log(W) + 2t(1-t)W^{2t(1-t)-1}W' \right] + U' [W^{2t(1-t)}]$$

where $U' = U\log(p^{-1}q)$, $V' = V\log(a^{-1}b)$, $W' = U^{-1}V' - U^{-2}U'V$

The result is not necessarily a unit quaternion even if all the input quaternions are unit.

Definition at line 751 of file quaternion.cpp.

References Quaternion::i(), Quaternion::power(), and Slerp().

Referenced by Spl_Quaternion::quat_w().

5.24 quaternion.h File Reference

5.24.1 Detailed Description

[Quaternion](#) class.

Definition in file [quaternion.h](#).

```
#include "robot.h"
```

Classes

- class [Quaternion](#)
[Quaternion](#) class definition.

Defines

- #define [BASE_FRAME](#) 0
- #define [BODY_FRAME](#) 1
- #define [EPSILON](#) 0.0000001

Functions

- [Quaternion operator *](#) (const Real c, const [Quaternion](#) &rhs)
*Overload * operator, multiplication by a scalar.*
- [Quaternion operator *](#) (const [Quaternion](#) &lhs, const Real c)
*Overload * operator, multiplication by a scalar.*
- [Quaternion operator/](#) (const Real c, const [Quaternion](#) &rhs)
Overload / operator, division by a scalar.
- [Quaternion operator/](#) (const [Quaternion](#) &lhs, const Real c)
- ReturnMatrix [Omega](#) (const [Quaternion](#) &q, const [Quaternion](#) &q_dot)
Return angular velocity from a quaternion and it's time derivative.
- short [Integ_quat](#) ([Quaternion](#) &dquat_present, [Quaternion](#) &dquat_past, [Quaternion](#) &quat, const Real dt)
Trapezoidal quaternion integration.
- Real [Integ_Trap_quat_s](#) (const [Quaternion](#) &present, [Quaternion](#) &past, const Real dt)

Trapezoidal quaternion scalar part integration.

- ReturnMatrix [Integ_Trap_quat_v](#) (const [Quaternion](#) &present, [Quaternion](#) &past, const Real dt)

Trapezoidal quaternion vector part integration.

- [Quaternion Slerp](#) (const [Quaternion](#) &q0, const [Quaternion](#) &q1, const Real t)

Spherical Linear Interpolation.

- [Quaternion Slerp_prime](#) (const [Quaternion](#) &q0, const [Quaternion](#) &q1, const Real t)

Spherical Linear Interpolation derivative.

- [Quaternion Squad](#) (const [Quaternion](#) &p, const [Quaternion](#) &a, const [Quaternion](#) &b, const [Quaternion](#) &q, const Real t)

Spherical Cubic Interpolation.

- [Quaternion Squad_prime](#) (const [Quaternion](#) &p, const [Quaternion](#) &a, const [Quaternion](#) &b, const [Quaternion](#) &q, const Real t)

Spherical Cubic Interpolation derivative.

Variables

- static const char [header_quat_rcsid](#) [] = "\$Id: quaternion.h,v 1.12 2005/11/15 19:25:58 gourdeau Exp \$"

RCS/CVS version.

5.24.2 Function Documentation

5.24.2.1 ReturnMatrix Omega (const [Quaternion](#) & q, const [Quaternion](#) & q_dot)

Return angular velocity from a quaternion and it's time derivative.

See [Quaternion::dot](#) for explanation.

Definition at line 560 of file quaternion.cpp.

References [BASE_FRAME](#), [Quaternion::E\(\)](#), and [Quaternion::v\(\)](#).

Referenced by [Spl_Quaternion::quat_w\(\)](#).

5.24.2.2 Quaternion operator * (const Real c, const Quaternion & q)

Overload * operator, multiplication by a scalar.

$q = [s, v]$ and let $r \in R$. Then $rq = qr = [r, 0][s, v] = [rs, rv]$

The result is not necessarily a unit quaternion even if q is a unit quaternions.

Definition at line 516 of file quaternion.cpp.

References Quaternion::s(), Quaternion::set_s(), Quaternion::set_v(), and Quaternion::v().

5.24.2.3 Quaternion operator / (const Real c, const Quaternion & q)

Overload / operator, division by a scalar.

Same explanation as multiplication by scalar.

Definition at line 542 of file quaternion.cpp.

References Quaternion::s(), Quaternion::set_s(), Quaternion::set_v(), and Quaternion::v().

5.24.2.4 Quaternion Slerp (const Quaternion & q0, const Quaternion & q1, const Real t)

Spherical Linear Interpolation.

Cite_:Dam

The quaternion $q(t)$ interpolate the quaternions q_0 and q_1 given the parameter t along the quaternion sphere.

$$q(t) = c_0(t)q_0 + c_1(t)q_1$$

where c_0 and c_1 are real functions with $0 \leq t \leq 1$. As t varies between 0 and 1. the values $q(t)$ varies uniformly along the circular arc from q_0 and q_1 . The angle between $q(t)$ and q_0 is $\cos(t\theta)$ and the angle between $q(t)$ and q_1 is $\cos((1-t)\theta)$. Taking the dot product of $q(t)$ and q_0 yields

$$\cos(t\theta) = c_0(t) + \cos(\theta)c_1(t)$$

and taking the dot product of $q(t)$ and q_1 yields

$$\cos((1-t)\theta) = \cos(\theta)c_0(t) + c_1(t)$$

These are two equations with c_0 and c_1 . The solution is

$$c_0 = \frac{\sin((1-t)\theta)}{\sin(\theta)}$$

$$c_1 = \frac{\sin(t\theta)}{\sin(\theta)}$$

The interpolation is then

$$\text{Slerp}(q_0, q_1, t) = \frac{q_0 \sin((1-t)\theta) + q_1 \sin(t\theta)}{\sin(\theta)}$$

If q_0 and q_1 are unit quaternions the $q(t)$ is also a unit quaternions. For unit quaternions we have

$$\text{Slerp}(q_0, q_1, t) = q_0(q_0^{-1}q_1)^t$$

For $t = 0$ and $t = 1$ we have

$$q_0 = \text{Slerp}(q_0, q_1, 0)$$

$$q_1 = \text{Slerp}(q_0, q_1, 1)$$

It is customary to choose the sign G on q_1 so that $q_0.Gq_1 \geq 0$ (the angle between q_0 and Gq_1 is acute). This choice avoids extra spinning caused by the interpolated rotations.

Definition at line 631 of file quaternion.cpp.

References q_0 .

Referenced by `Spl_Quaternion::quat()`, `Spl_Quaternion::quat_w()`, `Slerp_prime()`, `Squad()`, and `Squad_prime()`.

5.24.2.5 Quaternion Slerp_prime (const Quaternion & q_0 , const Quaternion & q_1 , const Real t)

Spherical Linear Interpolation derivative.

Cite_: Dam

The derivative of the function q^t where q is a constant unit quaternion is

$$\frac{d}{dt}q^t = q^t \log(q)$$

Using the preceding equation the Slerp derivative is then

$$\text{Slerp}'(q_0, q_1, t) = q_0(q_0^{-1}q_1)^t \log(q_0^{-1}q_1)$$

It is customary to choose the sign G on q_1 so that $q_0.Gq_1 \geq 0$ (the angle between q_0 and Gq_1 is acute). This choice avoids extra spinning caused by the interpolated rotations. The result is not necessary a unit quaternion.

Definition at line 692 of file quaternion.cpp.

References q_0 , and $\text{Slerp}()$.

Referenced by `Spl_Quaternion::quat_w()`.

5.24.2.6 Quaternion Squad (const Quaternion & p, const Quaternion & a, const Quaternion & b, const Quaternion & q, const Real t)

Spherical Cubic Interpolation.

Cite_: Dam

Let four quaternions be q_i (p), s_i (a), s_{i+1} (b) and q_{i+1} (q) be the ordered vertices of a quadrilateral. Obtain c from q_i to q_{i+1} interpolation. Obtain d from s_i to s_{i+1} interpolation. Obtain e, the final result, from c to d interpolation.

$$Squad(q_i, s_i, s_{i+1}, q_{i+1}, t) = Slerp(Slerp(q_i, q_{i+1}, t), Slerp(s_i, s_{i+1}, t), 2t(1 - t))$$

The intermediate quaternion s_i and s_{i+1} are given by

$$s_i = q_i \exp\left(-\frac{\log(q_i^{-1}q_{i+1}) + \log(q_i^{-1}q_{i-1})}{4}\right)$$

Definition at line 725 of file quaternion.cpp.

References Slerp().

Referenced by Spl_Quaternion::quat(), and Spl_Quaternion::quat_w().

5.24.2.7 Quaternion Squad_prime (const Quaternion & p, const Quaternion & a, const Quaternion & b, const Quaternion & q, const Real t)

Spherical Cubic Interpolation derivative.

Cite_: www.magic-software.com

The derivative of the function q^t where q is a constant unit quaternion is

$$\frac{d}{dt}q^t = q^t \log(q)$$

Recalling that $\log(q) = [0, v\theta]$ (see Quaternion::Log()). If the power is a function we have

$$\frac{d}{dt}q^{f(t)} = f'(t)q^{f(t)}\log(q)$$

If q is a function of time and the power is differentiable function of time we have

$$\frac{d}{dt}(q(t))^{f(t)} = f'(t)(q(t))^{f(t)}\log(q) + f(t)(q(t))^{f(t)-1}q'(t)$$

Using these last three equations Squad derivative can be define. Let $U(t) = Slerp(p, q, t)$, $V(t) = Slerp(q, b, t)$, $W(t) = U(t)^{-1}V(t)$. We then have $Squad(p, a, b, q, t) = Slerp(U(t), V(t), 2t(1 - t)) = U(t)W(t)^{2t(1-t)}$

$$Squad'(p, a, b, q, t) = \frac{d}{dt}[UW^{2t(1-t)}]$$

$$Squad'(p, a, b, q, t) = U \frac{d}{dt} [W^{2t(1-t)}] + U' [W^{2t(1-t)}]$$

$$Squad'(p, a, b, q, t) = U \left[(2-4t)W^{2t(1-t)} \log(W) + 2t(1-t)W^{2t(1-t)-1}W' \right] + U' [W^{2t(1-t)}]$$

where $U' = U \log(p^{-1}q)$, $V' = V \log(a^{-1}, b)$, $W' = U^{-1}V' - U^{-2}U'V$

The result is not necessarily a unit quaternion even if all the input quaternions are unit.

Definition at line 751 of file quaternion.cpp.

References Quaternion::i(), Quaternion::power(), and Slerp().

Referenced by Spl_Quaternion::quat_w().

5.25 robot.cpp File Reference

5.25.1 Detailed Description

Initialisation of different robot class.

Definition in file [robot.cpp](#).

```
#include <time.h>
#include "config.h"
#include "robot.h"
```

Functions

- void [perturb_robot](#) ([Robot_basic](#) &[robot](#), const double f)
Modify a robot.
- bool [Rhino_DH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Rhino on DH notation.
- bool [Puma_DH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Puma on DH notation.
- bool [Schilling_DH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Schilling on DH notation.
- bool [Rhino_mDH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Rhino on modified DH notation.
- bool [Puma_mDH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Puma on modified DH notation.
- bool [Schilling_mDH](#) (const [Robot_basic](#) &[robot](#))
Return true if the robot is like a Schilling on modified DH notation.

Variables

- static const char [rcsid](#) [] = "\$Id: robot.cpp,v 1.50 2006/05/16 19:24:26 gourdeau
Exp \$"
RCS/CVS version.

- Real `fourbyfourident` [] = { 1.0,0.0,0.0,0.0,0.0,0.0,1.0,0.0,0.0,0.0,0.0,1.0,0.0,0.0,0.0,0.0,1.0 }

Used to initialize a 4×4 matrix.

- Real `threebythreeident` [] = { 1.0,0.0,0.0,0.0,1.0,0.0,0.0,0.0,1.0 }

Used to initialize a 3×3 matrix.

5.25.2 Function Documentation

5.25.2.1 void perturb_robot (Robot_basic & robot, const double f)

Modify a robot.

Parameters:

robot,: `Robot_basic` reference.

f,: Percentage of erreur between 0 and 1.

f represents an error to added on the robot inertial parameter. f is between 0 (no error) and 1 (100% error).

Definition at line 1446 of file robot.cpp.

References `Link::get_B()`, `Link::get_Cf()`, `Robot_basic::get_dof()`, `Robot_basic::get_fix()`, `Link::get_I()`, `Link::get_Im()`, `Link::get_m()`, `Robot_basic::links`, `robot`, `Link::set_B()`, `Link::set_Cf()`, `Link::set_I()`, `Link::set_Im()`, and `Link::set_m()`.

5.25.2.2 bool Puma_DH (const Robot_basic & robot)

Return true if the robot is like a Puma on DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1516 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `Robot::robotType_inv_kin()`.

5.25.2.3 bool Puma_mDH (const Robot_basic & robot)

Return true if the robot is like a Puma on modified DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1615 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `mRobot_min_para::robotType_inv_kin()`, and `mRobot::robotType_inv_kin()`.

5.25.2.4 `bool Rhino_DH (const Robot_basic & robot)`

Return true if the robot is like a Rhino on DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1483 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `Robot::robotType_inv_kin()`.

5.25.2.5 `bool Rhino_mDH (const Robot_basic & robot)`

Return true if the robot is like a Rhino on modified DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1583 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `mRobot_min_para::robotType_inv_kin()`, and `mRobot::robotType_inv_kin()`.

5.25.2.6 `bool Schilling_DH (const Robot_basic & robot)`

Return true if the robot is like a Schilling on DH notation.

Compare the robot DH table with the Schilling DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1549 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by Robot::robotType_inv_kin().

5.25.2.7 bool Schilling_mDH (const Robot_basic & robot)

Return true if the robot is like a Schilling on modified DH notation.

Compare the robot DH table with the Schilling DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1649 of file robot.cpp.

References Link::get_a(), Link::get_alpha(), Link::get_d(), Robot_basic::get_dof(), Link::get_joint_type(), isZero(), Robot_basic::links, and robot.

Referenced by mRobot_min_para::robotType_inv_kin(), and mRobot::robotType_inv_kin().

5.26 robot.h File Reference

5.26.1 Detailed Description

Robots class definitions.

Definition in file [robot.h](#).

```
#include "utils.h"
```

Classes

- class [Link](#)
Link definitions.
- class [Robot_basic](#)
Virtual base robot class.
- class [Robot](#)
DH notation robot class.
- class [mRobot](#)
Modified DH notation robot class.
- class [mRobot_min_para](#)
Modified DH notation and minimal inertial parameters robot class.

Functions

- void [perturb_robot](#) ([Robot_basic](#) &robot, const double f=0.1)
Modify a robot.
- bool [Rhino_DH](#) (const [Robot_basic](#) &robot)
Return true if the robot is like a Rhino on DH notation.
- bool [Puma_DH](#) (const [Robot_basic](#) &robot)
Return true if the robot is like a Puma on DH notation.
- bool [Schilling_DH](#) (const [Robot_basic](#) &robot)
Return true if the robot is like a Schilling on DH notation.
- bool [Rhino_mDH](#) (const [Robot_basic](#) &robot)

Return true if the robot is like a Rhino on modified DH notation.

- bool **Puma_mDH** (const **Robot_basic** &robot)

Return true if the robot is like a Puma on modified DH notation.

- bool **Schilling_mDH** (const **Robot_basic** &robot)

Return true if the robot is like a Schilling on modified DH notation.

Variables

- static const char **header_rcsid** [] = "\$Id: robot.h,v 1.52 2006/05/16 16:11:15 gourdeau Exp \$"

RCS/CVS version.

5.26.2 Function Documentation

5.26.2.1 void perturb_robot (**Robot_basic** & robot, const double f)

Modify a robot.

Parameters:

robot,: **Robot_basic** reference.

f,: Percentage of erreur between 0 and 1.

f represents an error to added on the robot inertial parameter. f is between 0 (no error) and 1 (100% error).

Definition at line 1446 of file robot.cpp.

References **Link::get_B()**, **Link::get_Cf()**, **Robot_basic::get_dof()**, **Robot_basic::get_fix()**, **Link::get_I()**, **Link::get_Im()**, **Link::get_m()**, **Robot_basic::links**, **robot**, **Link::set_B()**, **Link::set_Cf()**, **Link::set_I()**, **Link::set_Im()**, and **Link::set_m()**.

5.26.2.2 bool Puma_DH (const **Robot_basic** & robot)

Return true if the robot is like a Puma on DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1516 of file robot.cpp.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `Robot::robotType_inv_kin()`.

5.26.2.3 `bool Puma_mDH (const Robot_basic & robot)`

Return true if the robot is like a Puma on modified DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1615 of file `robot.cpp`.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `mRobot::robotType_inv_kin()`, and `mRobot_min_para::robotType_inv_kin()`.

5.26.2.4 `bool Rhino_DH (const Robot_basic & robot)`

Return true if the robot is like a Rhino on DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1483 of file `robot.cpp`.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `Robot::robotType_inv_kin()`.

5.26.2.5 `bool Rhino_mDH (const Robot_basic & robot)`

Return true if the robot is like a Rhino on modified DH notation.

Compare the robot DH table with the Puma DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1583 of file `robot.cpp`.

References `Link::get_a()`, `Link::get_alpha()`, `Link::get_d()`, `Robot_basic::get_dof()`, `Link::get_joint_type()`, `isZero()`, `Robot_basic::links`, and `robot`.

Referenced by `mRobot::robotType_inv_kin()`, and `mRobot_min_para::robotType_inv_kin()`.

5.26.2.6 bool Schilling_DH (const Robot_basic & robot)

Return true if the robot is like a Schilling on DH notation.

Compare the robot DH table with the Schilling DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1549 of file robot.cpp.

References Link::get_a(), Link::get_alpha(), Link::get_d(), Robot_basic::get_dof(), Link::get_joint_type(), isZero(), Robot_basic::links, and robot.

Referenced by Robot::robotType_inv_kin().

5.26.2.7 bool Schilling_mDH (const Robot_basic & robot)

Return true if the robot is like a Schilling on modified DH notation.

Compare the robot DH table with the Schilling DH table. The function return true if the tables are similar (same alpha and similar a and d parameters).

Definition at line 1649 of file robot.cpp.

References Link::get_a(), Link::get_alpha(), Link::get_d(), Robot_basic::get_dof(), Link::get_joint_type(), isZero(), Robot_basic::links, and robot.

Referenced by mRobot::robotType_inv_kin(), and mRobot_min_para::robotType_inv_kin().

5.27 rtest.cpp File Reference

5.27.1 Detailed Description

A test file.

Compares results with Peter Corke MATLAB toolbox

Definition in file [rtest.cpp](#).

```
#include "robot.h"
#include "quaternion.h"
#include "precisio.h"
#include <fstream>
```

Functions

- int [main](#) (void)

Variables

- static const char [rcsid](#) [] = "\$Id: rtest.cpp,v 1.15 2005/07/01 17:44:53 gourdeau Exp \$"
RCS/CVS version.
- const Real [PUMA560_data_DH](#) []
- Real [PUMA560_data_mDH](#) []
- const Real [PUMA560_motor](#) []
- const Real [STANFORD_data_DH](#) []

5.27.2 Variable Documentation

5.27.2.1 const Real [PUMA560_data_DH](#) []

Initial value:

```
{0, 0, 0, 0, M_PI/2.0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0.35, 0, 0, 0,
0, 0, 0, 0.4318, 0, 0, 0, 0, 17.4, -0.3638, 0.006, 0.2275, 0.13, 0, 0, 0.524, 0, 0.539, 0,
0, 0, 0.15005, 0.0203, -M_PI/2.0, 0, 0, 0, 4.8, -0.0203, -0.0141, 0.07, 0.066, 0, 0, 0.086, 0, 0.0125,
0, 0, 0.4318, 0.0, M_PI/2.0, 0, 0, 0, 0.82, 0, 0.019, 0, 0.0018, 0, 0, 0.0013, 0, 0.0018, 0,
0, 0, 0, 0.0, -M_PI/2.0, 0, 0, 0, 0.34, 0.0, 0.0, 0.0, 0.0003, 0.0, 0.0, 0.0004, 0.0, 0.0003, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0.09, 0.0, 0.0, 0.032, 0.00015, 0.0, 0.0, 0.00015, 0.0, 0.00004, 0}
```

Definition at line 61 of file rtest.cpp.

Referenced by main().

5.27.2.2 Real PUMA560_data_mDH[]

Initial value:

```
{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0.35, 0,
0, 0, 0, 0.0, -M_PI/2, 0, 0, 0, 17.4, 0.068, 0.006, -0.016, 0.13, 0, 0, 0.524, 0, 0.539, 0,
0, 0, -0.15005, 0.4318, 0, 0, 0, 0, 4.8, 0, -0.070, 0.014, 0.066, 0, 0, 0.0125, 0, 0.066, 0,
0, 0, -0.4318, 0.0203, -M_PI/2.0, 0, 0, 0, 0.82, 0.0, 0.0, -0.019, 0.0018, 0, 0, 0.0018, 0, 0,
0, 0, 0, 0, M_PI/2.0, 0, 0, 0, 0.34, 0, 0, 0.0, 0.0003, 0, 0, 0.0003, 0, 0.0004, 0,
0, 0, 0, 0, -M_PI/2, 0, 0, 0, 0.09, 0, 0, 0.032, 0.00015, 0, 0, 0.00015, 0, 0.00004, 0}
```

Definition at line 68 of file rtest.cpp.

Referenced by main().

5.27.2.3 const Real PUMA560_motor[]

Initial value:

```
{200e-6, -62.6111, 1.48e-3, 0,
200e-6, 107.815, .817e-3, 0,
200e-6, -53.7063, 1.38e-3, 0,
33e-6, 76.0364, 71.2e-6, 0,
33e-6, 71.923, 82.6e-6, 0,
33e-6, 76.686, 36.7e-6, 0}
```

Definition at line 76 of file rtest.cpp.

5.27.2.4 const Real STANFORD_data_DH[]

Initial value:

```
{0.0, 0.0, 0.4120, 0.0, -M_PI/2, 0,0,0,9.29, 0.0, 0.0175, -0.1105, 0.276, 0.0, 0, 0.255, 0.0,
0.0, 0.0, 0.1540, 0.0, M_PI/2.0, 0,0,0,5.01, 0.0, -1.054, 0.0, 0.108, 0.0, 0.0, 0.018, 0.0,
1.0, -M_PI/2.0, 0.0, 0.0, 0.0, 0,0,0,4.25, 0.0, 0.0, -6.447, 2.51, 0.0, 0.0, 2.51, 0.0, 0.0,
0.0, 0.0, 0.0, 0.0, -M_PI/2.0, 0,0,0,1.08, 0.0, 0.092, -0.054, 0.002, 0.0, 0.0, 0.001, 0.0,
0.0, 0.0, 0.0, 0.0, M_PI/2.0, 0,0,0,0.63, 0.0, 0.0, 0.566, 0.003, 0.0, 0.0, 0.003, 0.0, 0.0,
0.0, 0.0, 0.2630, 0.0, 0.0, 0,0,0,0.51, 0.0, 0.0, 1.5540, 0.013, 0.0, 0.0, 0.013, 0.0, 0.000
```

Definition at line 84 of file rtest.cpp.

Referenced by main().

5.28 sensitiv.cpp File Reference

5.28.1 Detailed Description

Delta torque (linearized dynamics).

Definition in file [sensitiv.cpp](#).

```
#include "robot.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: sensitiv.cpp,v 1.13 2004/07/06 02:16:37 gourdeau Exp \$"
RCS/CVS version.

5.29 stewart.cpp File Reference

5.29.1 Detailed Description

Initialisation of [Stewart](#) platform class.

Definition in file [stewart.cpp](#).

```
#include "config.h"
```

```
#include "stewart.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: stewart.cpp,v 1.6 2006/05/16 19:24:26 gourdeau
Exp \$"

RCS/CVS version.

5.30 `stewart.h` File Reference

5.30.1 Detailed Description

[Stewart](#) class definitions.

Definition in file [stewart.h](#).

```
#include "utils.h"
```

Classes

- class [LinkStewart](#)
LinkStewart definitions.
- class [Stewart](#)
Stewart definitions.

Variables

- static const char [header_stewart_rcsid](#) [] = "\$Id: stewart.h,v 1.2 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/CVS version.

5.31 trajectory.cpp File Reference

5.31.1 Detailed Description

Trajectory member functions.

Definition in file [trajectory.cpp](#).

```
#include "trajectory.h"
```

Variables

- static const char [rcsid](#) [] = "\$Id: trajectory.cpp,v 1.8 2006/05/16 19:24:26 gourdeau Exp \$"

RCS/CVS version.

5.32 trajectory.h File Reference

5.32.1 Detailed Description

Header file for trajectory generation class.

Definition in file [trajectory.h](#).

```
#include <sstream>
#include <map>
#include "quaternion.h"
#include "utils.h"
```

Classes

- class [Spl_cubic](#)
Natural cubic splines class.
- class [Spl_path](#)
Cartesian or joint space trajectory.
- class [Spl_Quaternion](#)
Cubic quaternions spline.
- class [Trajectory_Select](#)
Trajectory class selection.

Defines

- #define [K_ZERO](#) 1
- #define [BAD_DATA](#) -1
- #define [EXTRAPOLLATION](#) -2
- #define [NOT_IN_RANGE](#) -3
- #define [NONE](#) 0
- #define [JOINT_SPACE](#) 1
- #define [CARTESIAN_SPACE](#) 2

Typedefs

- typedef std::map< Real, ColumnVector, less< Real > > [point_map](#)

Data at control points.

- typedef std::map< Real, Quaternion, less< Real > > quat_map

Data at control points.

Variables

- static const char header_trajectory_rcsid [] = "\$Id: trajectory.h,v 1.10 2006/05/16 19:24:26 gourdeau Exp \$"

RCS/CVS version.

5.33 utils.cpp File Reference

5.33.1 Detailed Description

Utility functions.

Definition in file [utils.cpp](#).

```
#include "utils.h"
```

Defines

- #define [PGROW](#) -0.20
- #define [PSHRNK](#) -0.25
- #define [FCOR](#) 0.06666666
- #define [SAFETY](#) 0.9
- #define [ERRCON](#) 6.0E-4
- #define [MAXSTP](#) 10000
- #define [TINY](#) 1.0e-30

Functions

- ReturnMatrix [x_prod_matrix](#) (const ColumnVector &x)
Cross product matrix.
- ReturnMatrix [pinv](#) (const Matrix &M)
Matrix pseudo inverse using SVD.
- ReturnMatrix [Integ_Trap](#) (const ColumnVector &present, ColumnVector &past, const Real dt)
Trapezoidal integration.
- void [Runge_Kutta4_Real_time](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin, bool &exit, bool &init), const Matrix &x0, Real to, Real tf, int nsteps)
Fixed step size fourth-order Runge-Kutta integrator.
- void [Runge_Kutta4_Real_time](#) (ReturnMatrix(*xdot)(const Real time, const Matrix &xin), const Matrix &x0, const Real to, const Real tf, const int nsteps)
- void [Runge_Kutta4](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin), const Matrix &x0, Real to, Real tf, int nsteps, RowVector &tout, Matrix &xout)
Fixed step size fourth-order Runge-Kutta integrator.

- ReturnMatrix [rk4](#) (const Matrix &x, const Matrix &dxdt, Real t, Real h, ReturnMatrix(*xdot)(Real time, const Matrix &xin))

Compute one Runge-Kutta fourth order step.

- void [rkqc](#) (Matrix &x, Matrix &dxdt, Real &t, Real htry, Real eps, Matrix &xscal, Real &hdid, Real &hnext, ReturnMatrix(*xdot)(Real time, const Matrix &xin))

Compute one adaptive step based on two rk4.

- void [odeint](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin), Matrix &xo, Real to, Real tf, Real eps, Real h1, Real hmin, int &nok, int &nbad, RowVector &tout, Matrix &xout, Real dtsav)

Integrate the ordinary differential equation xdot from time to to time tf using an adaptive step size strategy.

- ReturnMatrix [sign](#) (const Matrix &x)

Sign of a matrix.

- short [sign](#) (const Real x)

Sign of real.

Variables

- static const char [rcsid](#) [] = "\$Id: utils.cpp,v 1.26 2006/05/16 16:11:15 gourdeau Exp \$"

RCS/ CVS version.

5.33.2 Function Documentation

5.33.2.1 void odeint (ReturnMatrix(*) (Real time, const Matrix &xin) xdot, Matrix & xo, Real to, Real tf, Real eps, Real h1, Real hmin, int & nok, int & nbad, RowVector & tout, Matrix & xout, Real dtsav)

Integrate the ordinary differential equation xdot from time to to time tf using an adaptive step size strategy.

adapted from: Numerical Recipes in C, The Art of Scientific Computing, Press, William H. and Flannery, Brian P. and Teukolsky, Saul A. and Vetterling, William T., Cambridge University Press, 1988.

Definition at line 347 of file utils.cpp.

References MAXSTP, rkqc(), and TINY.

Referenced by dynamics_demo().

5.33.2.2 ReturnMatrix pinv (const Matrix & M)

Matrix pseudo inverse using SVD.

If $A = U^*QV$ is a singular value decomposition of A, then $A^\dagger = V^*Q^\dagger U$ where X^*

is the conjugate transpose of X and $Q^\dagger = \begin{bmatrix} 1/\sigma_1 & & & \\ & 1/\sigma_2 & & \\ & & \ddots & \\ & & & 0 \end{bmatrix}$ where the $1/\sigma_i$

are replaced by 0 when $1/\sigma_i < tol$

Definition at line 99 of file utils.cpp.

References epsilon, and pinv().

Referenced by pinv().

5.33.2.3 ReturnMatrix rk4 (const Matrix & x, const Matrix & dxdt, Real t, Real h, ReturnMatrix(*) (Real time, const Matrix & xin) xdot)

Compute one Runge-Kutta fourth order step.

adapted from: Numerical Recipes in C, The Art of Scientific Computing, Press, William H. and Flannery, Brian P. and Teukolsky, Saul A. and Vetterling, William T., Cambridge University Press, 1988.

Definition at line 260 of file utils.cpp.

Referenced by rkqc().

5.33.2.4 void rkqc (Matrix & x, Matrix & dxdt, Real & t, Real htry, Real eps, Matrix & xscal, Real & hdid, Real & hnext, ReturnMatrix(*) (Real time, const Matrix & xin) xdot)

Compute one adaptive step based on two rk4.

adapted from: Numerical Recipes in C, The Art of Scientific Computing, Press, William H. and Flannery, Brian P. and Teukolsky, Saul A. and Vetterling, William T., Cambridge University Press, 1988.

Definition at line 295 of file utils.cpp.

References ERRCON, FCOR, PGROW, PSHRNK, rk4(), and SAFETY.

Referenced by odeint().

5.34 utils.h File Reference

5.34.1 Detailed Description

Utility header file.

Definition in file [utils.h](#).

```
#include <stdio.h>
#include <limits>
#include "newmatap.h"
#include "newmatio.h"
```

Defines

- #define [WANT_STRING](#)
- #define [WANT_STREAM](#)
- #define [WANT_FSTREAM](#)
- #define [WANT_MATH](#)
- #define [M_PI](#) 3.14159265358979
- #define [GRAVITY](#) 9.81

Functions

- double [deg2rad](#) (const double angle_deg)
- double [rad2deg](#) (const double angle_rad)
- ReturnMatrix [x_prod_matrix](#) (const ColumnVector &x)
Cross product matrix.
- ReturnMatrix [pinv](#) (const Matrix &M)
Matrix pseudo inverse using SVD.
- ReturnMatrix [Integ_Trap](#) (const ColumnVector &present, ColumnVector &past, const Real dt)
Trapezoidal integration.
- void [Runge_Kutta4](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin), const Matrix &xo, Real to, Real tf, int nsteps, RowVector &tout, Matrix &xout)
Fixed step size fourth-order Runge-Kutta integrator.
- void [Runge_Kutta4_Real_time](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin), const Matrix &xo, Real to, Real tf, int nsteps)

- void [Runge_Kutta4_Real_time](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin, bool &exit, bool &init), const Matrix &xo, Real to, Real tf, int nsteps)

Fixed step size fourth-order Runge-Kutta integrator.

- void [odeint](#) (ReturnMatrix(*xdot)(Real time, const Matrix &xin), Matrix &xo, Real to, Real tf, Real eps, Real h1, Real hmin, int &nok, int &nbad, RowVector &tout, Matrix &xout, Real dtsav)

Integrate the ordinary differential equation xdot from time to to time tf using an adaptive step size strategy.

- ReturnMatrix [sign](#) (const Matrix &x)

Sign of a matrix.

- short [sign](#) (const Real x)

Sign of real.

- bool [isZero](#) (const double x)

- ReturnMatrix [trans](#) (const ColumnVector &a)

Translation.

- ReturnMatrix [rotx](#) (const Real alpha)

Rotation around x axis.

- ReturnMatrix [roty](#) (const Real beta)

Rotation around x axis.

- ReturnMatrix [rotz](#) (const Real gamma)

Rotation around z axis.

- ReturnMatrix [rotk](#) (const Real theta, const ColumnVector &k)

Rotation around arbitrary axis.

- ReturnMatrix [rpy](#) (const ColumnVector &a)

Roll Pitch Yaw rotation.

- ReturnMatrix [eulzxz](#) (const ColumnVector &a)

Euler ZXZ rotation.

- ReturnMatrix [rotd](#) (const Real theta, const ColumnVector &k1, const ColumnVector &k2)

Rotation around an arbitrary line.

- ReturnMatrix [irotk](#) (const Matrix &R)
Obtain axis from a rotation matrix.
- ReturnMatrix [irpy](#) (const Matrix &R)
Obtain Roll, Pitch and Yaw from a rotation matrix.
- ReturnMatrix [ieulzxz](#) (const Matrix &R)
Obtain Roll, Pitch and Yaw from a rotation matrix.

Variables

- static const char [header_utils_rcsid](#) [] = "\$Id: utils.h,v 1.10 2006/05/16 16:11:15 gourdeau Exp \$"
RCS/CVS version.
- Real [fourbyfourident](#) []
Used to initialize a 4×4 matrix.
- Real [threebythreeident](#) []
Used to initialize a 3×3 matrix.
- const double [epsilon](#) = 0.0000001

5.34.2 Function Documentation

5.34.2.1 void odeint (ReturnMatrix(*) (Real time, const Matrix &xin) xdot, Matrix &xo, Real to, Real tf, Real eps, Real h1, Real hmin, int &nok, int &nbad, RowVector &tout, Matrix &xout, Real dtsav)

Integrate the ordinary differential equation xdot from time to to time tf using an adaptive step size strategy.

adapted from: Numerical Recipes in C, The Art of Scientific Computing, Press, William H. and Flannery, Brian P. and Teukolsky, Saul A. and Vetterling, William T., Cambridge University Press, 1988.

Definition at line 347 of file utils.cpp.

References MAXSTP, rkqc(), and TINY.

Referenced by dynamics_demo().

5.34.2.2 ReturnMatrix pinv (const Matrix & M)

Matrix pseudo inverse using SVD.

If $A = U^* Q V$ is a singular value decomposition of A, then $A^\dagger = V^* Q^\dagger U$ where X^*

is the conjugate transpose of X and $Q^\dagger = \begin{bmatrix} 1/\sigma_1 & & & \\ & 1/\sigma_2 & & \\ & & \ddots & \\ & & & 0 \end{bmatrix}$ where the $1/\sigma_i$

are replaced by 0 when $1/\sigma_i < tol$

Definition at line 99 of file utils.cpp.

References epsilon, and pinv().

Referenced by pinv().

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